

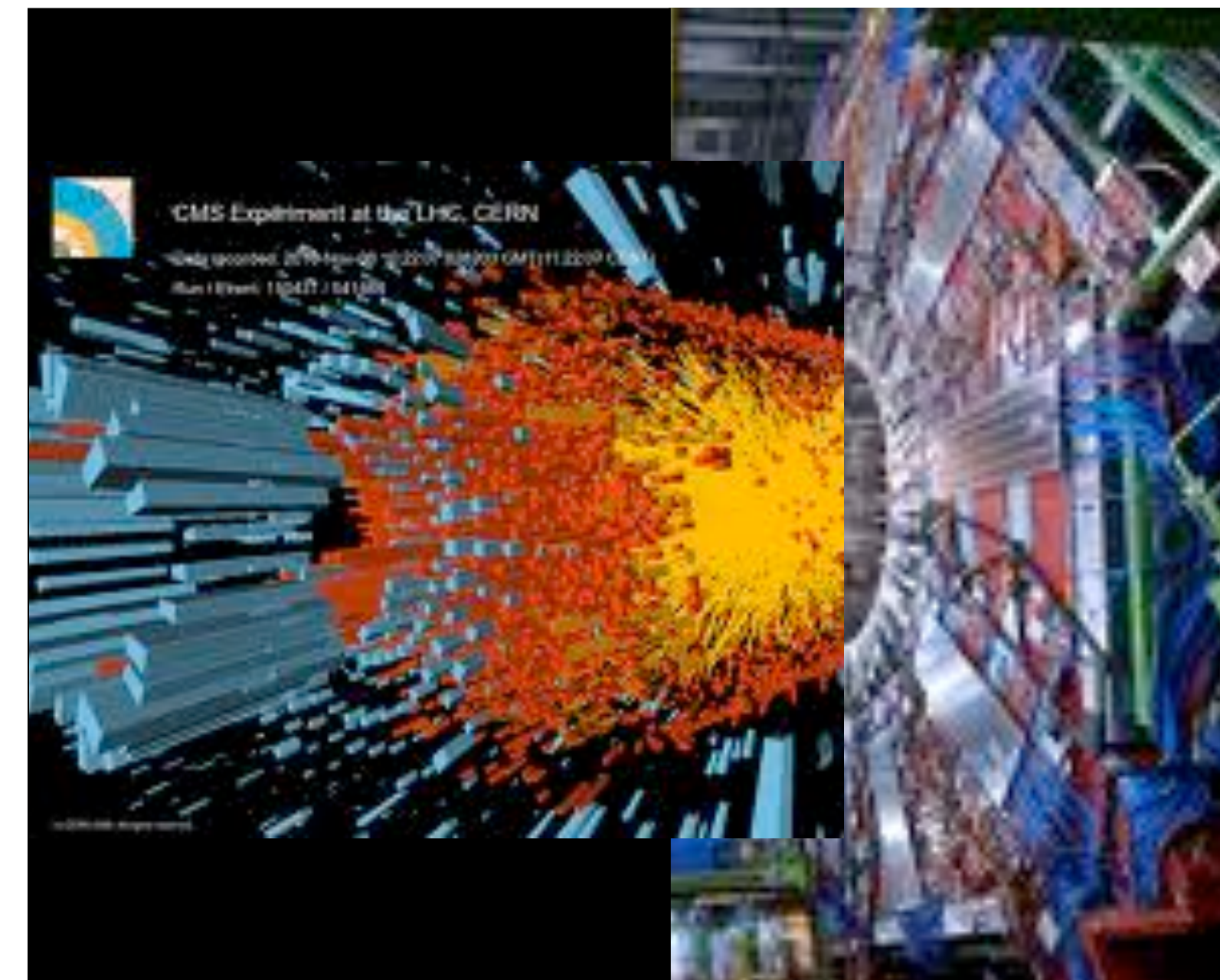
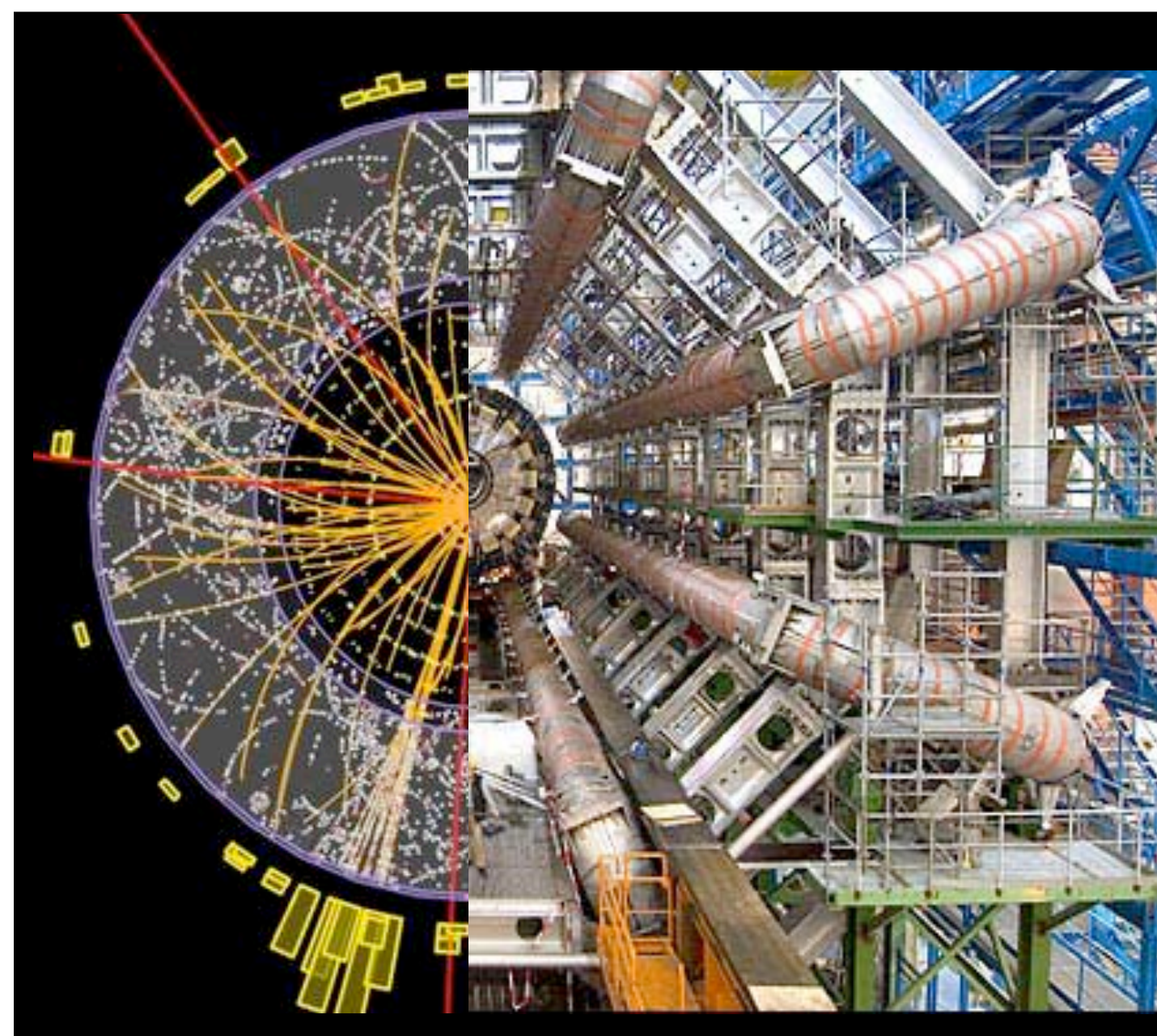
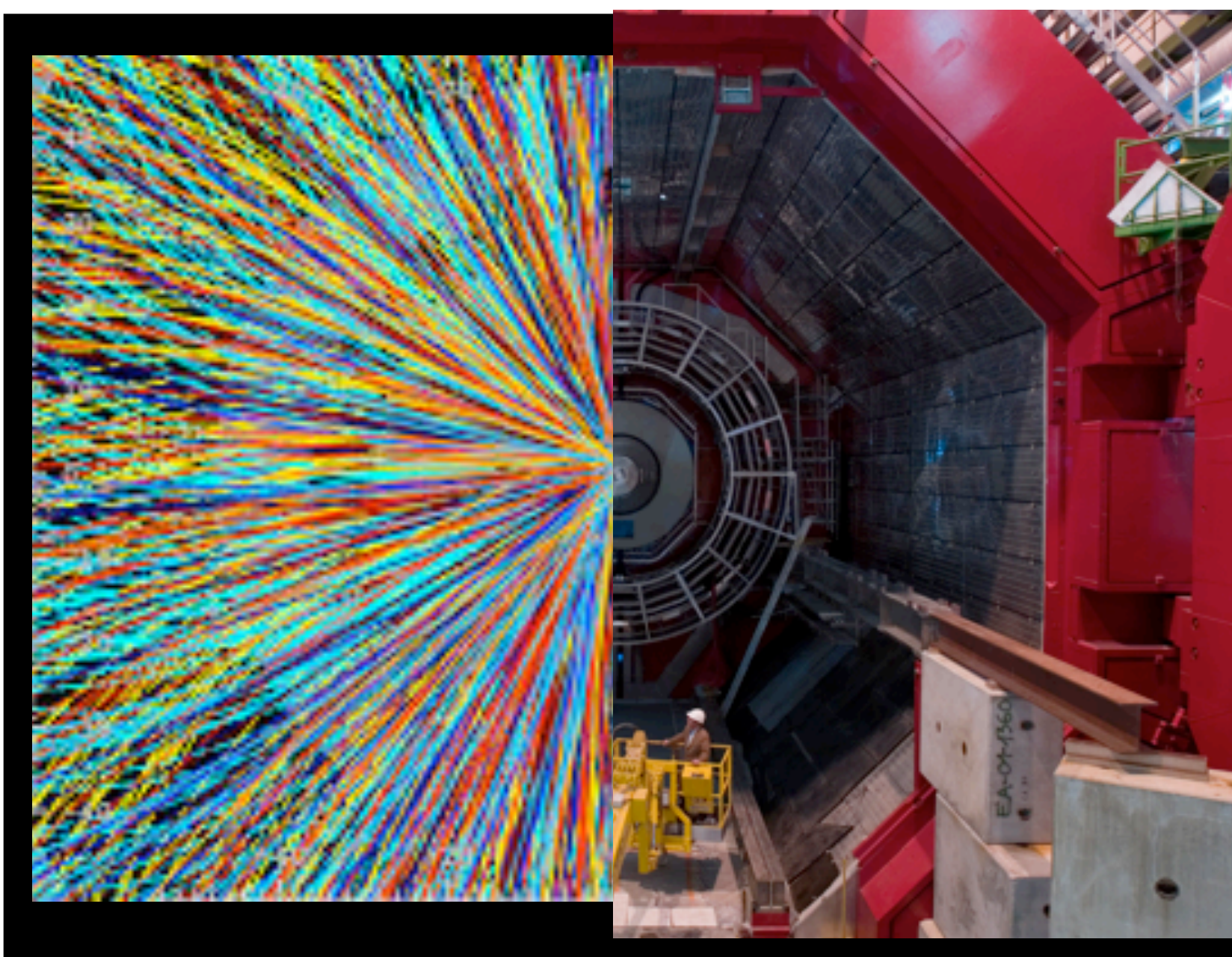
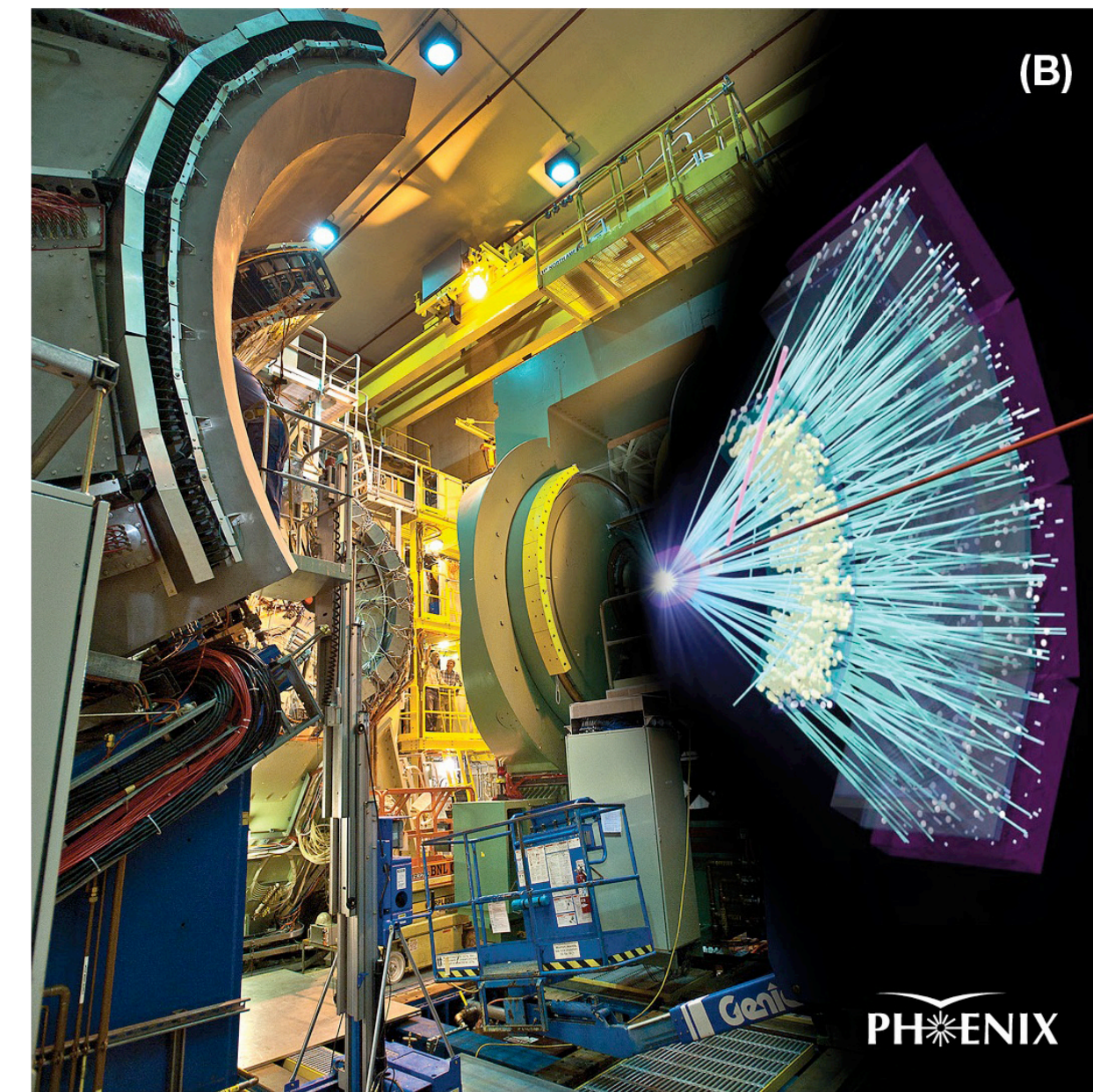
Relativistic Heavy Ions

Helen Caines (she/her), Wright Lab, Yale University

Lecture 1: Creating the QGP

Lecture 2: Using Hard Probes

Lecture 3: Unexpected Physics & the Future



Relativistic Heavy Ions I - The What, Why, Where, and How of It All

By the end of today's talk I aim for you to be able to discuss at dinner :

The Basics of QCD, Asymptotic Freedom, and the QGP
The Necessary Conditions to Make the QGP
Evidence for QGP Creation in Heavy-Ion Collisions
Our Current Understanding of the QGP's Evolution
Critical Points and How to Search for Them

Color confinement - QCD

Quarks seem to be confined within colorless hadrons

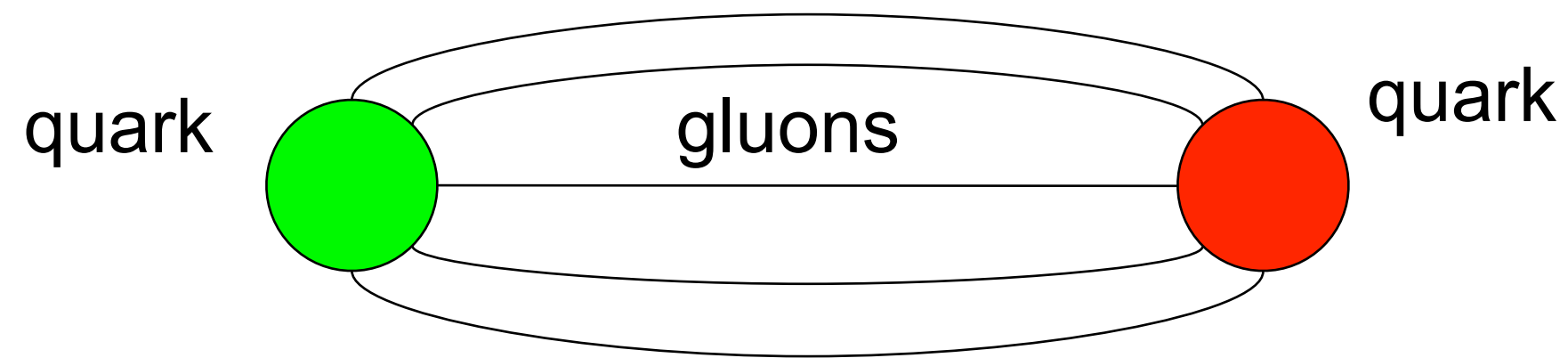
Nobody ever succeeded in detecting an isolated quark or gluon

One half of the fundamental fermions are not directly observable.

Why? The strong force

To understand the strong force and confinement:
Create and study a system of deconfined
colored quarks and gluons

We don't see free quarks

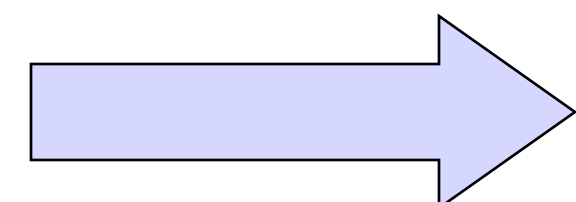


Strong force becomes ~constant at ~size of a hadron which is ~1 fm (10^{-15} m)

$$1 \frac{GeV}{fm} = \frac{10^9 eV}{10^{-15} m} \times \frac{1.6 \times 10^{-19} J}{eV} = 1.6 \times 10^5 N$$

Compare to gravitational force at Earth's surface

$$F = 1.6 \times 10^5 N = M \times g = M \times 9.8 m/s^2$$

 $M = 16,300 kg$

Quarks exert 16 metric tons of force on each other!

Asymptotic freedom

Coupling constant is not a “constant”

Runs with Q^2 (mtm transfer)
accounts for vacuum polarisation

$$\alpha_s(Q^2) = \frac{\alpha_s(\mu^2)}{[1 + (\alpha_s(\mu^2) \frac{(33-2n_f)}{12\pi}) \ln(Q^2/\mu^2)]}$$

$\alpha_s(\mu^2) \sim 1$!!

μ^2 : renormalization scale

33 : $11 * \#$ colors

n_f : # quark flavors = (3-6)

$(33-(2*6))/(12\pi)$ is positive

$\alpha_s(Q^2) \rightarrow 0$, as $Q \rightarrow \infty$, $r \rightarrow 0$

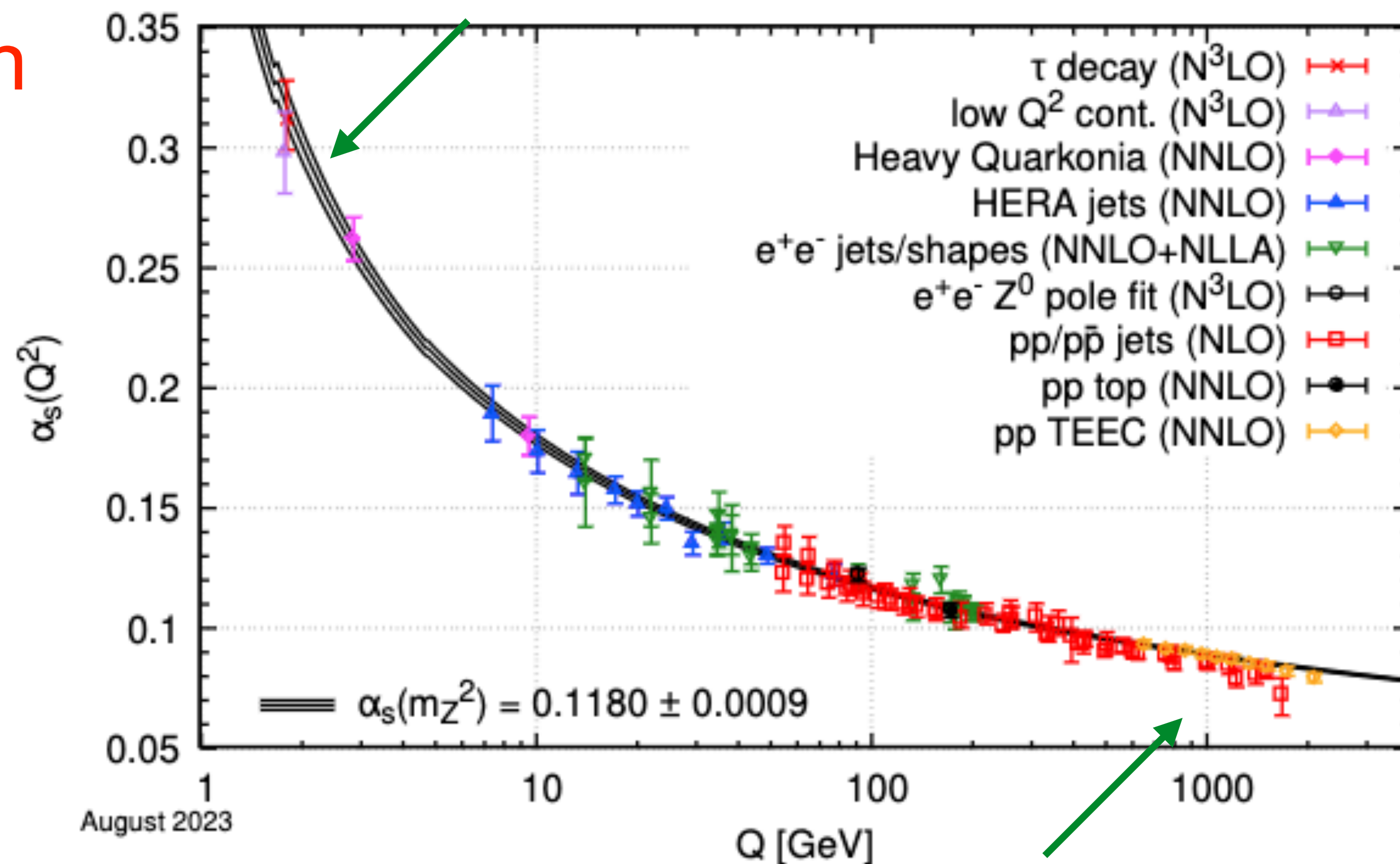
Coupling very weak

→ partons are essentially free

Asymptotic Freedom

Measured experimentally

Small E/large r scales - coupling constant large - perturbative corrections are large - confinement/hadrons



Large E/small r scales - coupling constant small - perturbative calculations valid - deconfinement/asymptotic freedom

Asymptotic freedom

Measured experimentally

Coupling

Runs with accounts

$$\alpha_s(Q^2) = \frac{4\pi}{(33 - 2 \cdot n_f) \ln(Q^2/\mu^2)}$$

α_s
 μ^2
33
 n_f

(33 - (2 * 6))

$\alpha_s(Q^2)$

Coupling

→ partons



"for the discovery of asymptotic freedom in the theory of the strong interaction"



David J. Gross



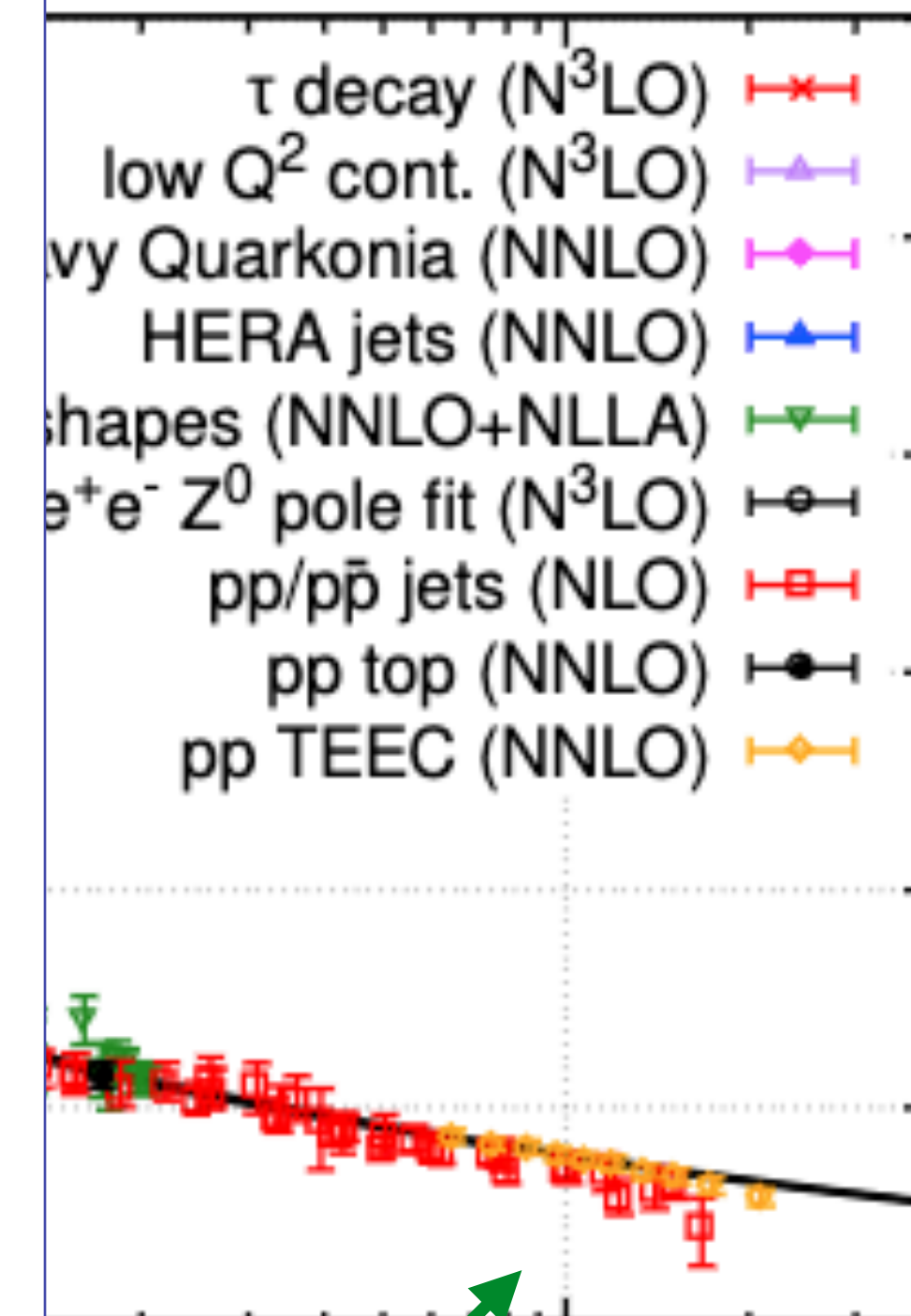
H. David Politzer



Frank Wilczek

Asymptotic Freedom

Coupling constant calculations are large -



coupling constant calculations valid - deconfinement/asymptotic freedom

Asymptotic freedom vs Debye screening

Asymptotic freedom occurs at very high Q^2

Problem: Q^2 much higher than available in the lab.

So how to create and study this new phase of matter?

Solution: Use effects of **Debye screening**

In the presence of many **color** charges (charge density n), the **short** range term of the strong potential is modified:

$$V_s(r) \propto \frac{1}{r} \implies \frac{1}{r} \exp\left[-\frac{r}{r_D}\right]$$

where $r_D = \frac{1}{3\sqrt{n}}$ is the **Debye radius**

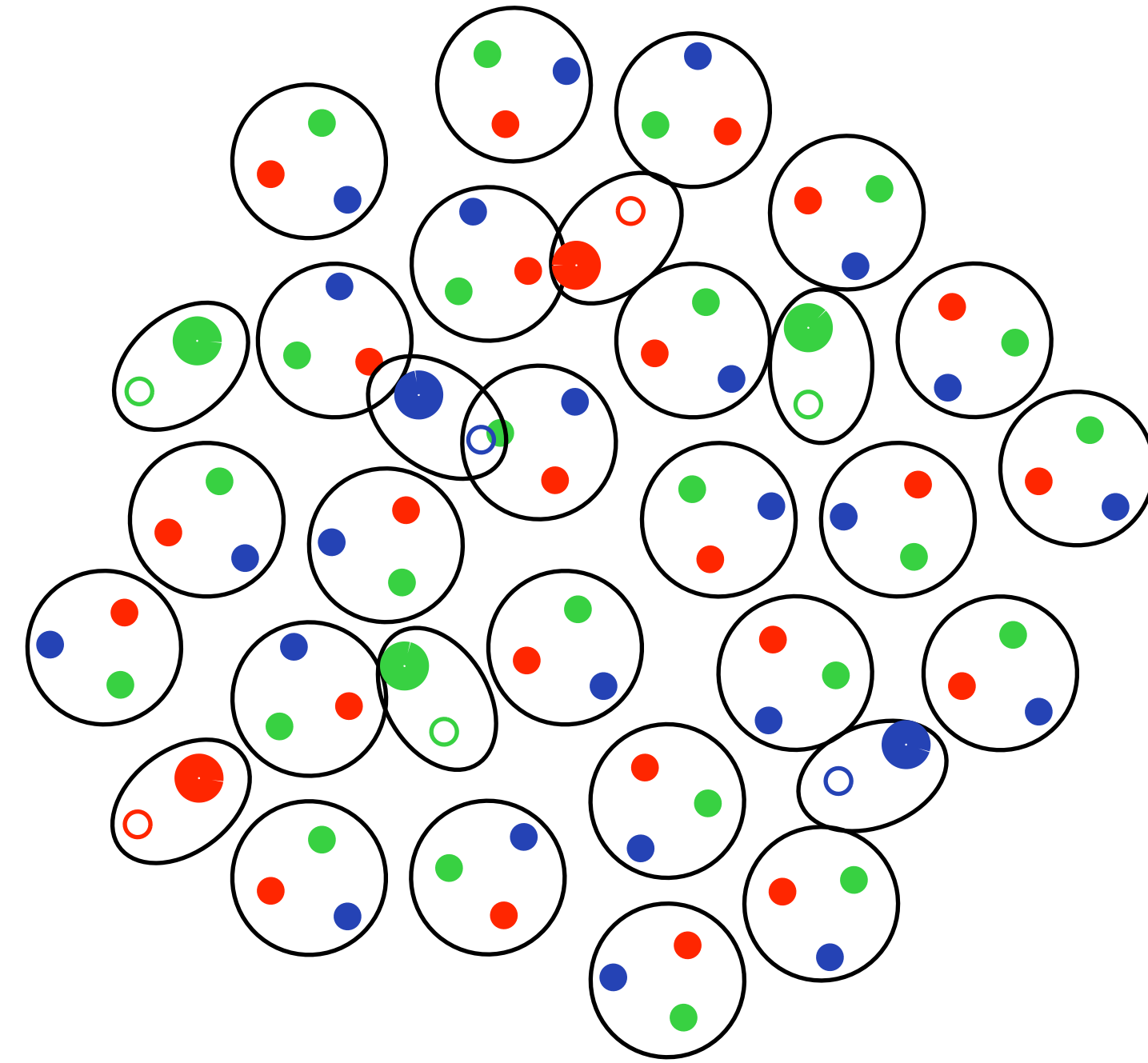
Charges at long range ($r > r_D$) are screened

QCD and Debye screening

At low color densities:

quarks and gluons confined into
color singlets

→ hadrons (baryons and mesons)

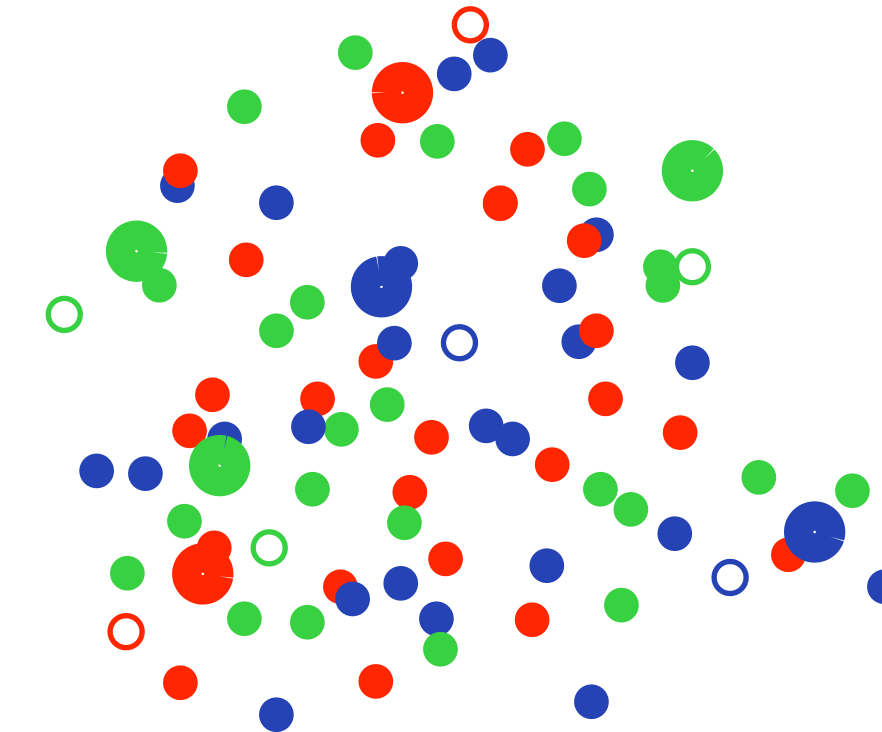


QCD and Debye screening

At low color densities:

quarks and gluons confined into
color singlets

→ hadrons (baryons and mesons)



At high color densities:

quarks and gluons unbound

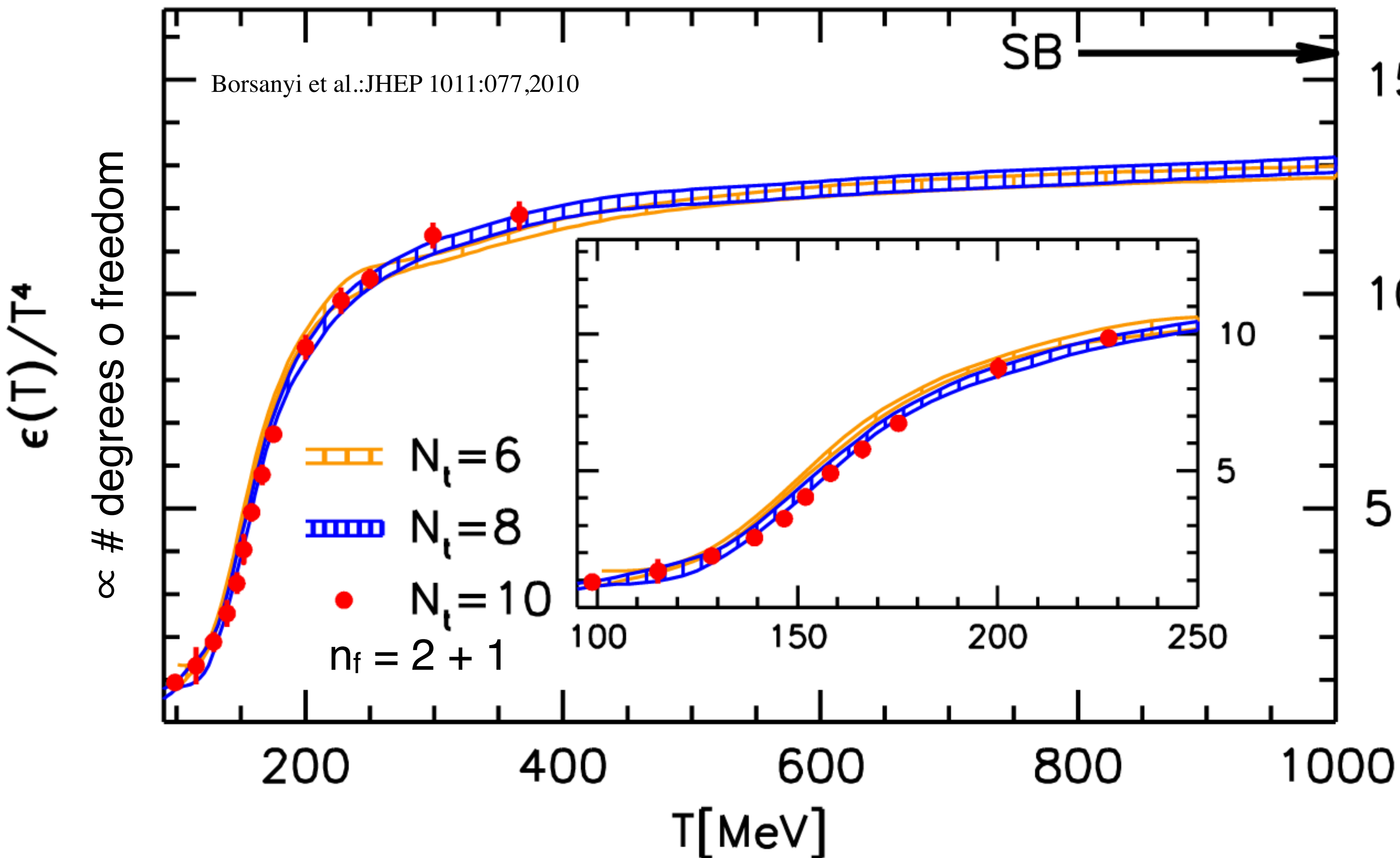
Debye screening of color charge

→ QGP - color conductor

Can create high color density by heating or compressing

→ QGP creation via accelerators or in neutron stars

Goal of Hot QCD in a nutshell



Number of degrees of freedom increases by factor 10 at $T \sim 150$ MeV
→ quarks and gluons

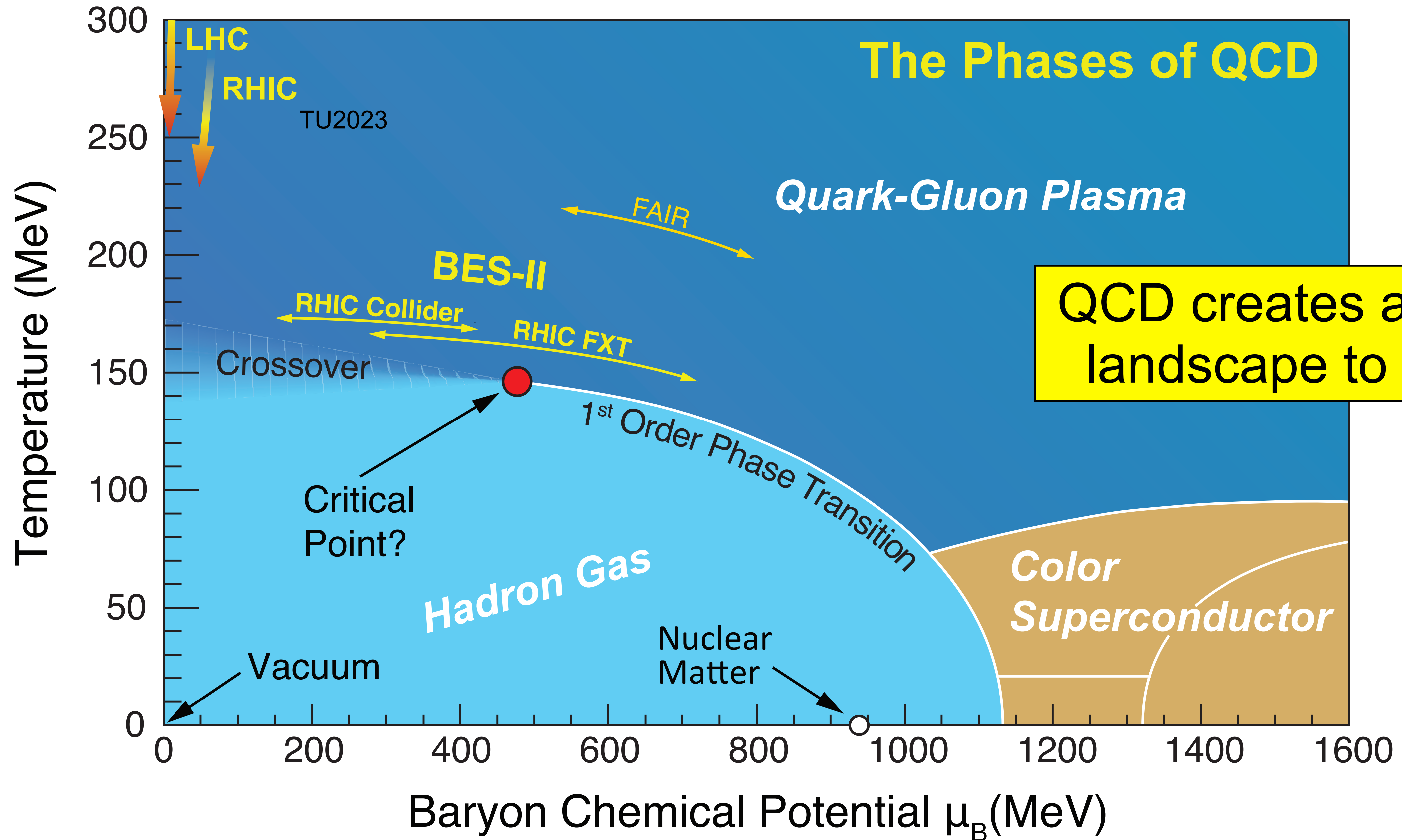
Lattice calculations:
rapid smooth cross-over
at $\mu_B \sim 0$

$$T_{pc} \approx 156.5 \pm 1.5 \text{ MeV}$$

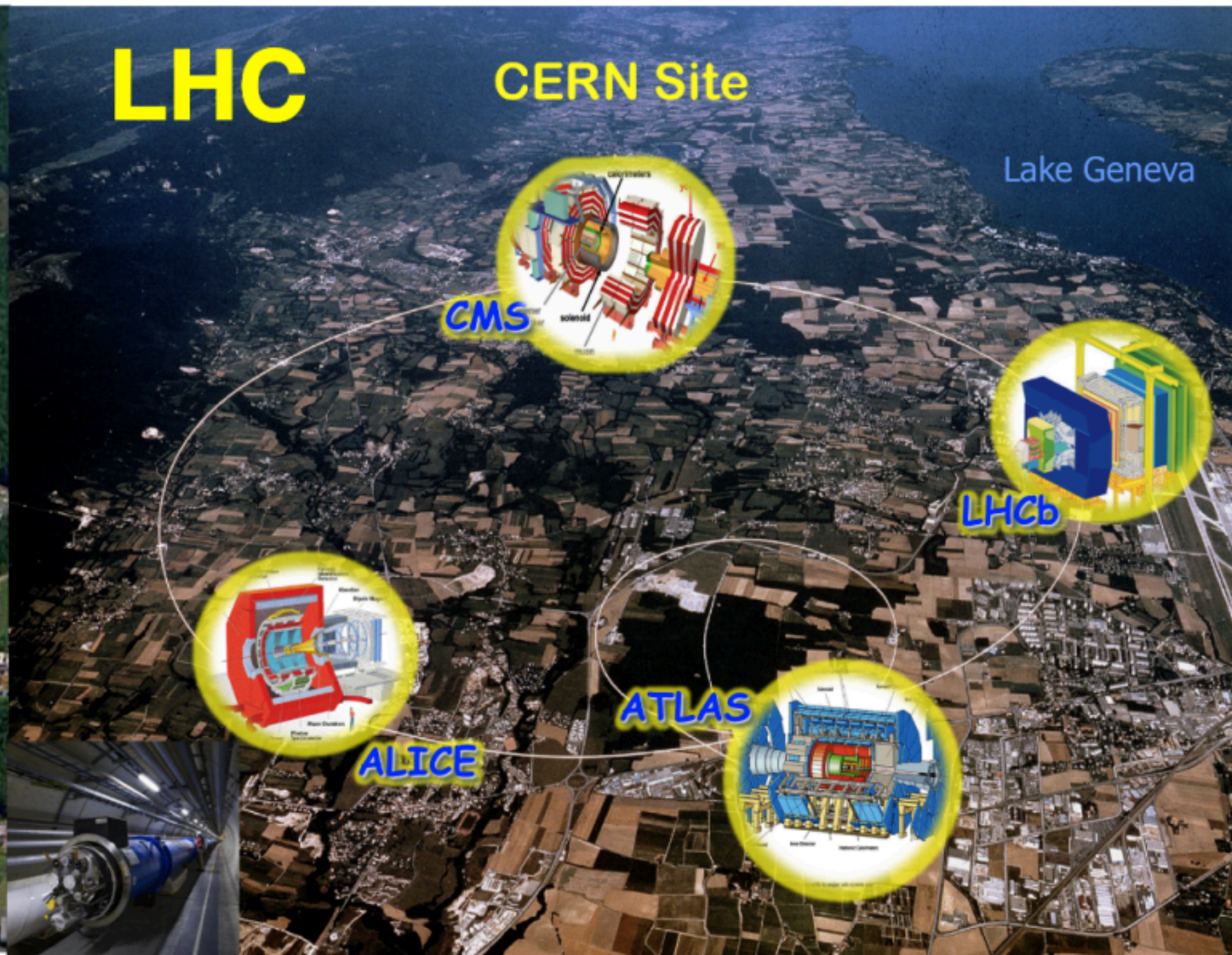
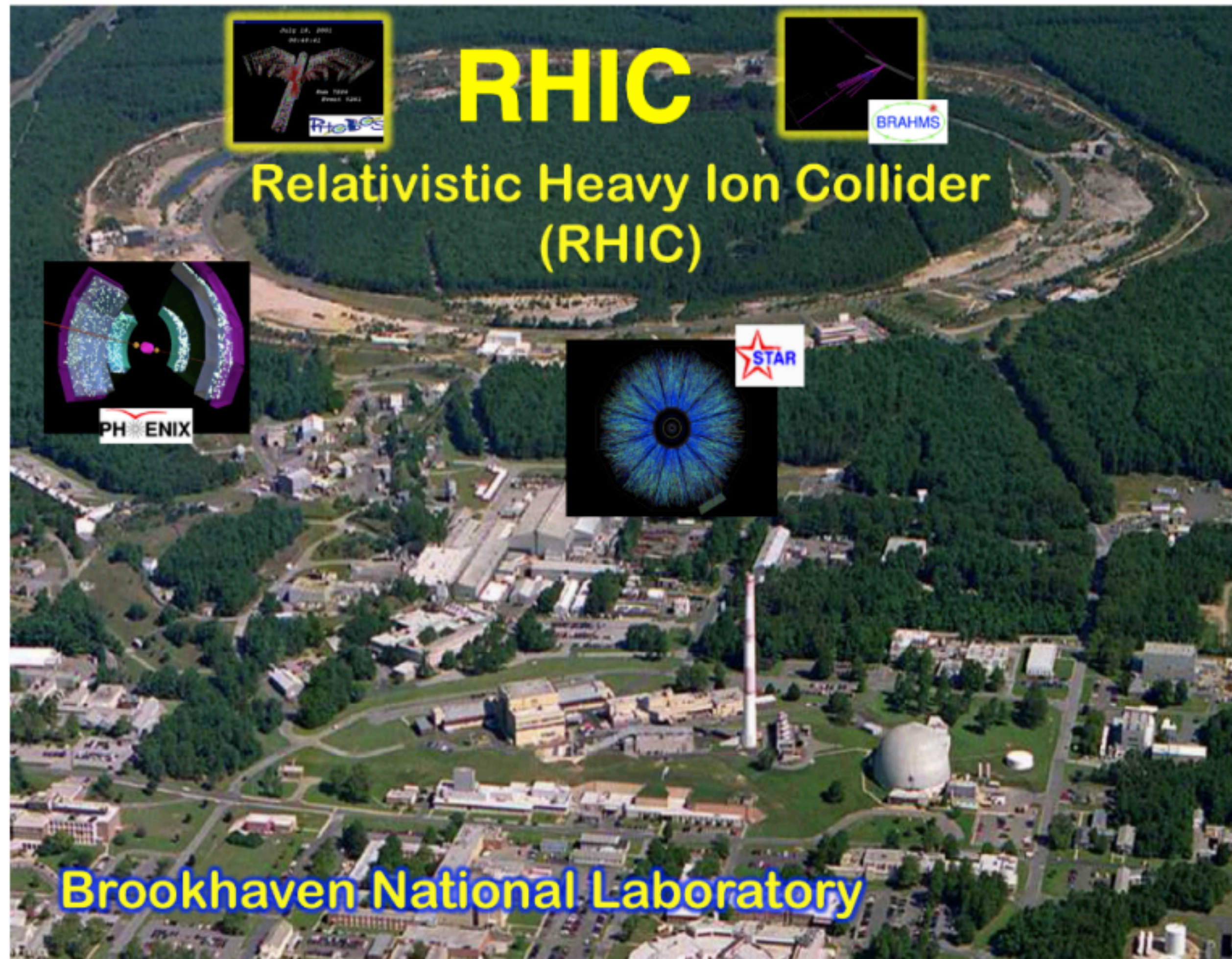
$$\epsilon_{pc} \approx 0.70 \text{ GeV/fm}^3$$

Such conditions can be created via HI collisions at RHIC and LHC

The phase diagram of QCD



Recreating in the lab



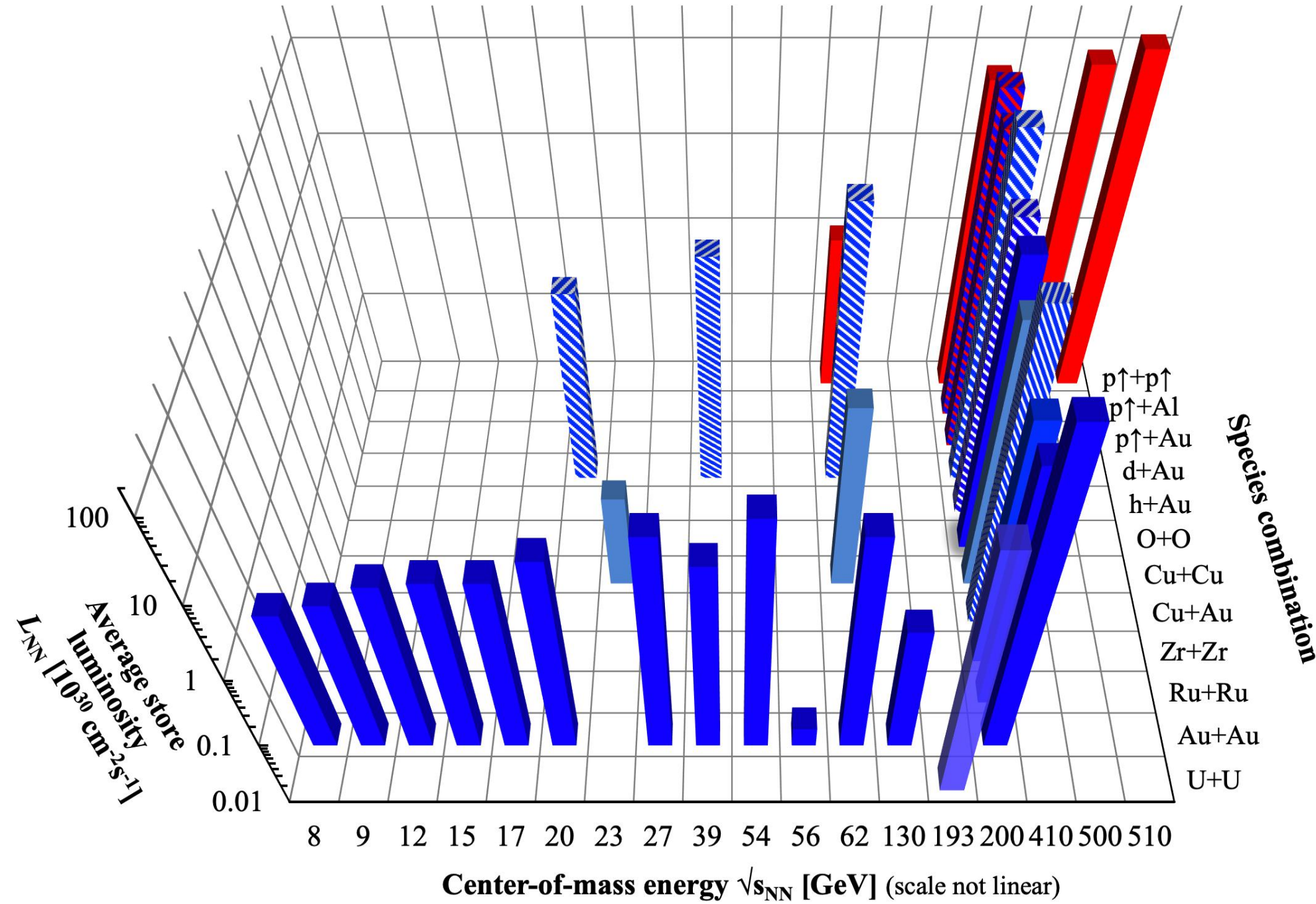
RHIC Start date: 2001

LHC Start date: 2010

sPHENIX taking first data at RHIC now

Wealth of data available

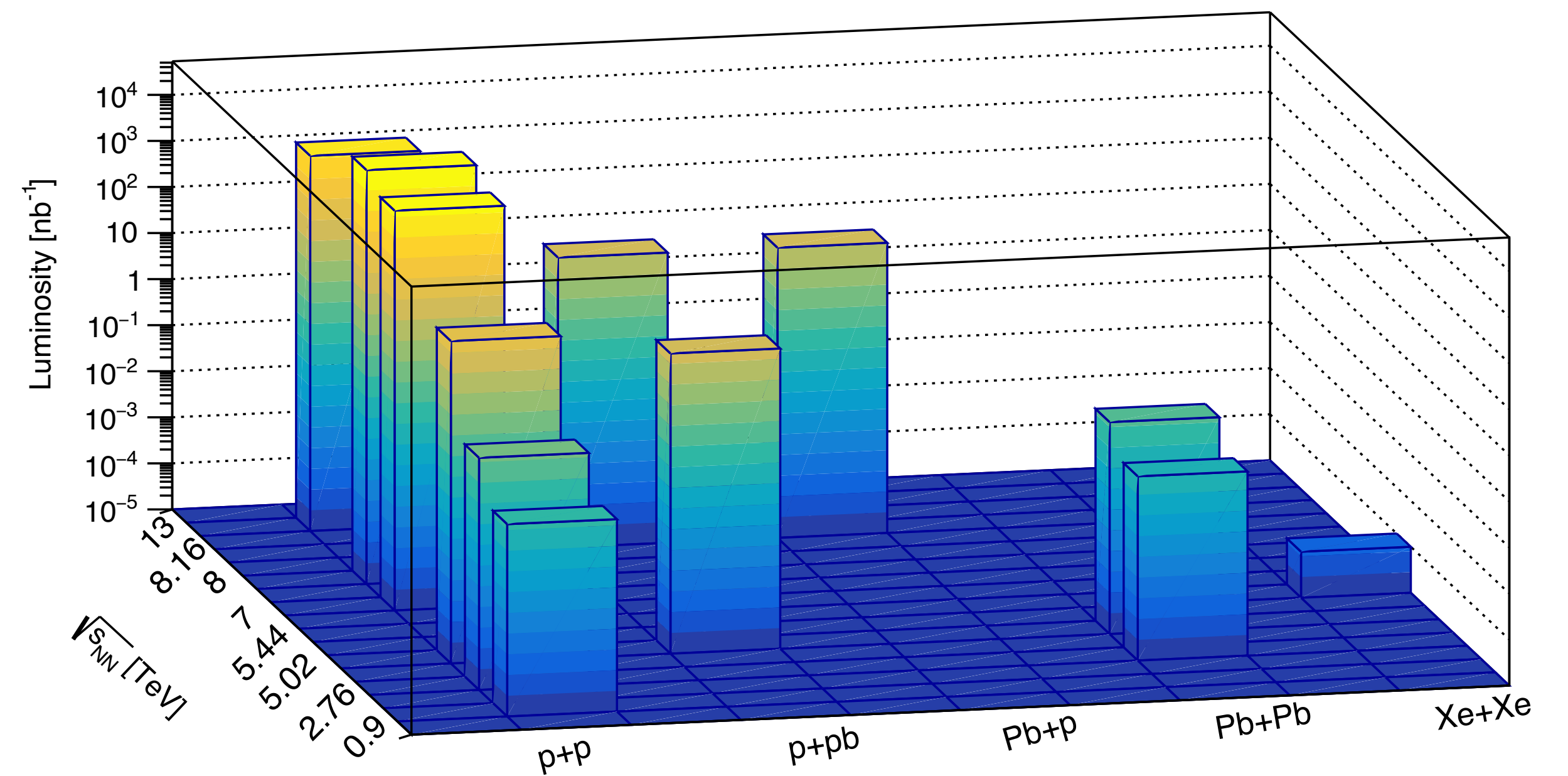
RHIC energies, species combinations and luminosities (Run-1 to 22)



LHC (top energy, rare probes):
 Pb+Pb, Xe+Xe, p+Pb, p+p
 For Pb+Pb mostly at 5.02 TeV
 HUGE datasets
 (significantly bigger at ATLAS and CMS)

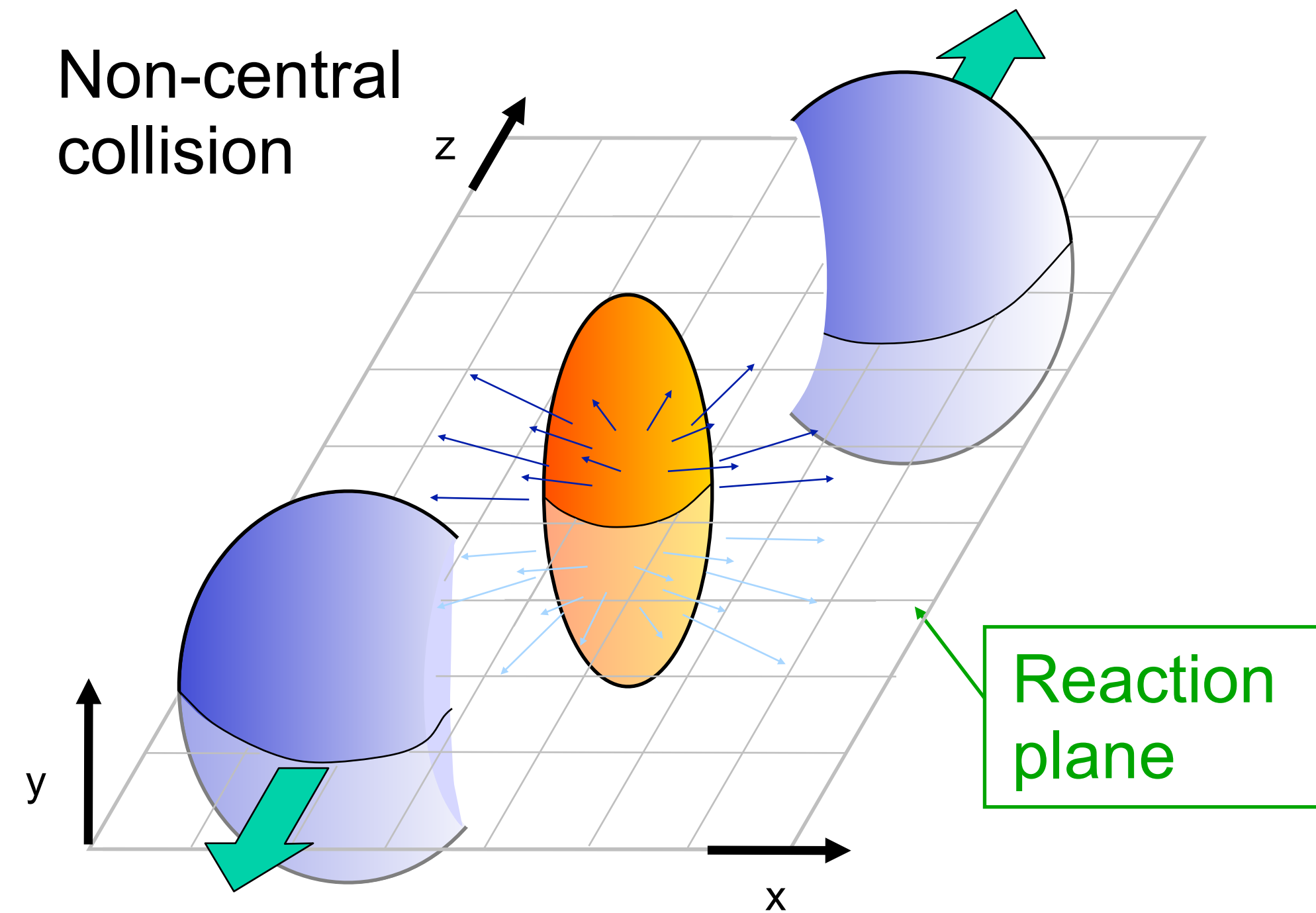
RHIC (beam energy scan, different nuclei):
 U+U, Au+Au, Ru+Ru, Zr+Zr, Cu+Cu, O+O,
 Cu+Au, He³+Au, d+Au, p+Au, p+Al, p+p
 Mostly at 200 GeV but Au+Au from 3-200 GeV

LHC Beams@ALICE Run 1 and 2 (2009-2017)

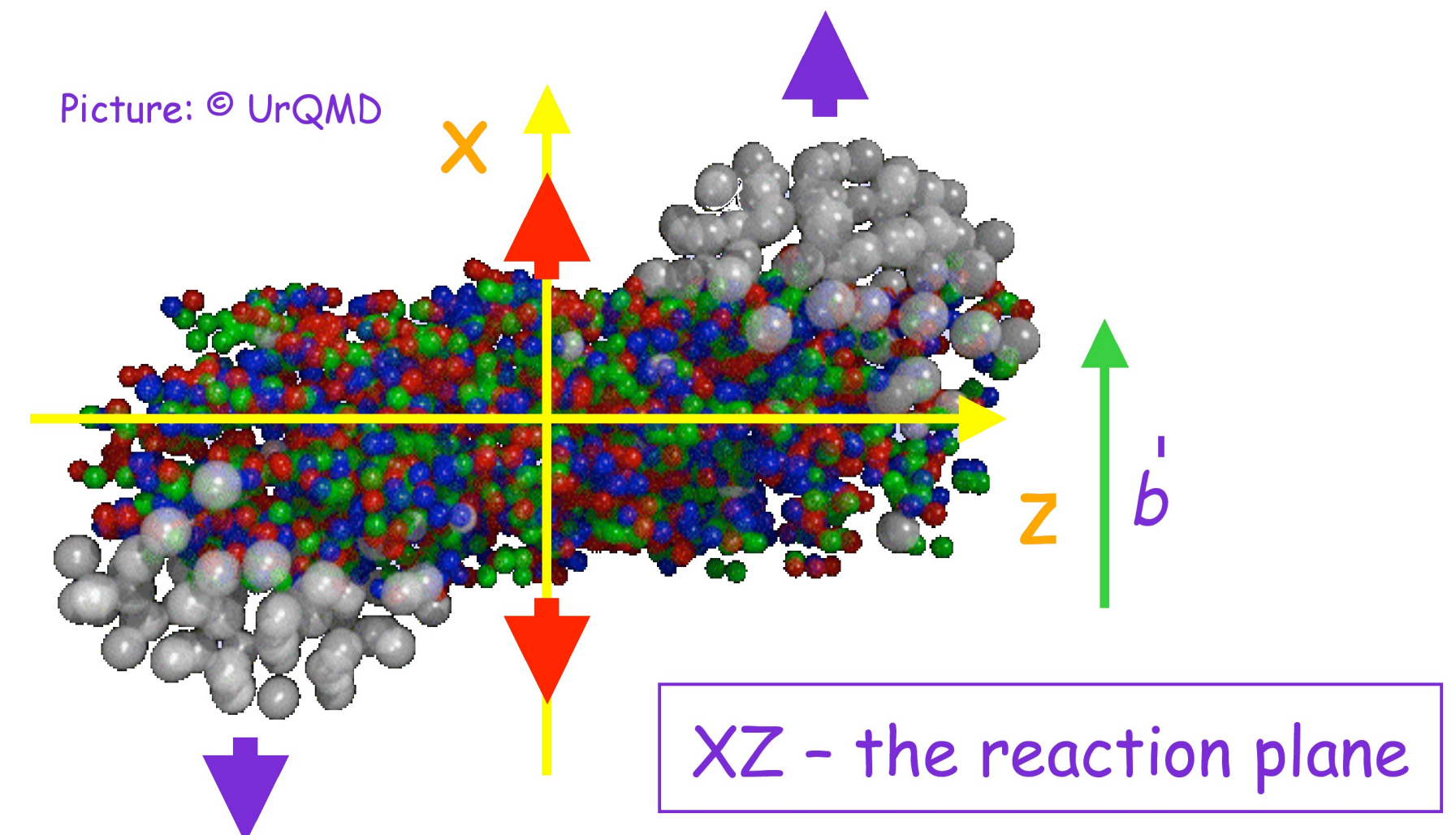


Complimentary datasets

Geometry of a heavy-ion collision



“peripheral” collision ($b \sim b_{\text{max}}$)
“central” collision ($b \sim 0$)



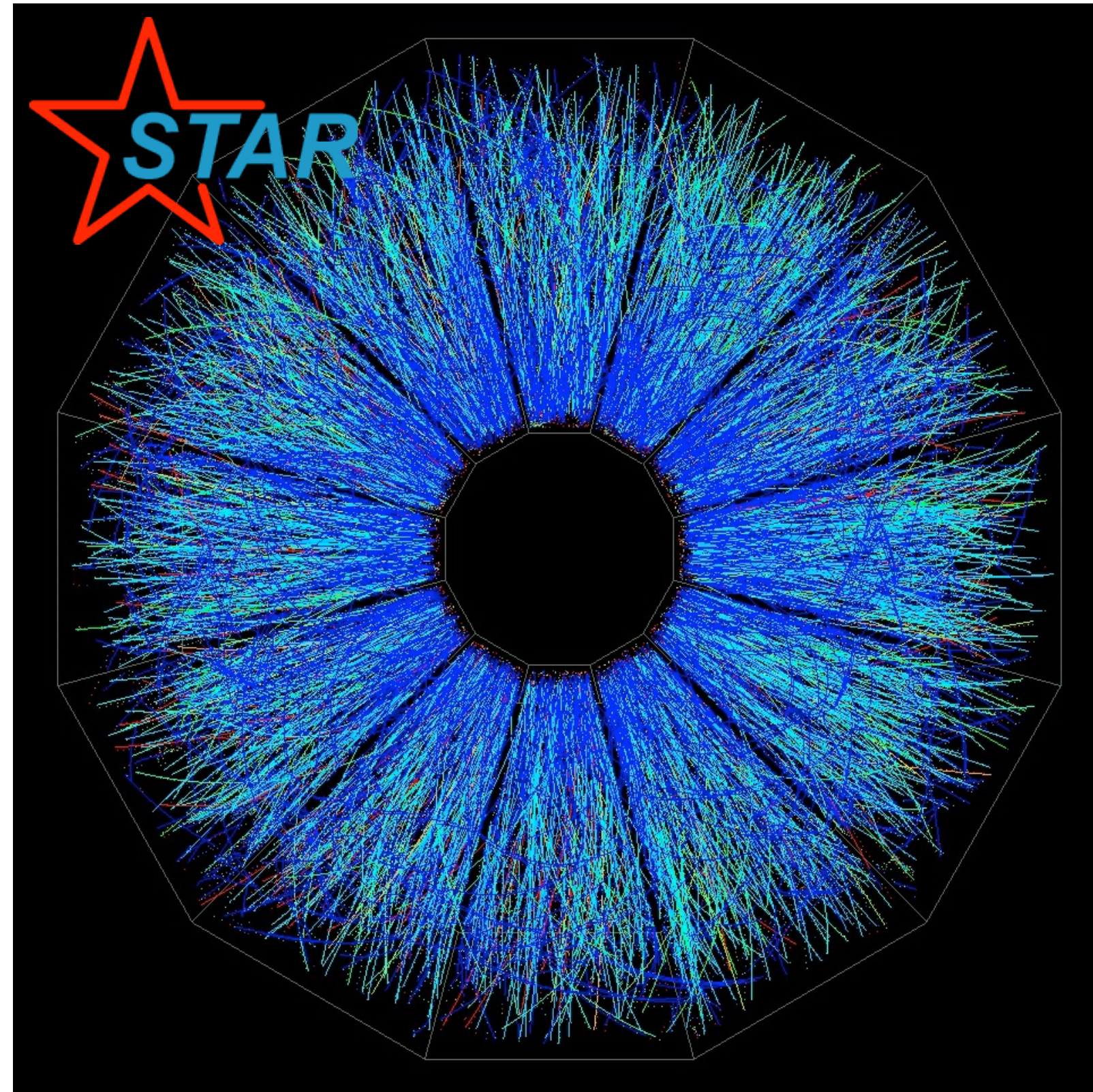
Number of participants (N_{part}): number of incoming nucleons (participants) in overlap region

Number of binary collisions (N_{bin}): number of equivalent inelastic nucleon-nucleon collisions

$$N_{\text{bin}} \geq N_{\text{part}}/2$$

More central collisions produce more particles

39.4 TeV in central Au-Au collision

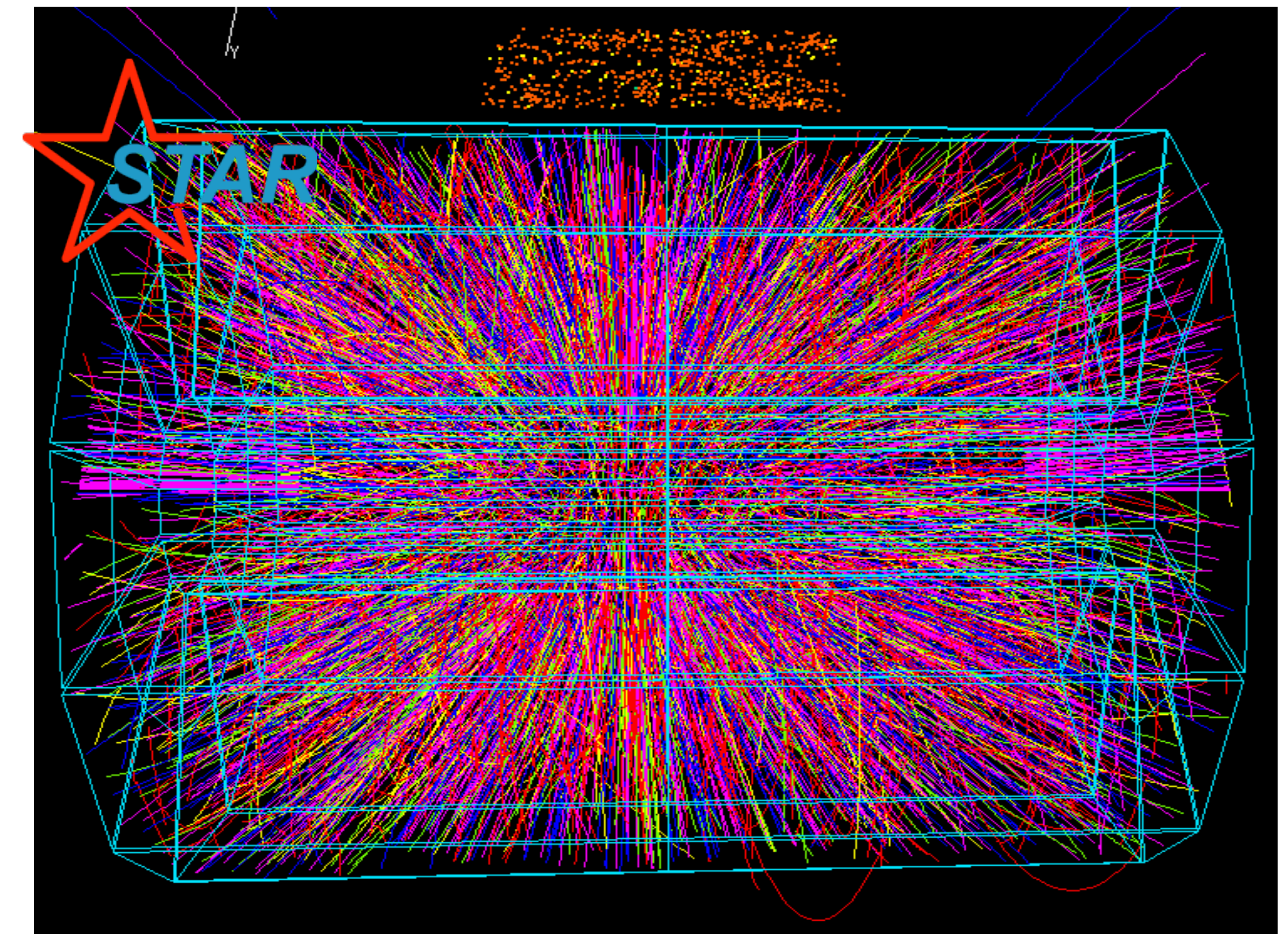


Only **charged** particles shown

Neutrals don't ionize the TPC's gas so are not "seen" by this detector.

>5000 hadrons and leptons

26 TeV is removed from colliding beams.



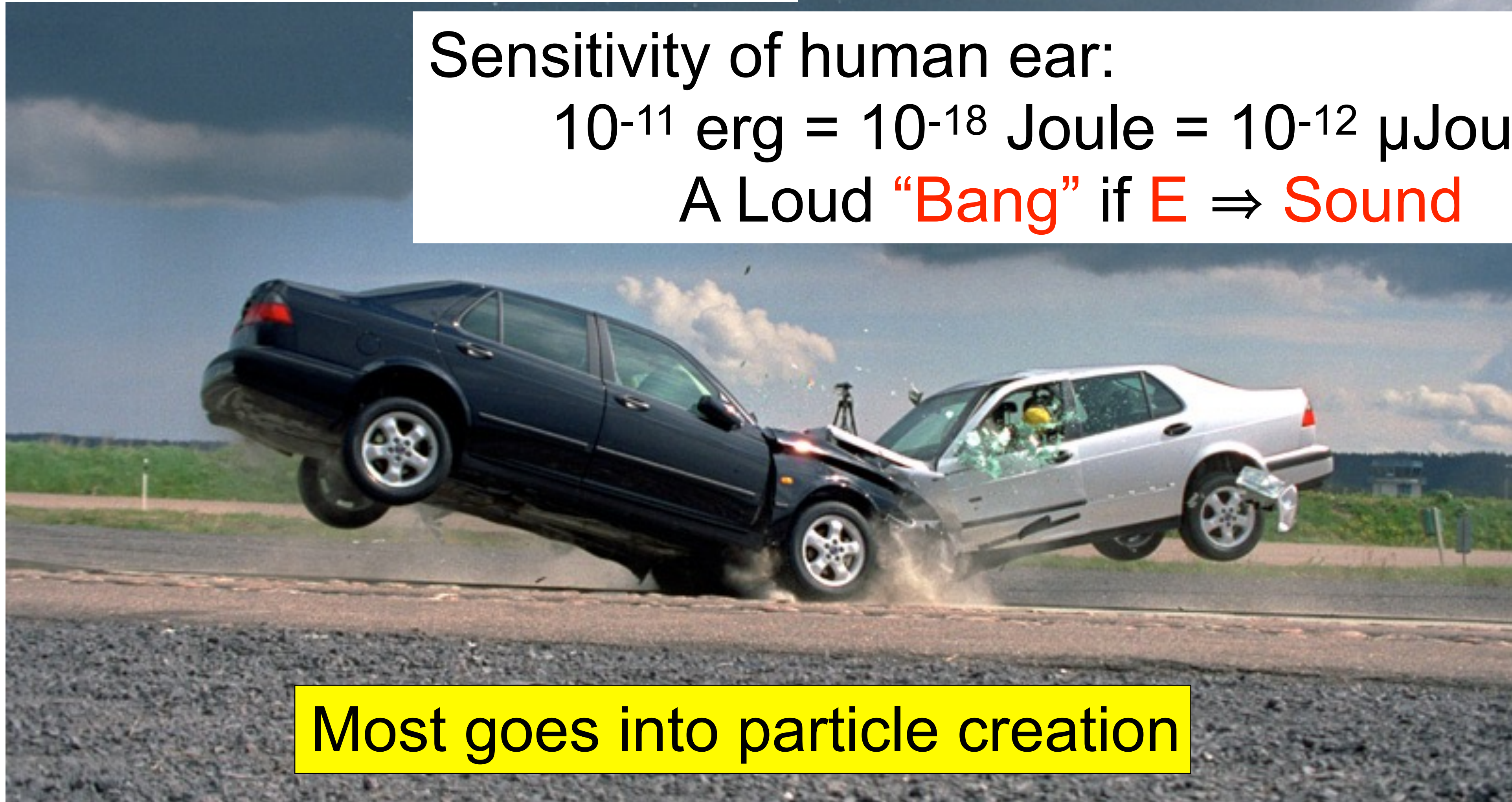
The energy contained in one collision

Central Au+Au Collision:
26 TeV \sim 6 μ Joule

Sensitivity of human ear:

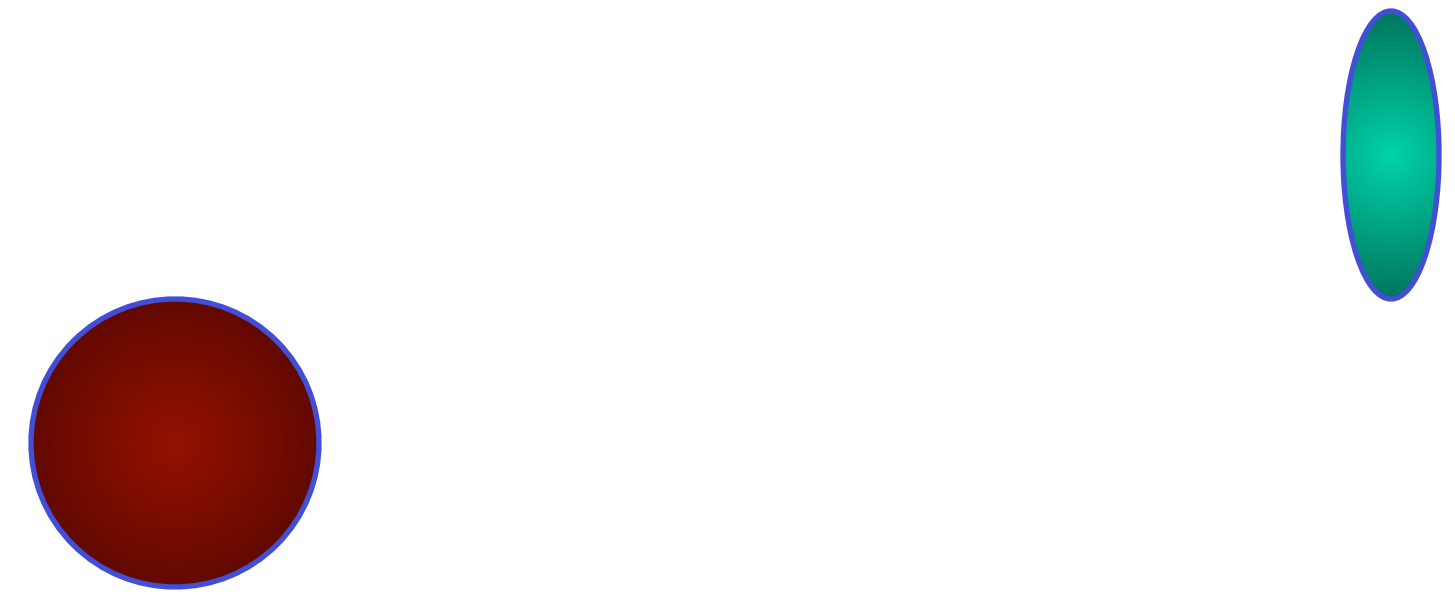
10^{-11} erg = 10^{-18} Joule = 10^{-12} μ Joule

A Loud “Bang” if $E \Rightarrow$ Sound



Quantifying the collision

p+p: 2 Participants, 1 Binary Collision

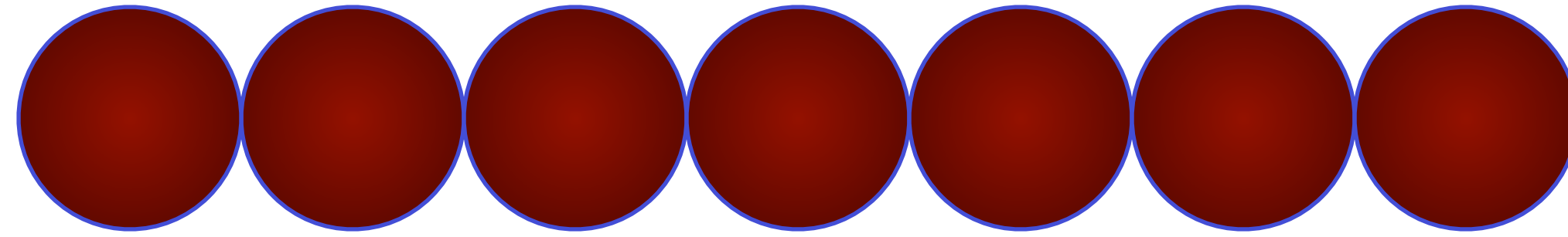
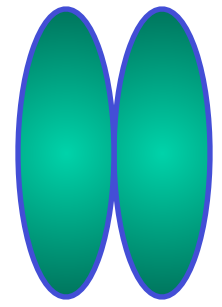


Participants: those nucleons that have interacted at least once

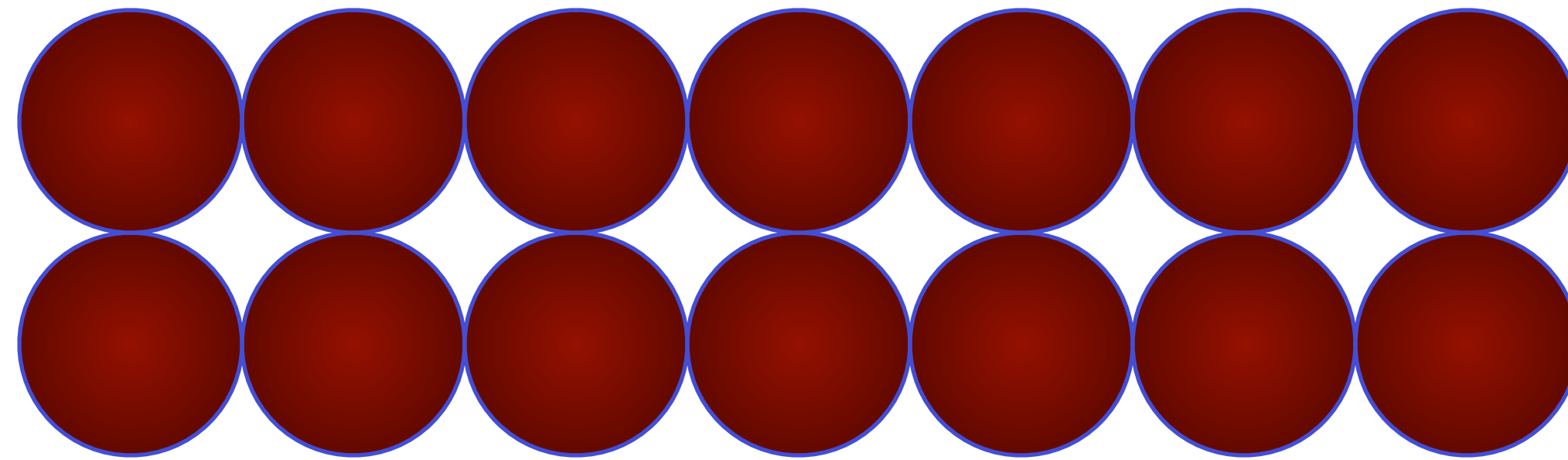
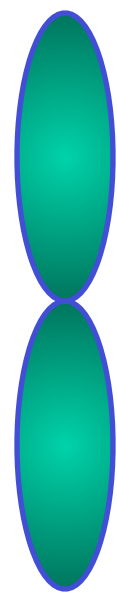
Binary collisions: the number of 1+1 collisions

Quantifying the collision

A+A:



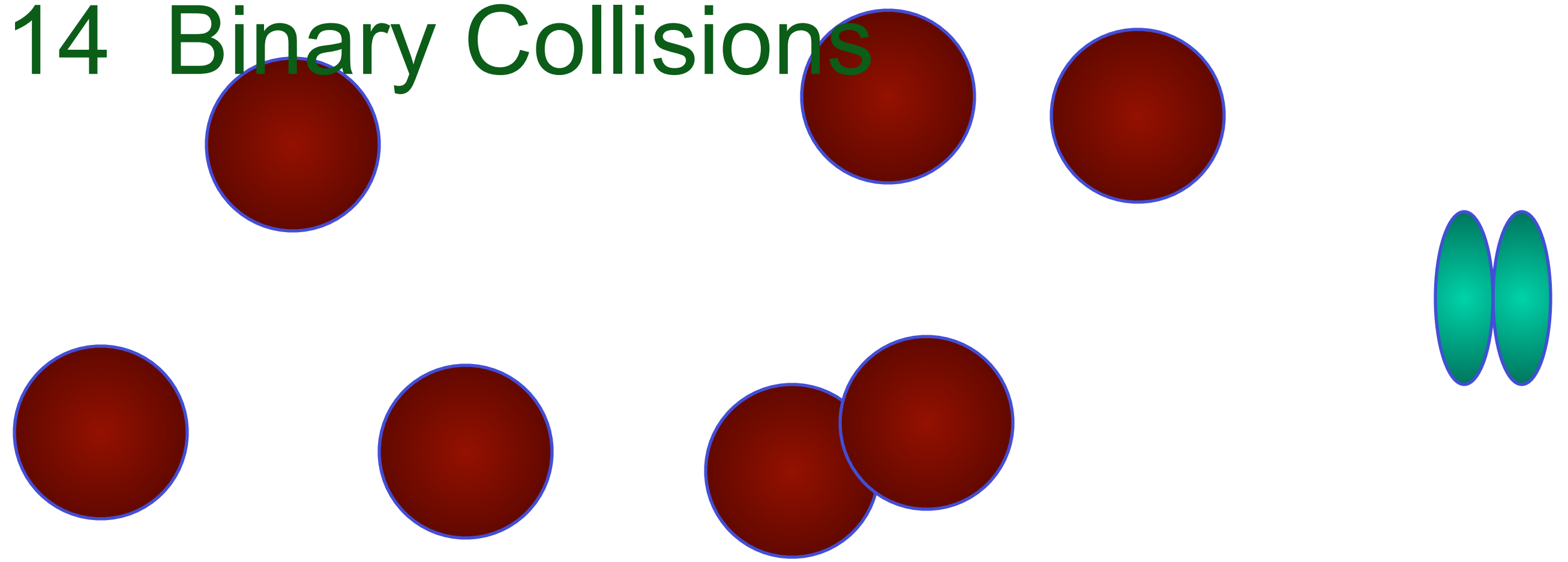
A+A:



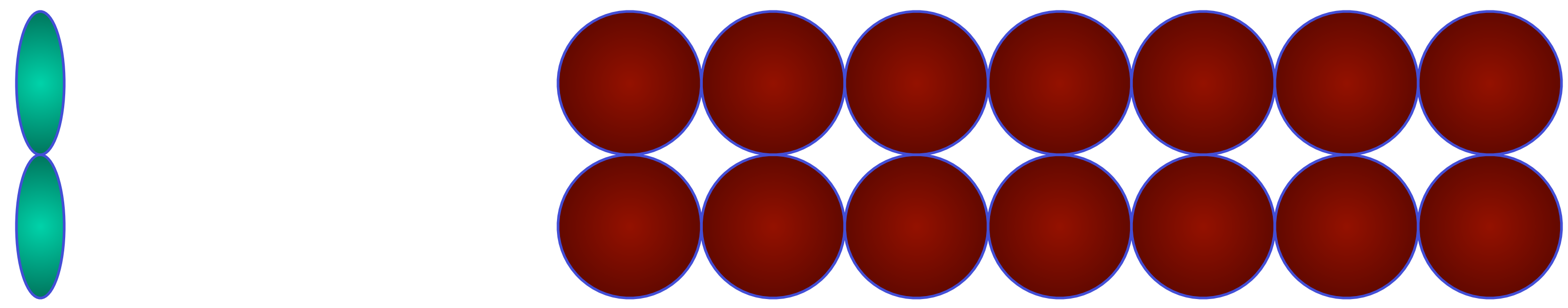
Multiplicity of event and N_{part} correlated

Quantifying the collision

A+A: 9 Participants, 14 Binary Collisions



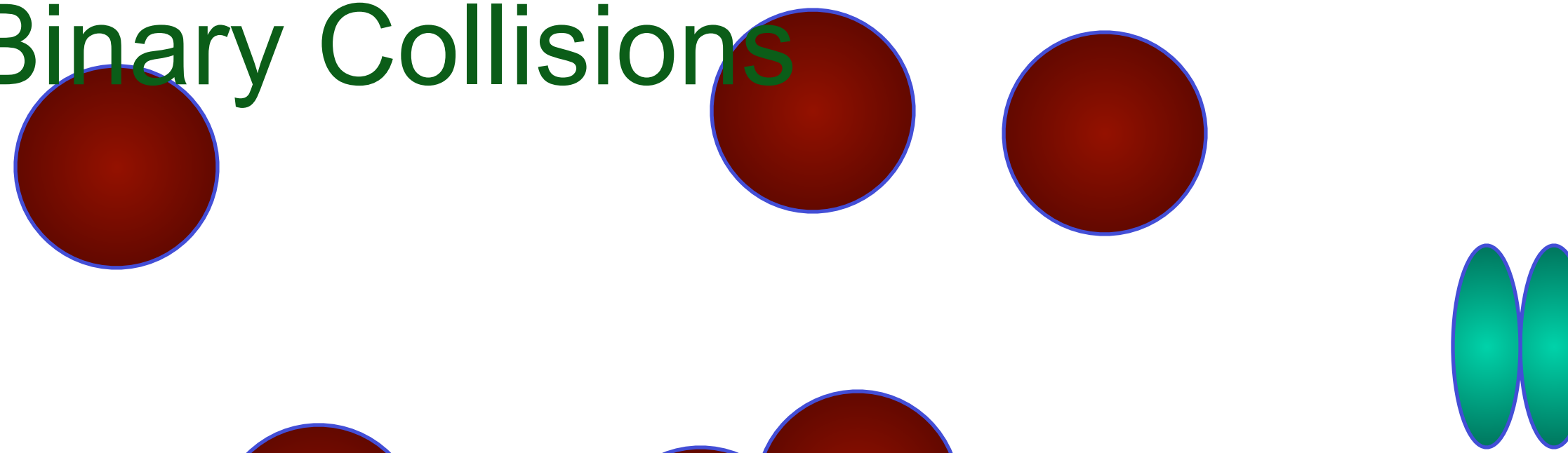
A+A:



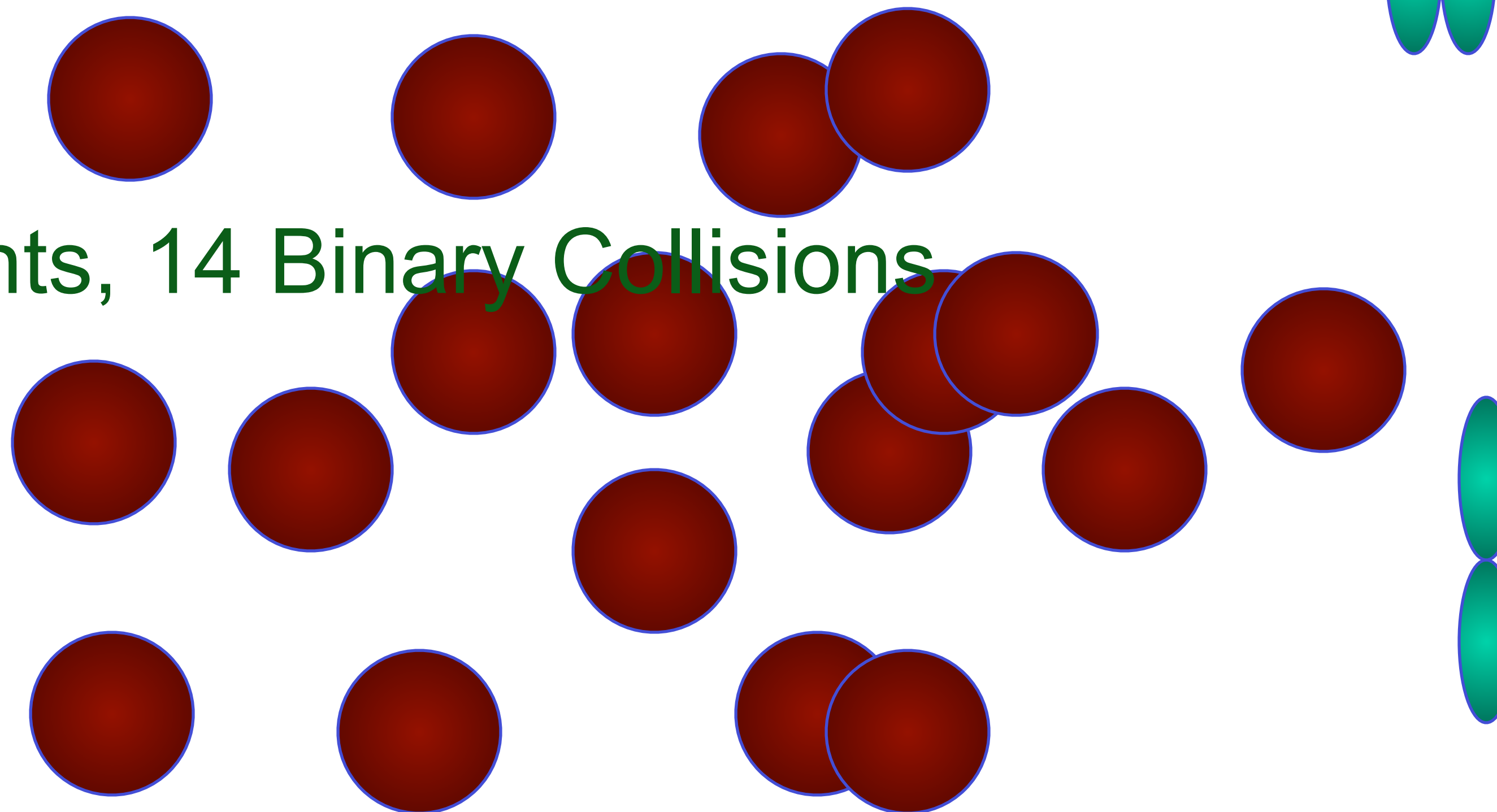
Multiplicity of event and N_{part} correlated

Quantifying the collision

A+A: 9 Participants, 14 Binary Collisions



A+A: 16 Participants, 14 Binary Collisions



Multiplicity of event and N_{part} correlated

Glauber to the rescue

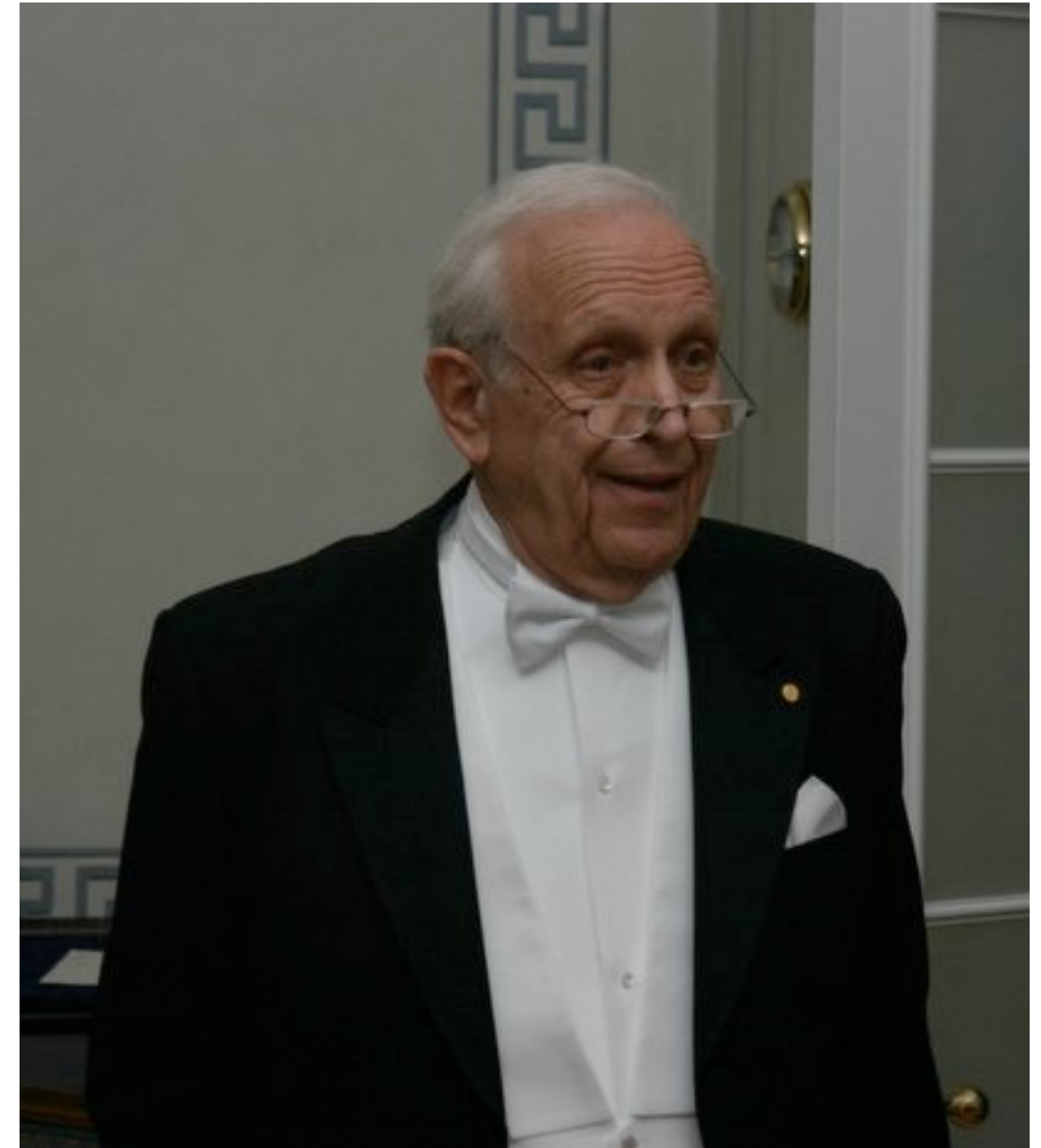
Use a Glauber calculation to estimate N_{bin} and N_{part}

Roy Glauber: 2005 Nobel prize for “his contribution to the quantum theory of optical coherence”

Application of Glauber theory to heavy ion collisions does not use the full sophistication of these methods.

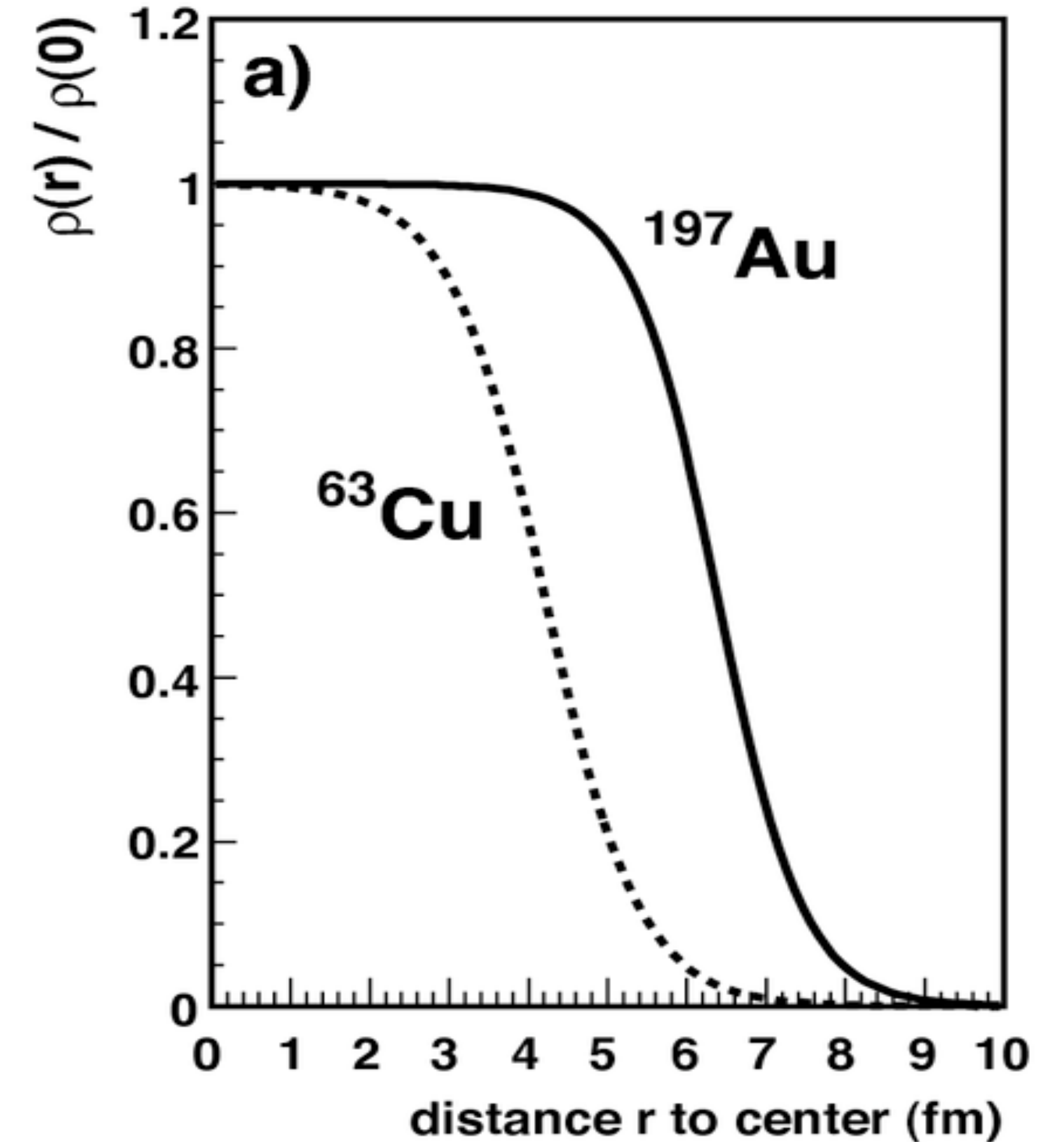
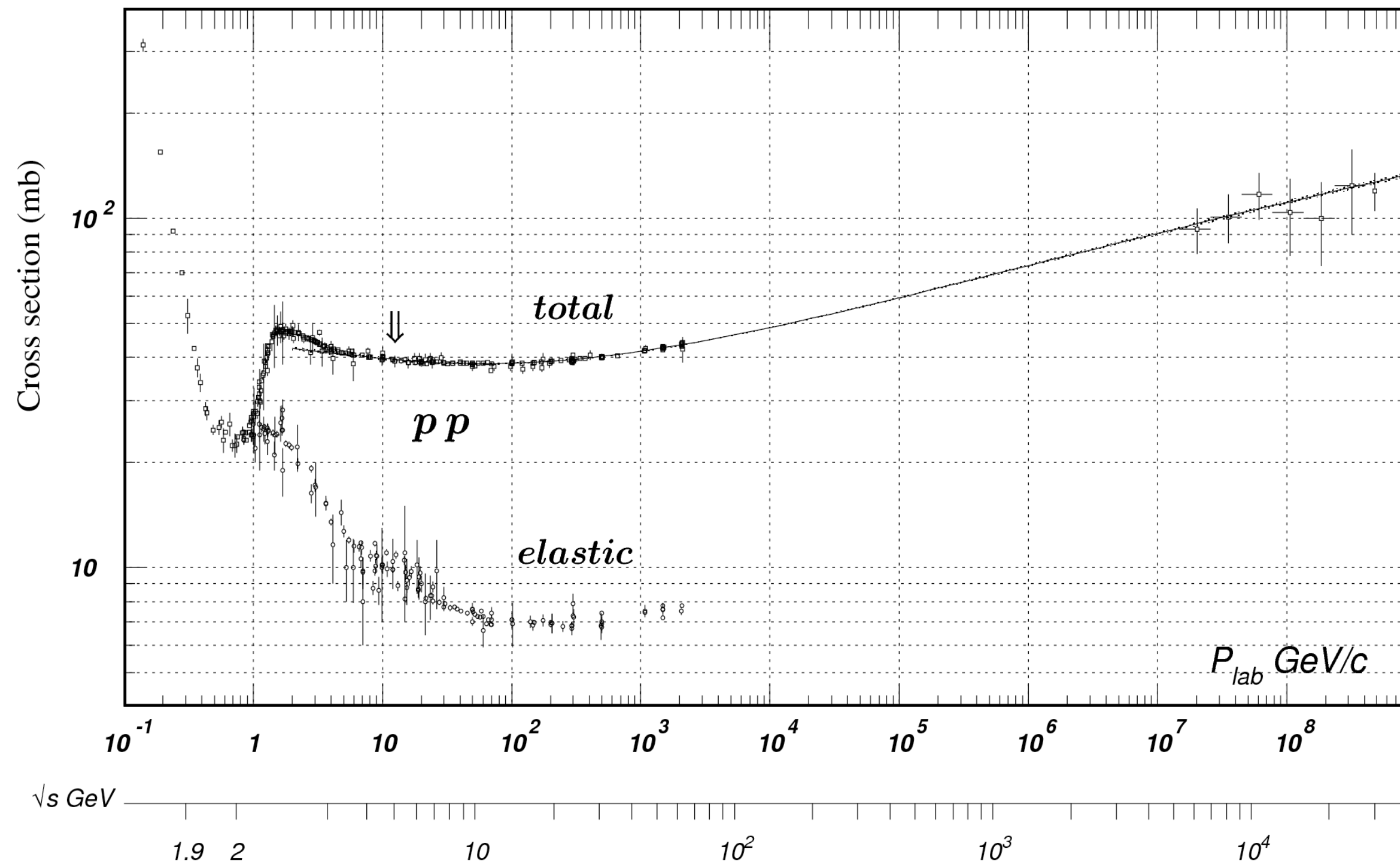
Two simple assumptions:

- 1) Eikonal - constituents of nuclei proceed in straight-line trajectories
- 2) Interactions determined by initial-state shape of overlapping nuclei



Ingredients for Glauber calculations

Particle Data Book: W.-M. Yao et al., J. Phys. G 33,1 (2006) Fig 40.11



Nucleon-nucleon interaction cross section

Most use inelastic: 42 mb at $\sqrt{s}=200$ GeV

Probability density distribution for nucleons:

'Wood-Saxon' from electron scattering experiments

Monte-carlo Glauber modeling

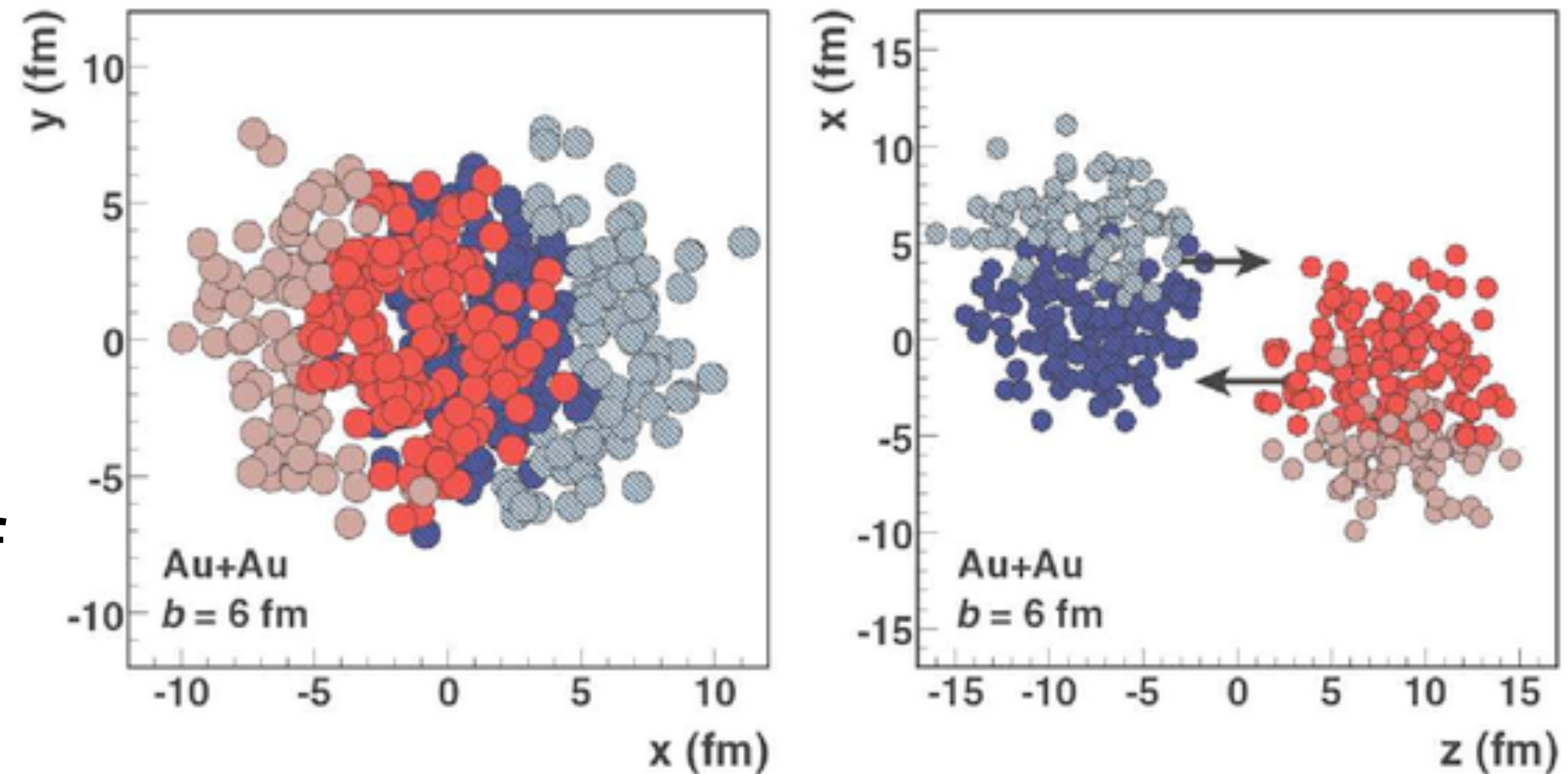
Randomly initialize nucleons

Randomly select impact parameter

Randomly sample probability of nucleons to interact from interaction cross-section if separated by

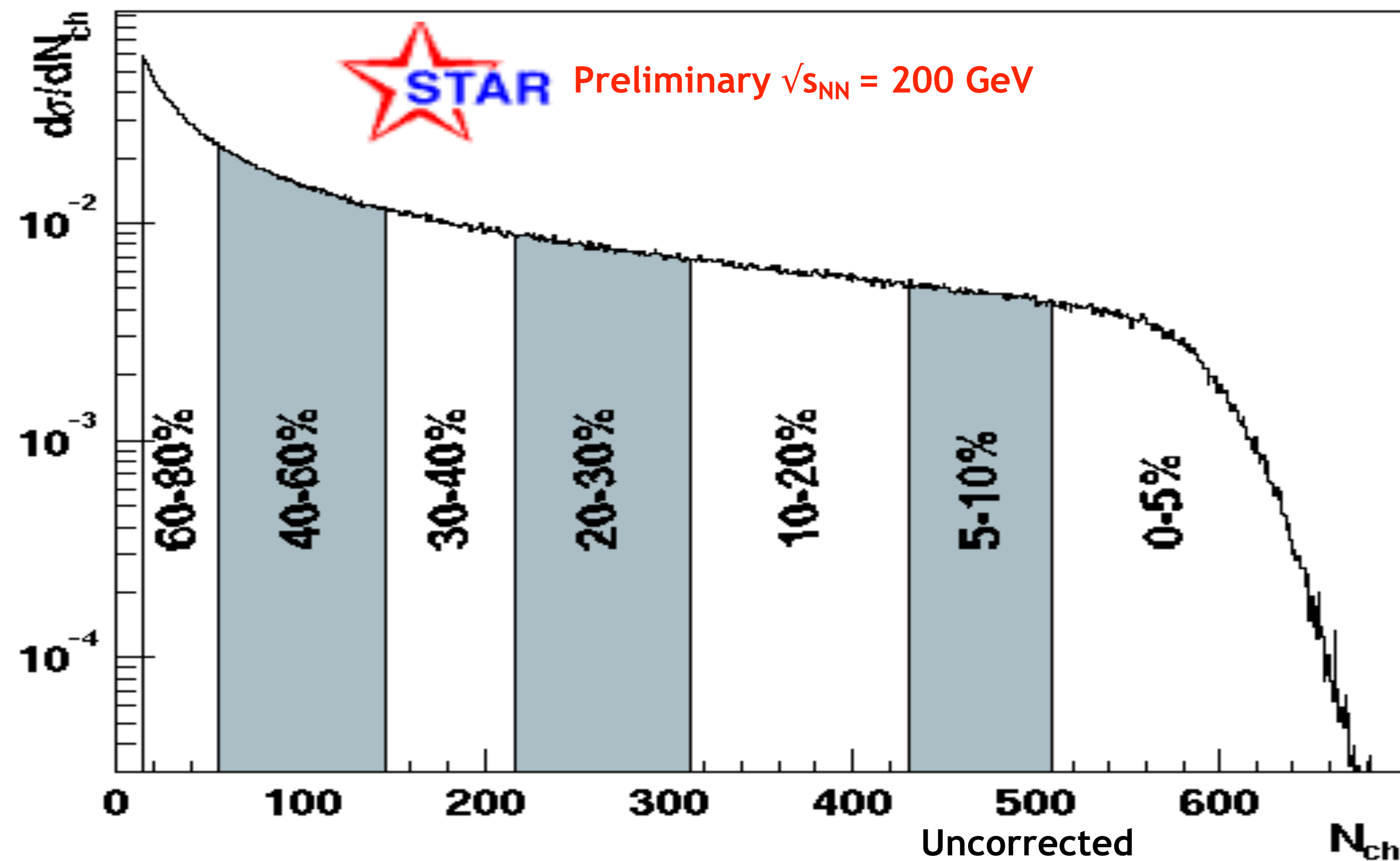
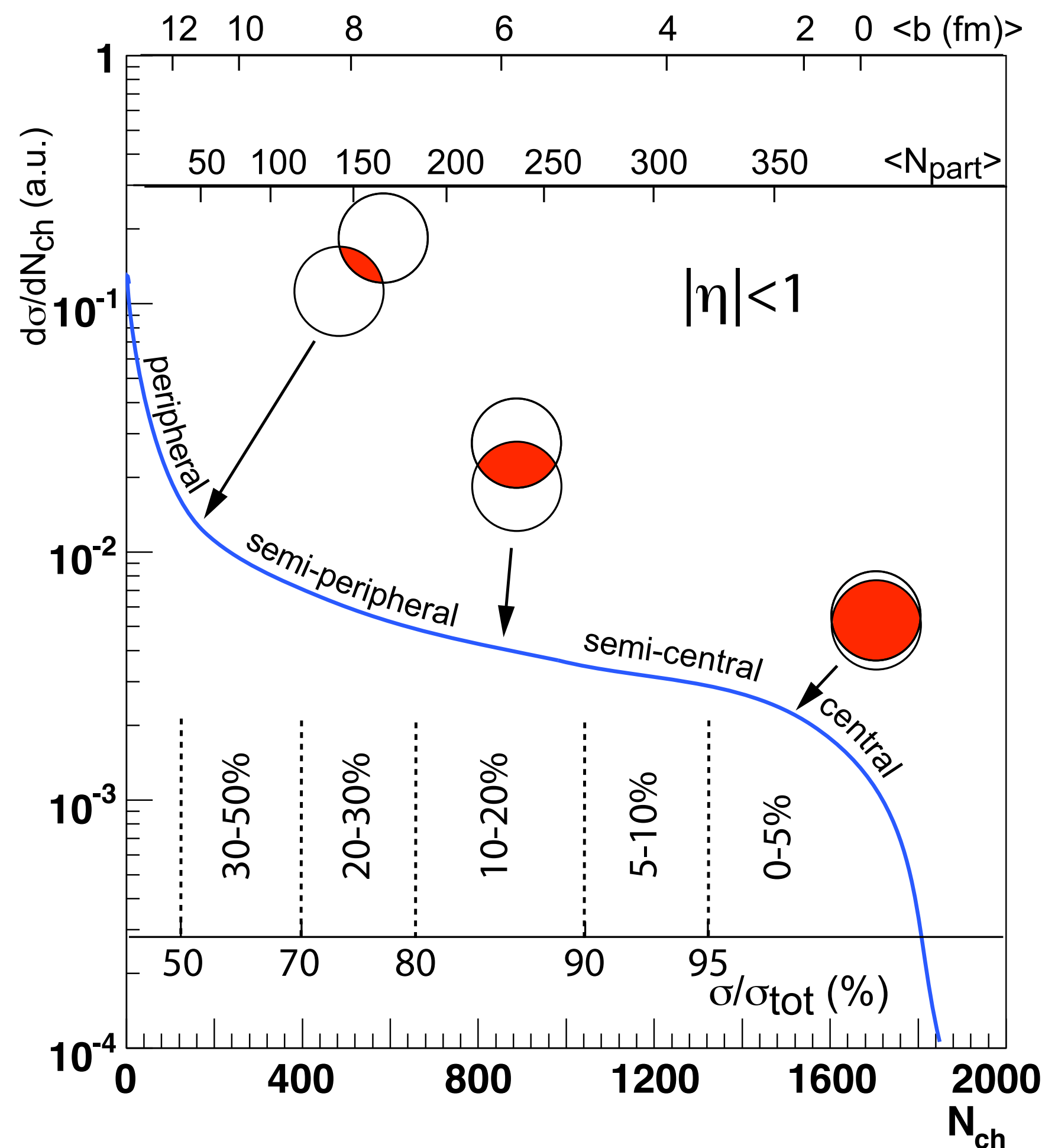
$$d < \sqrt{\sigma_{\text{int}}/\pi}$$

Calculate probability that N_{part} or N_{bin} occurs per event



Map onto an experimentally measurable variable expected to scale with centrality
i.e. particle multiplicity

Comparing to data

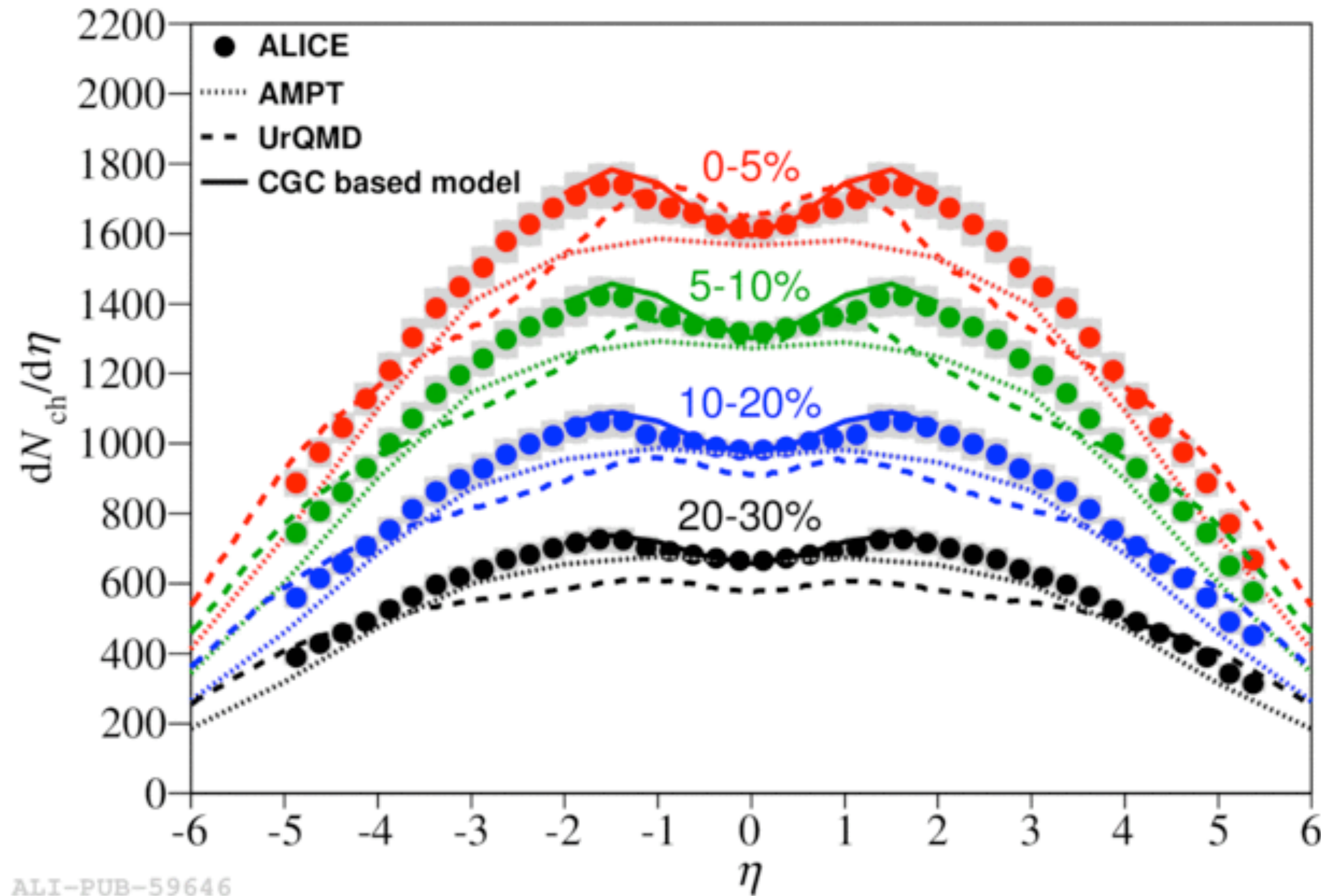


Good agreement between data and calculation

Measured mid-rapidity particle yield can be related to size of overlap region

**Do we create the necessary
initial conditions?**

Energy density of a central collision



In central Pb-Pb events:

$$dN_{ch}/d\eta \sim 1600$$

$$\langle p_T \rangle \sim 650 \text{ MeV}$$

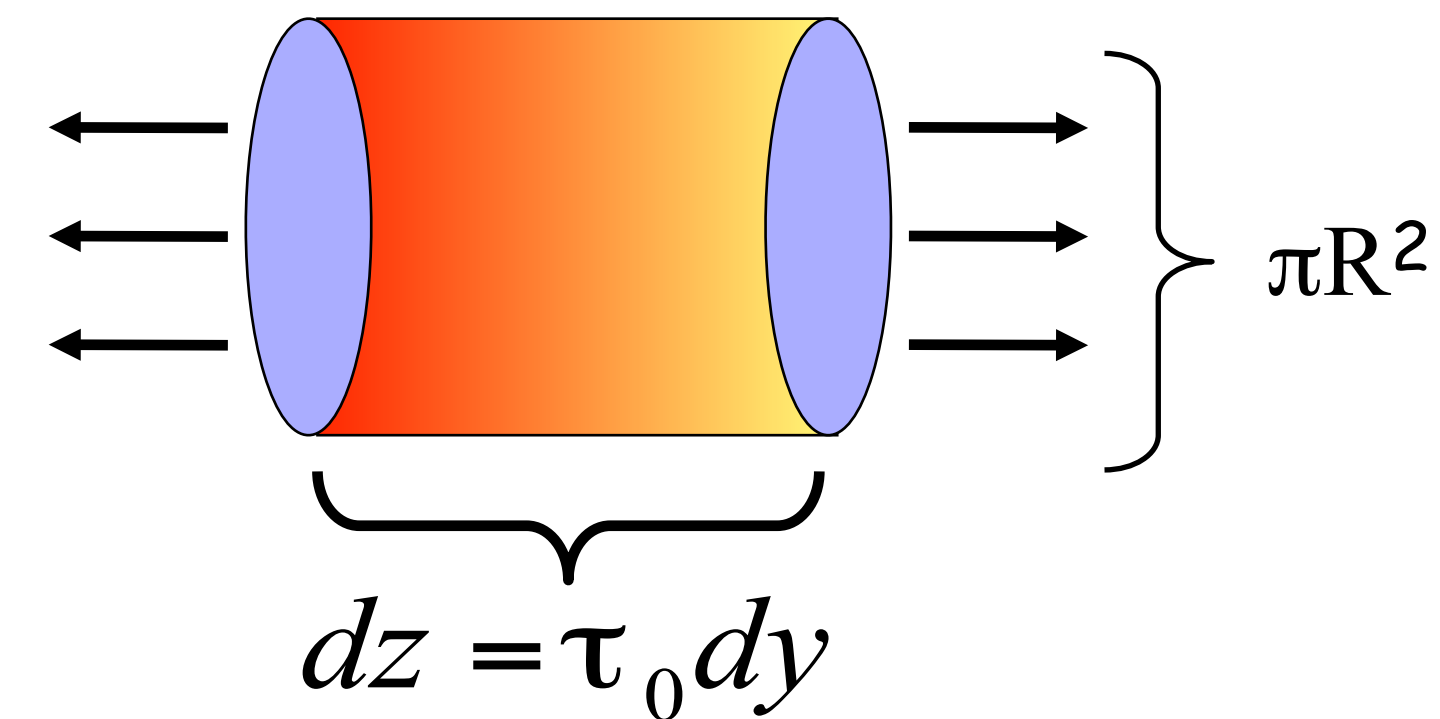
$$\tau_0 \sim 1 \text{ fm}$$

Bjorken-Formula for Energy Density:

$$\epsilon_{Bj} = \frac{\Delta E_T}{\Delta V} = \frac{1}{\pi R^2} \frac{1}{\tau_0} \frac{3}{2} \frac{dN_{ch}}{d\eta} \langle p_T \rangle$$

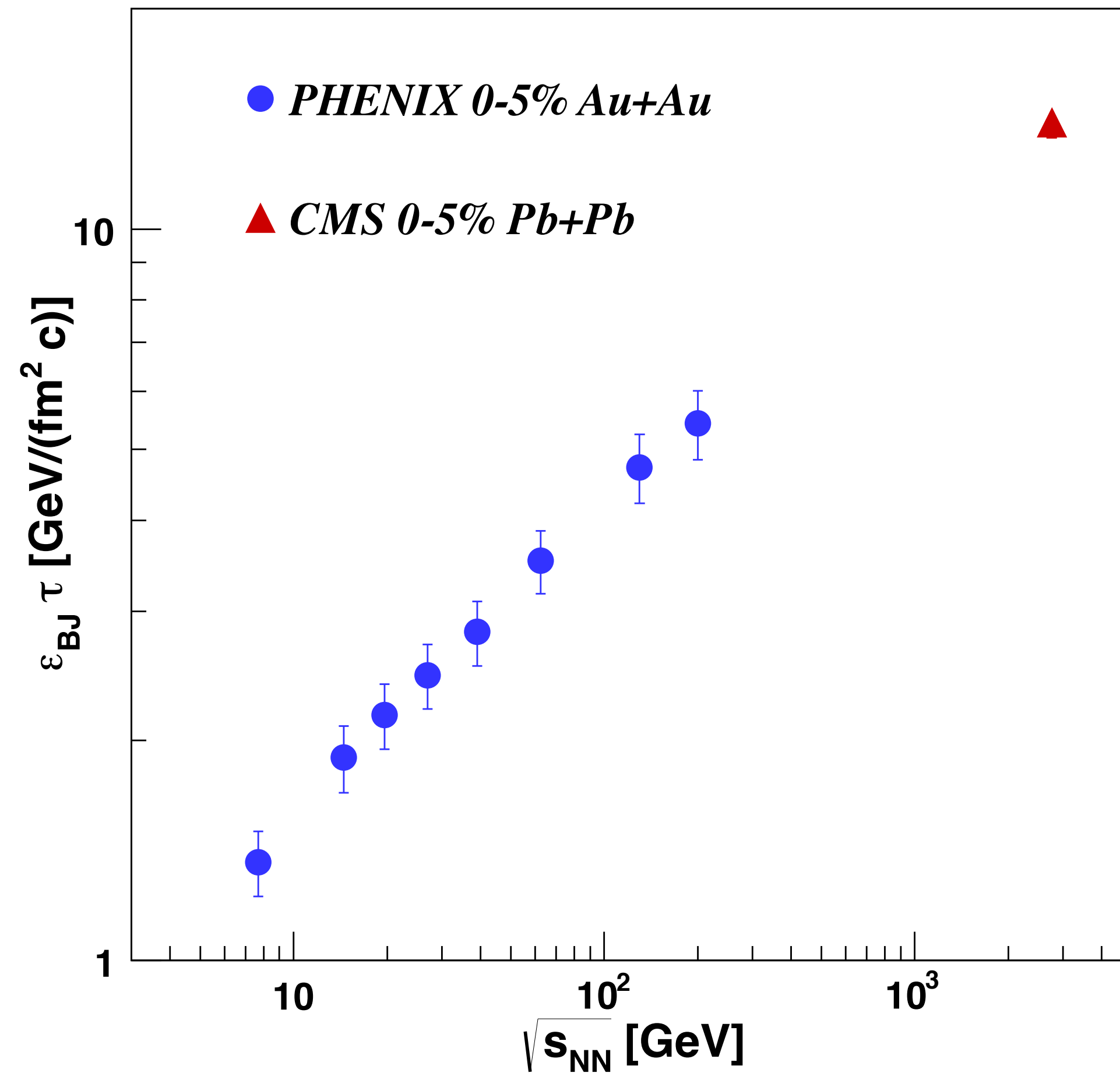
Radius of medium $\sim 7 \text{ fm}$

Time to thermalize system



ALI-PUB-59646

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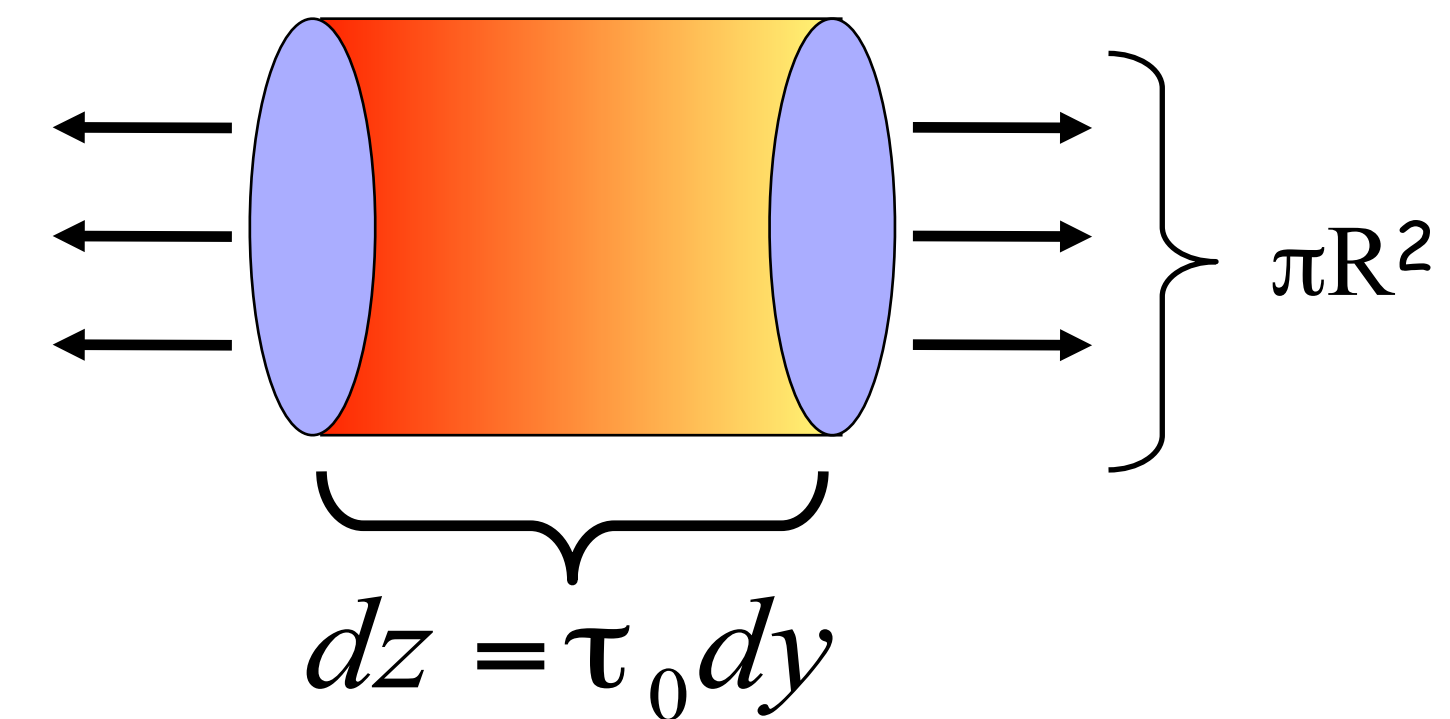
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Radius of medium $\sim 7 \text{ fm}$

Time to thermalize system



ϵ_{Bj} (LHC) $\approx 10 \text{ GeV}/\text{fm}^3$
 ~ 75 times normal nuclear density
 ~ 15 times $> \epsilon_{\text{critical}}$ (lattice QCD)

10 GeV/fm³. Is that a lot?

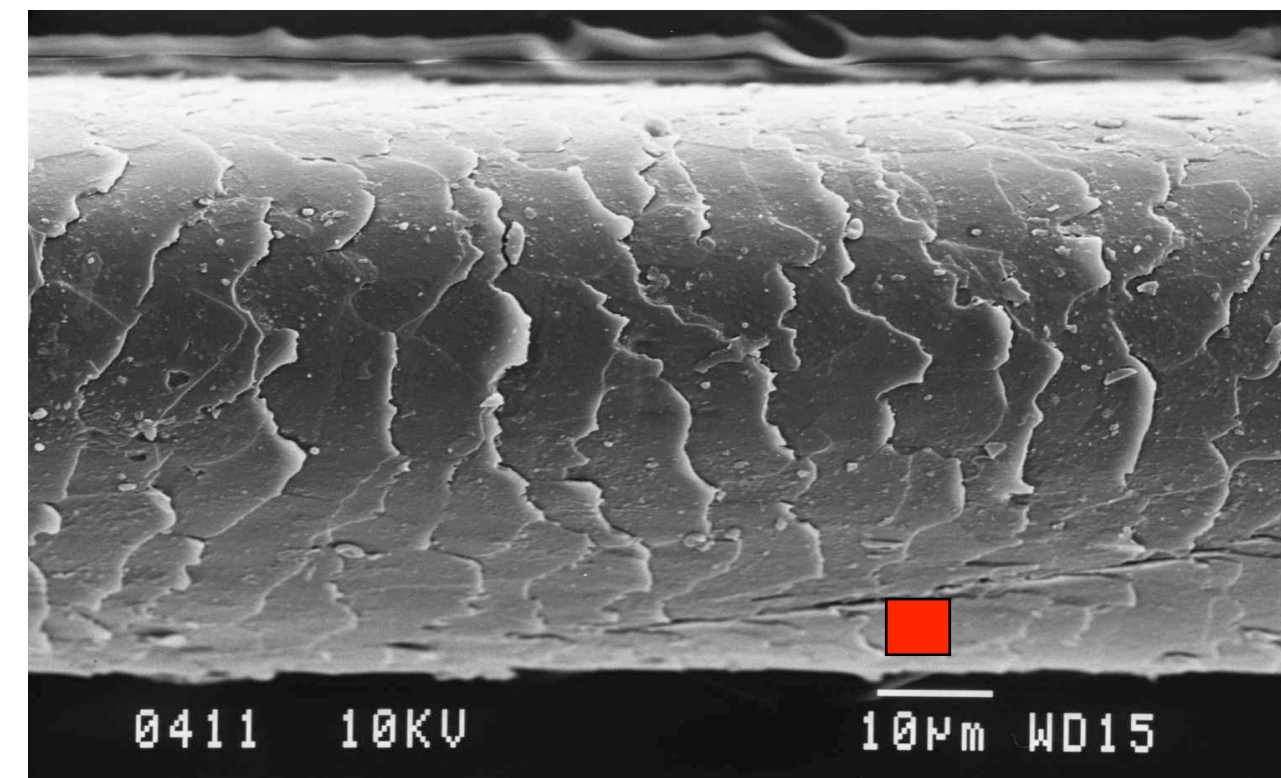
In a year, U.S.A (known energy hog) uses ~100 quadrillion BTUs of energy (1 BTU raises 1 lb water 1° F = 1 burnt match = 1,055 J). What size cube would you need to pack this energy into to produce equivalent energy density?

- A. A cube ~5 μm x ~5 μm x ~5 μm (approximate size of red blood cell)
- B. A cube ~10 mm x ~10 mm x ~5 mm (approximate size of corn kernel)
- C. A cube ~1 cm x ~30 cm x ~20 cm (approximately size of your laptop)
- D. A cube ~1 m high by 94,326 km² (approximately the area of Indiana)?

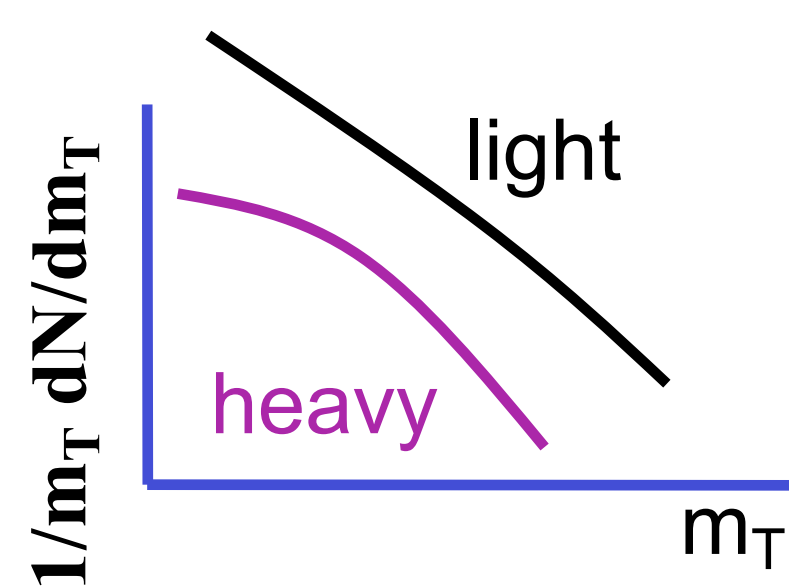
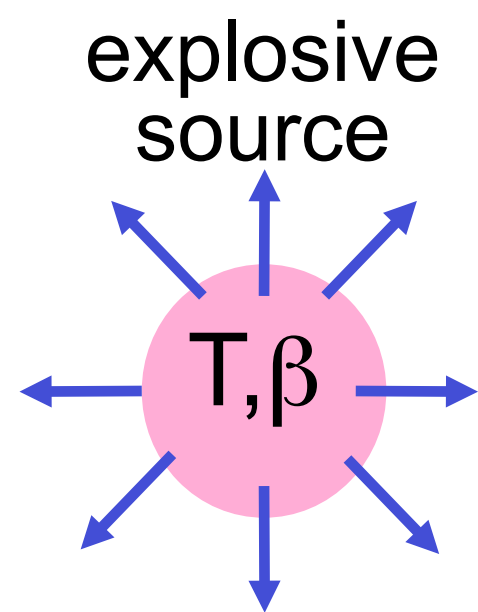
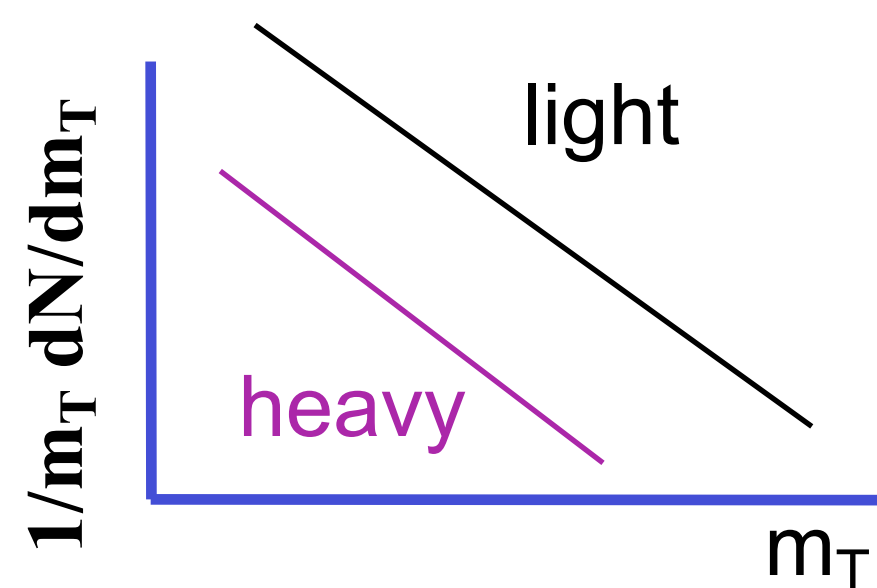
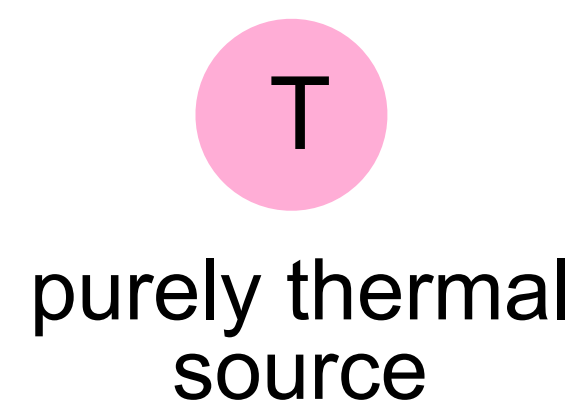
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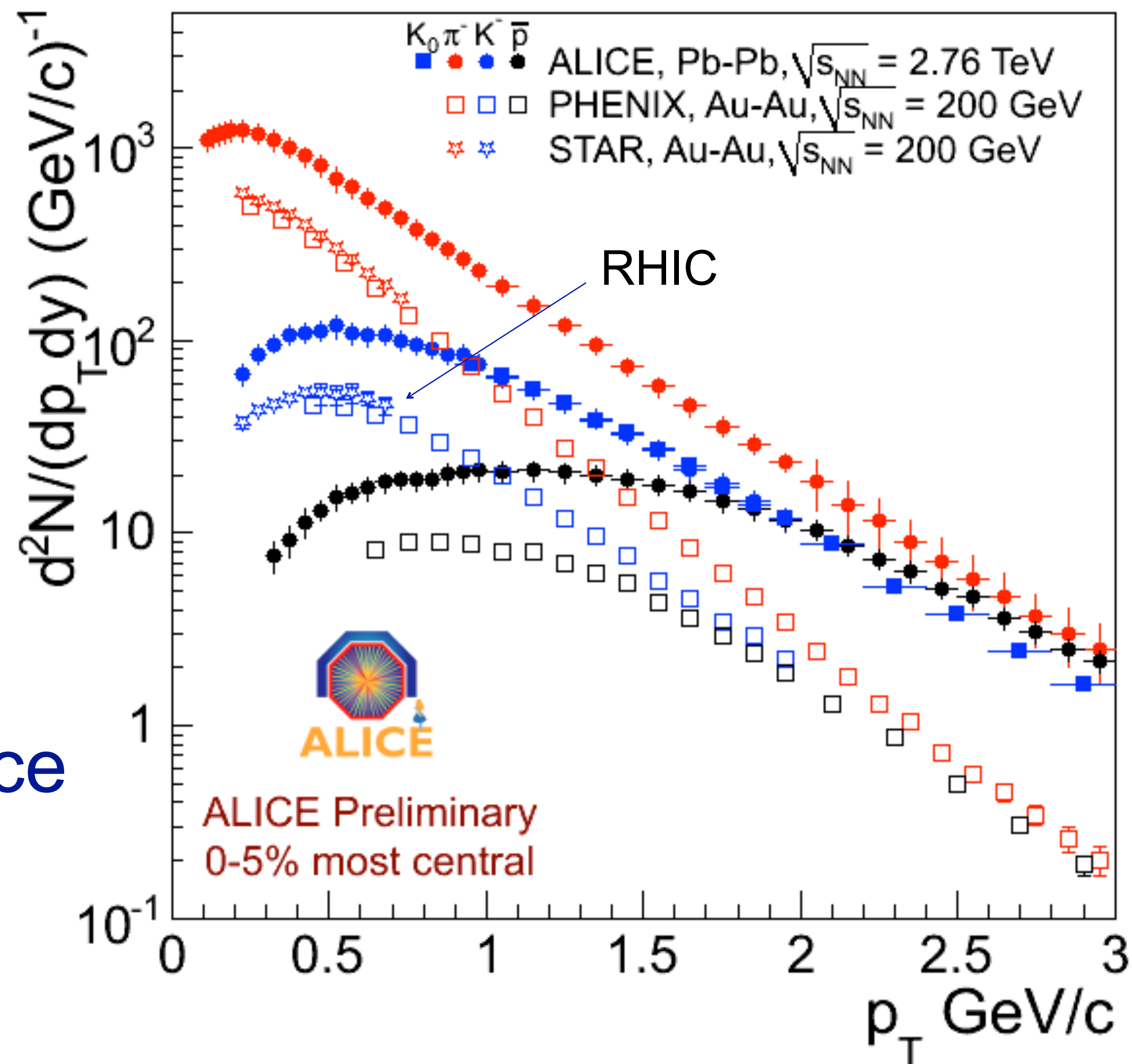
Kinematics after last scattering



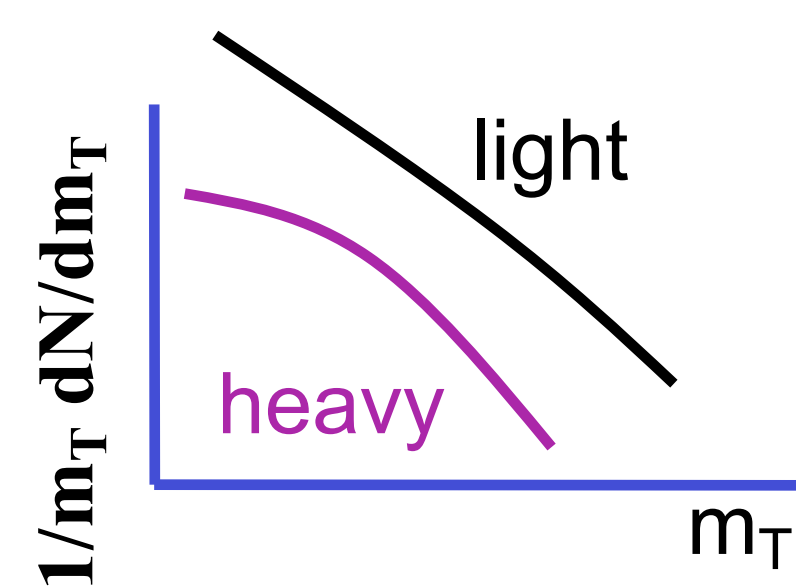
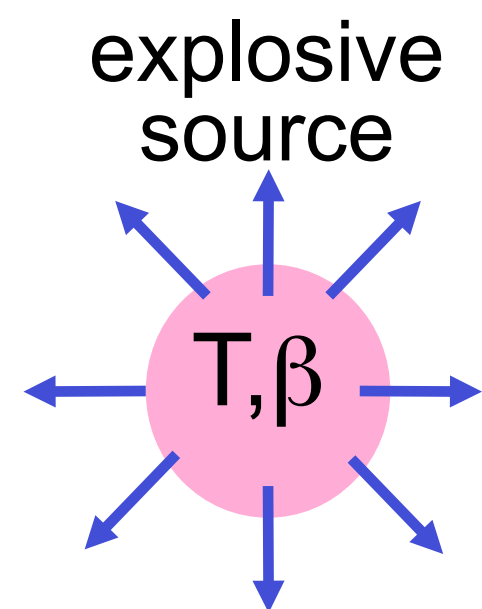
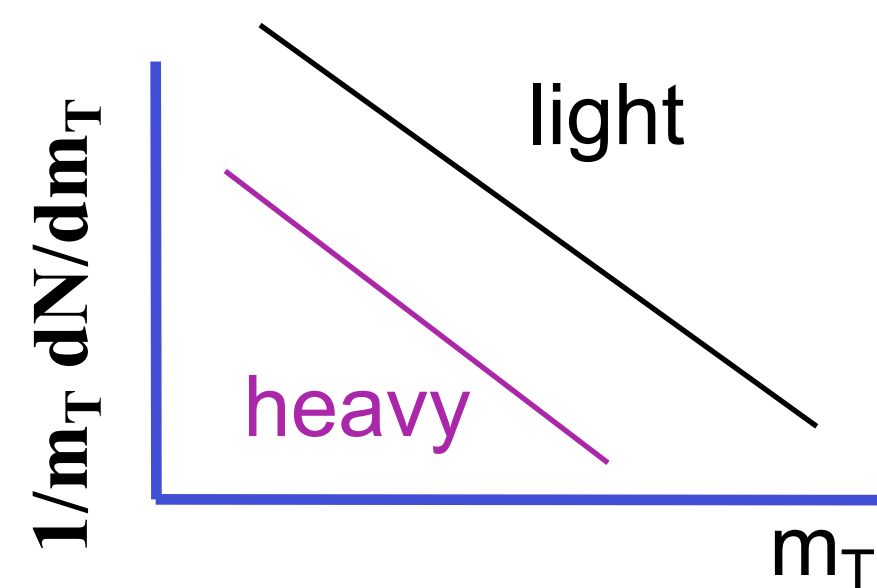
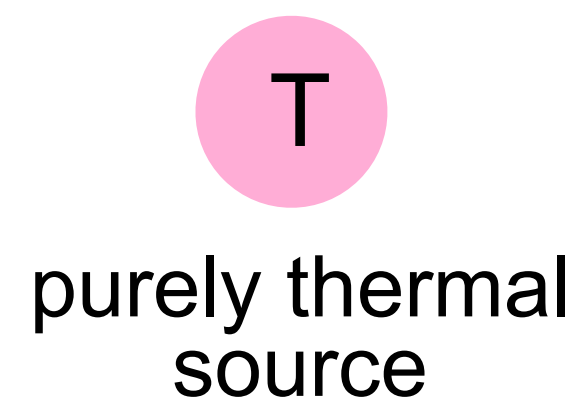
$$m_T = (p_T^2 + m^2)^{1/2}$$

See expected mass dependence

Spectra much harder and yield higher at LHC than RHIC



Kinematics after last scattering

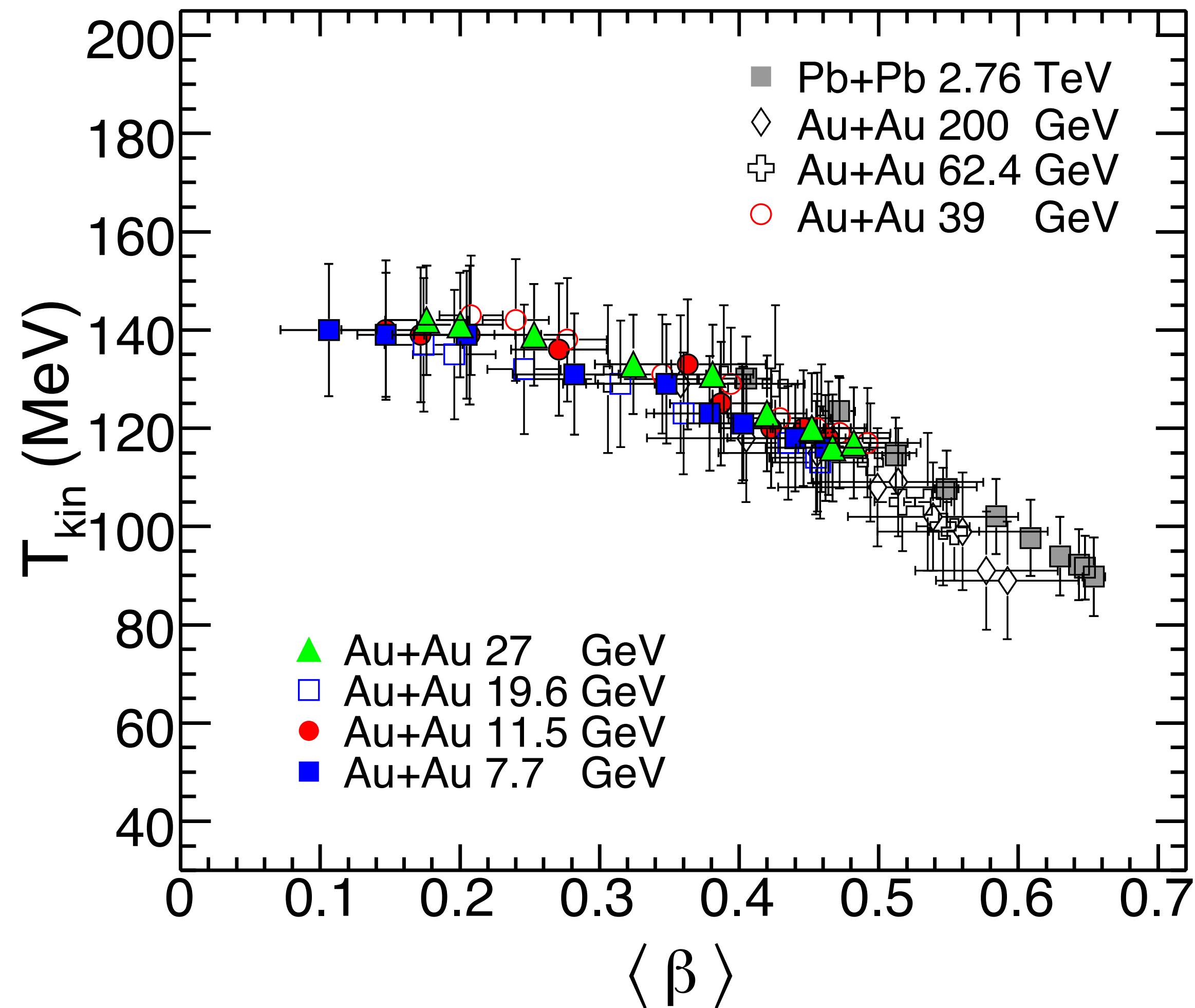


$$m_T = (p_T^2 + m^2)^{1/2}$$

See expected mass dependence

Spectra much harder and yield higher at LHC than RHIC

QGP expands explosively



Only gives access to temp at kinetic freeze-out

Temperature of chemical freeze-out

Number of particles of a given species related to T

$$dn_i \sim e^{-(E-\mu_B)/T} d^3p$$

Assume all particles described by same T and μ_B
 One ratio (e.g., \bar{p} / p) determines μ_B / T :

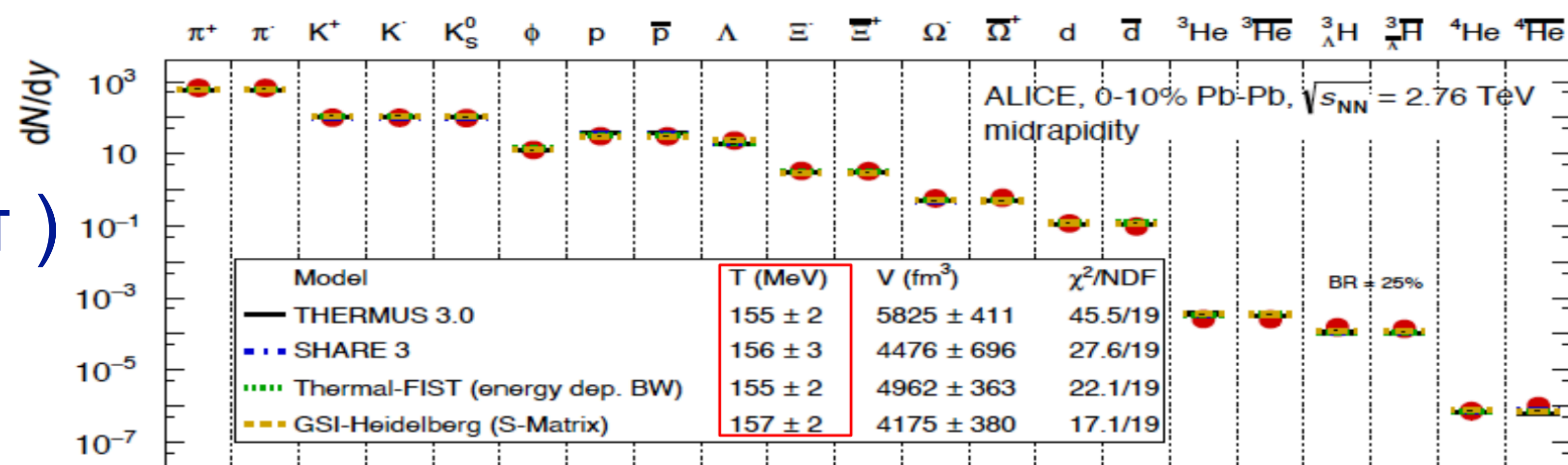
$$\frac{\bar{p}}{p} = \frac{e^{-(E+\mu_B)/T}}{e^{-(E-\mu_B)/T}} = e^{-2\mu_B/T}$$

A second ratio (e.g., K / π) provides $T \rightarrow \mu$

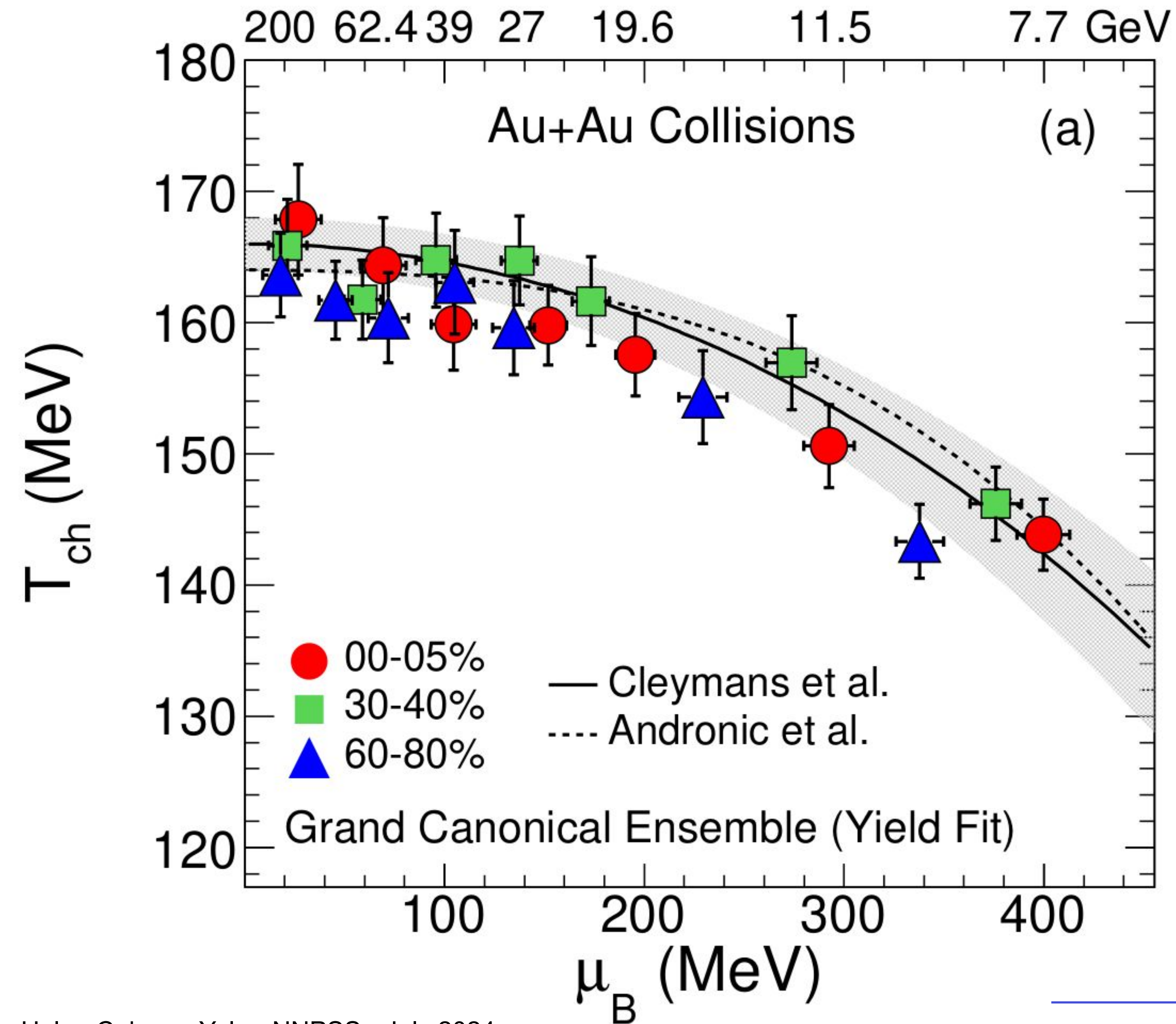
$$\frac{K}{\pi} = \frac{e^{-E_K/T}}{e^{-E_\pi/T}} = e^{-(E_K - E_\pi)/T}$$

Then all other hadronic ratios (and yields) defined

Chemical Freeze-out temperature T_{ch} close to that of T_{pc} at top energies



Temperature of chemical freeze-out



Below 200 GeV:

Baryon chemical potential becomes significant
 T_{ch} reduces

But this is T at which hadronic ratios are fixed.

Still not the initial T

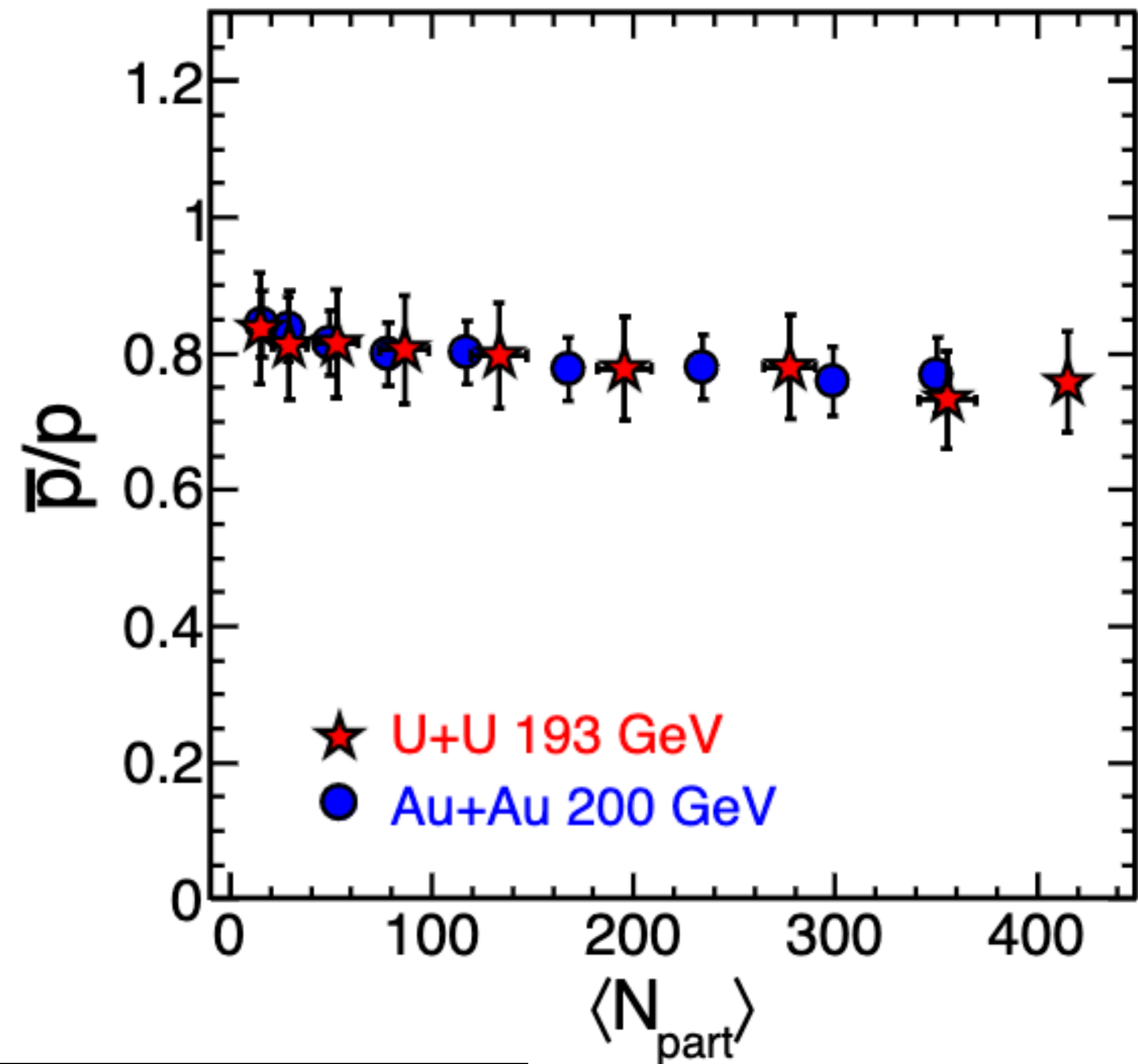
By the way!

Take a second look at the anti-proton/proton ratio

$$\bar{p}/p \sim 0.8$$

There is a net baryon number at mid-rapidity!!

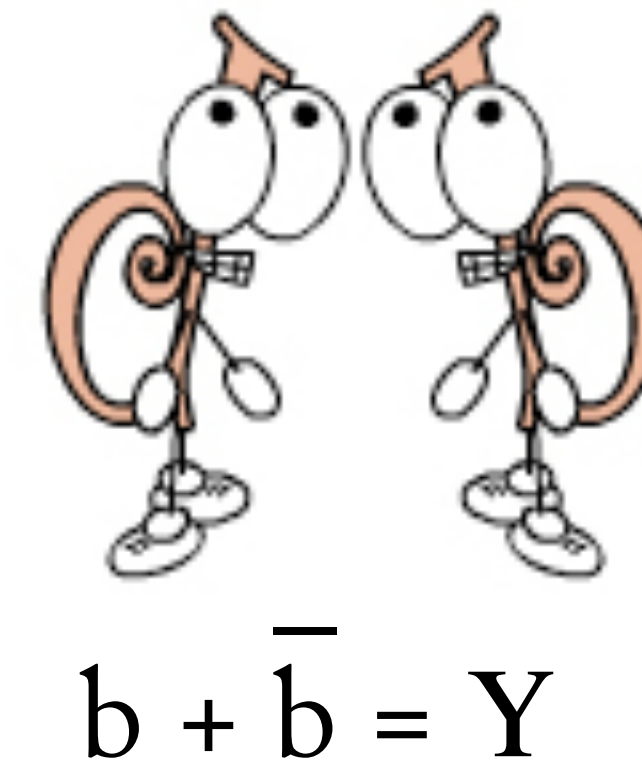
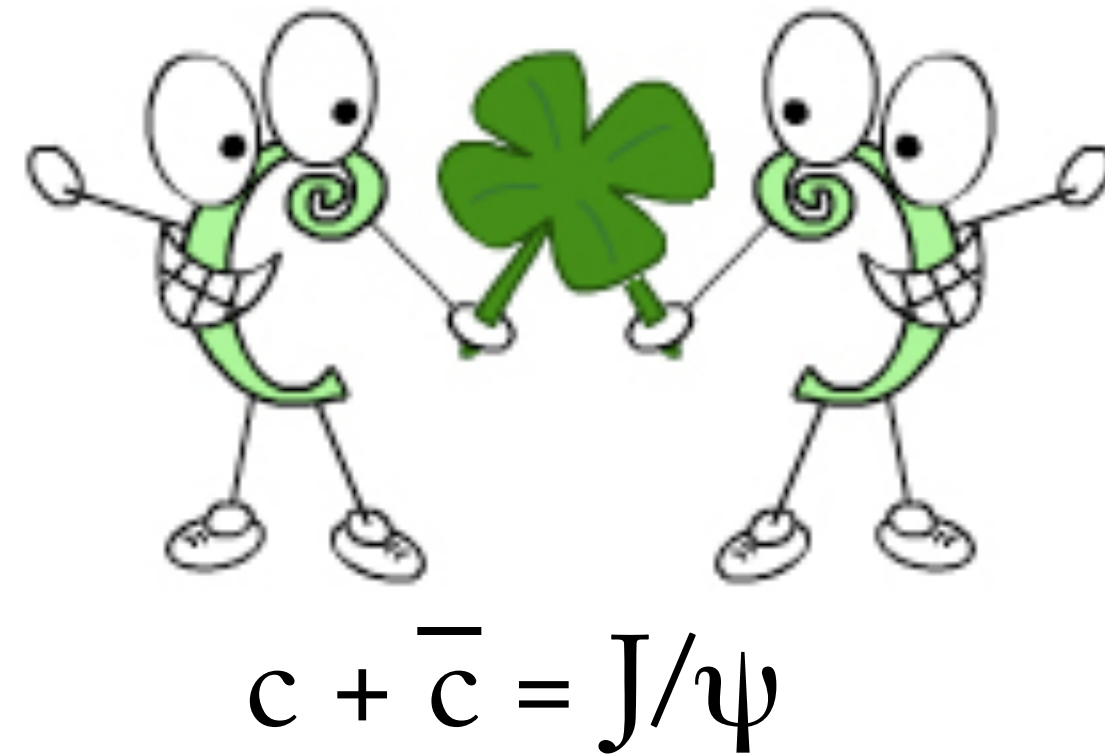
Baryons number is being transported over 6 units of rapidity from the incoming beams to the collision zone!



Where does baryon number reside?

Melting quarkonia

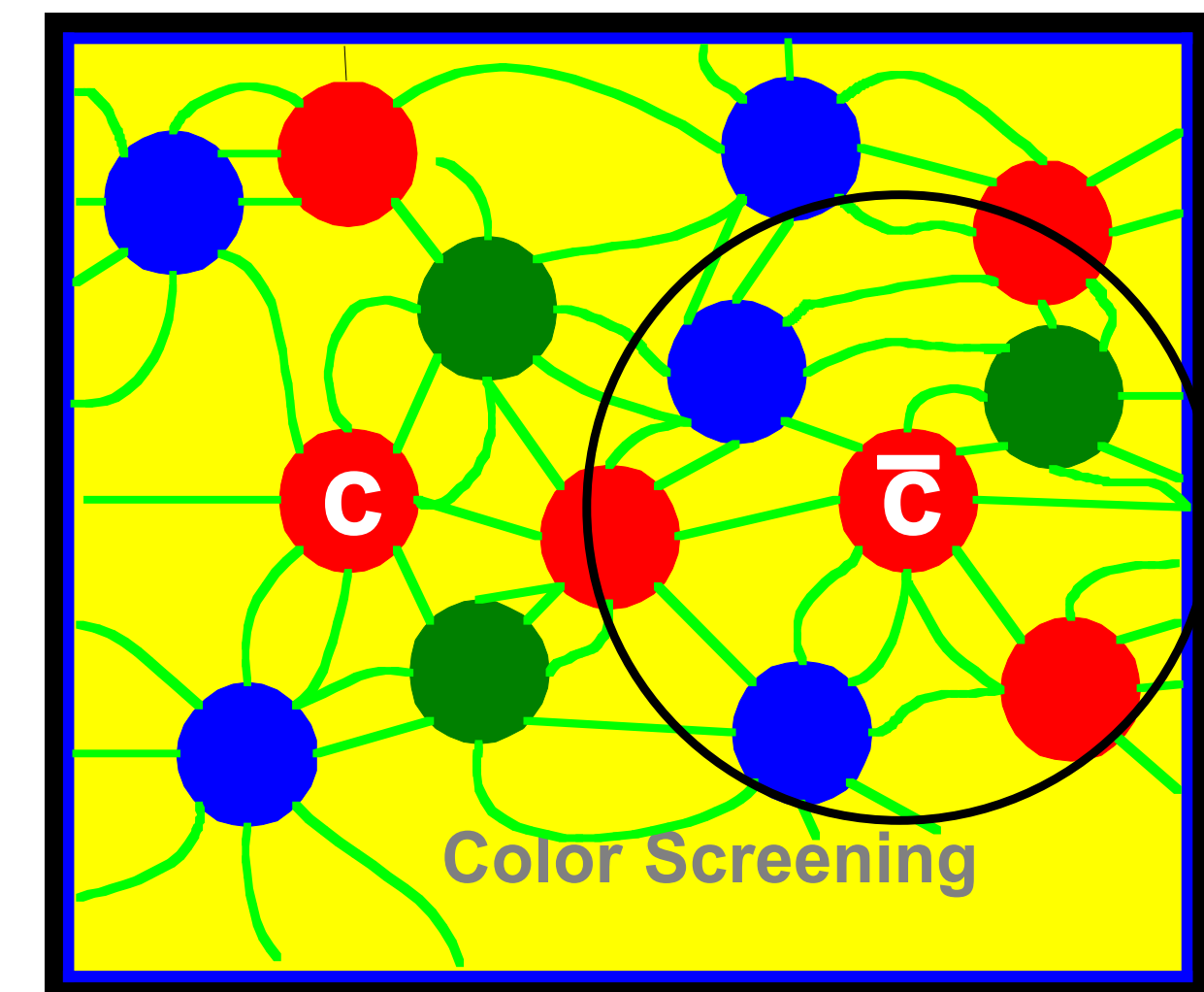
Quarkonia - bound states of heavy quark-anti-quark pairs



Formed only in the very early stages of the collision due to their high masses

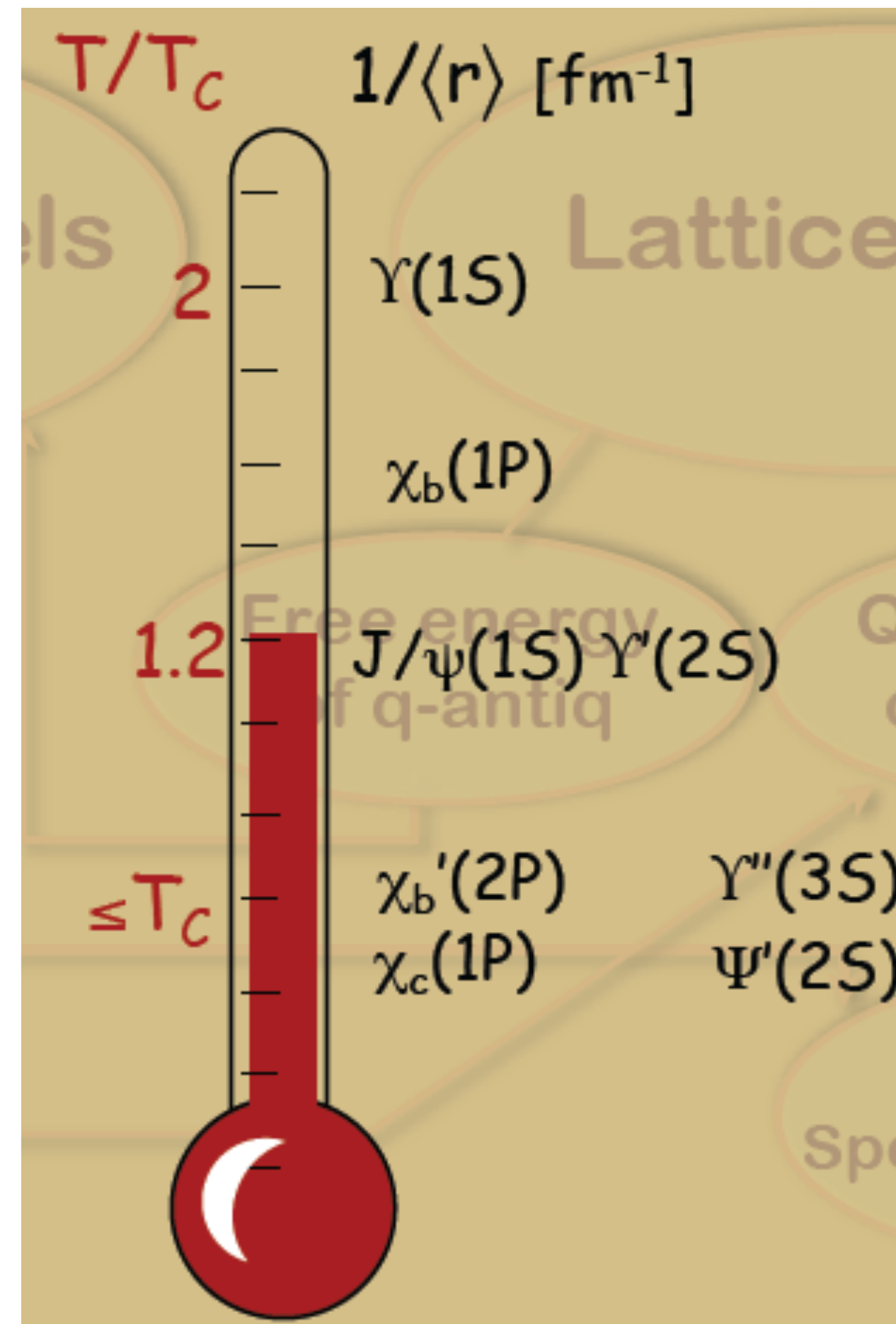
Only loosely bound

Melt in the QGP



Quarkonia - QGP thermometers

Color screening of static potential between heavy quarks



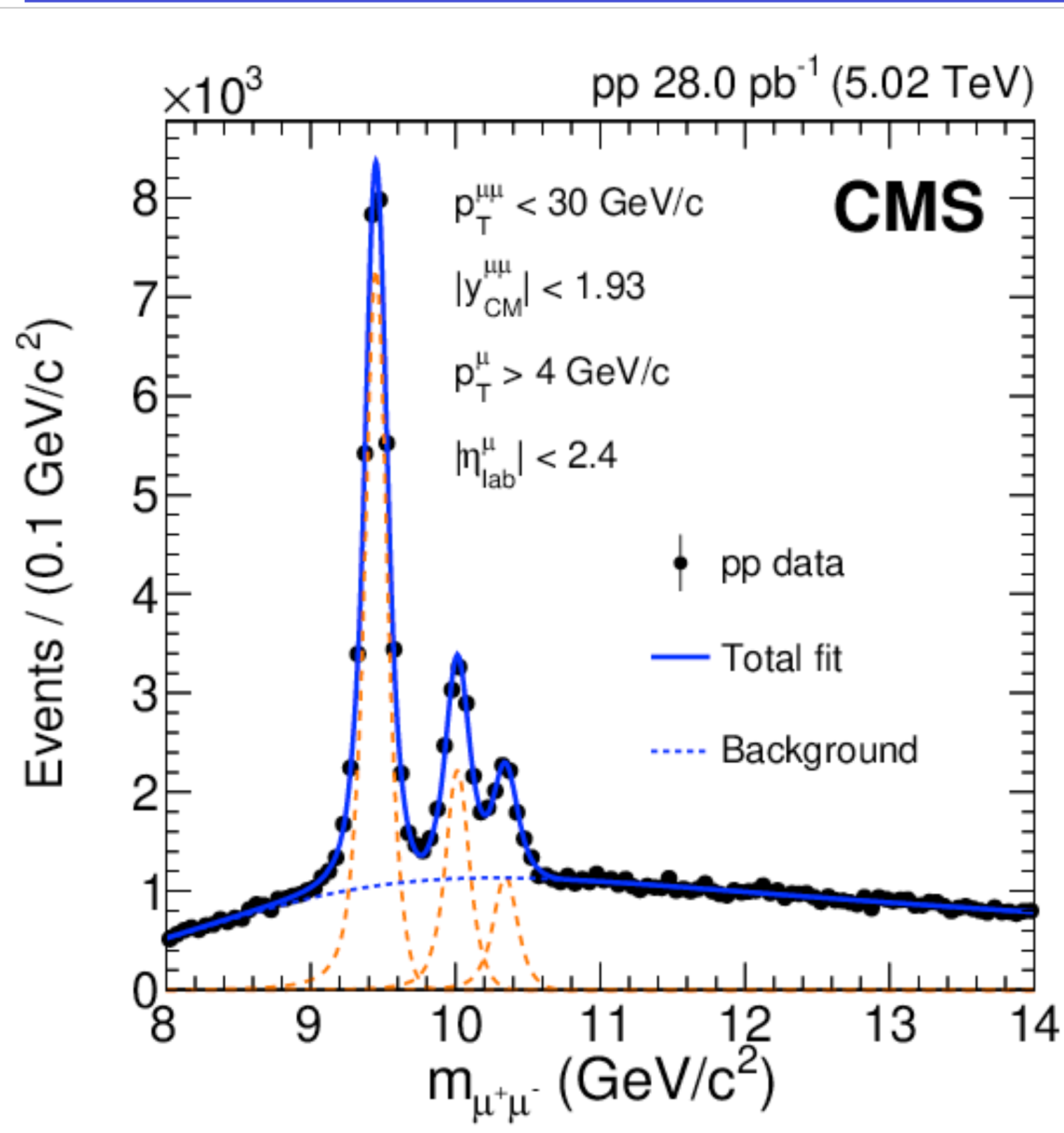
Charmonia: J/ψ , Ψ' , χ_c

Bottomonia: $\Upsilon(1S)$, $\Upsilon(2S)$, $\Upsilon(3S)$

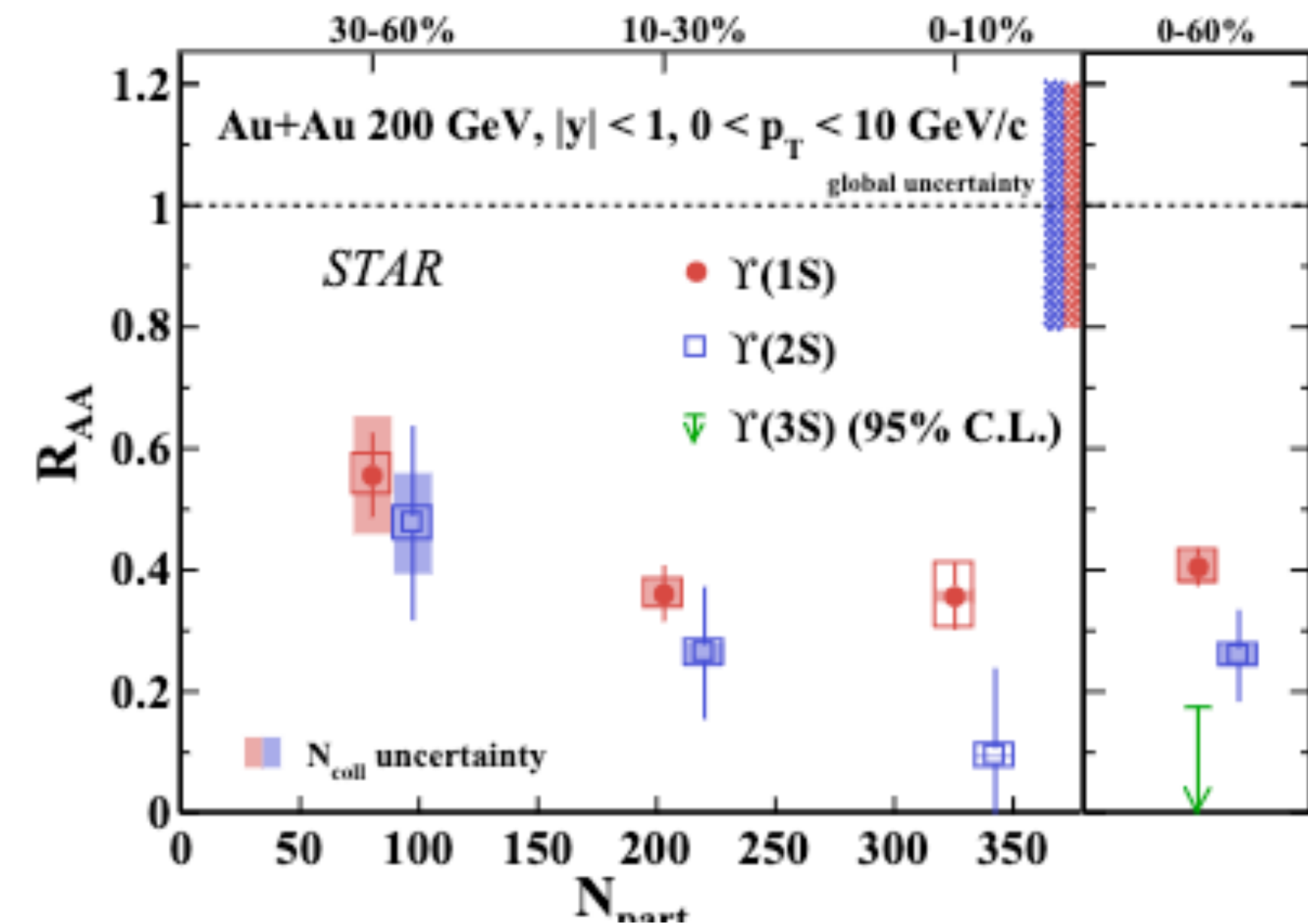
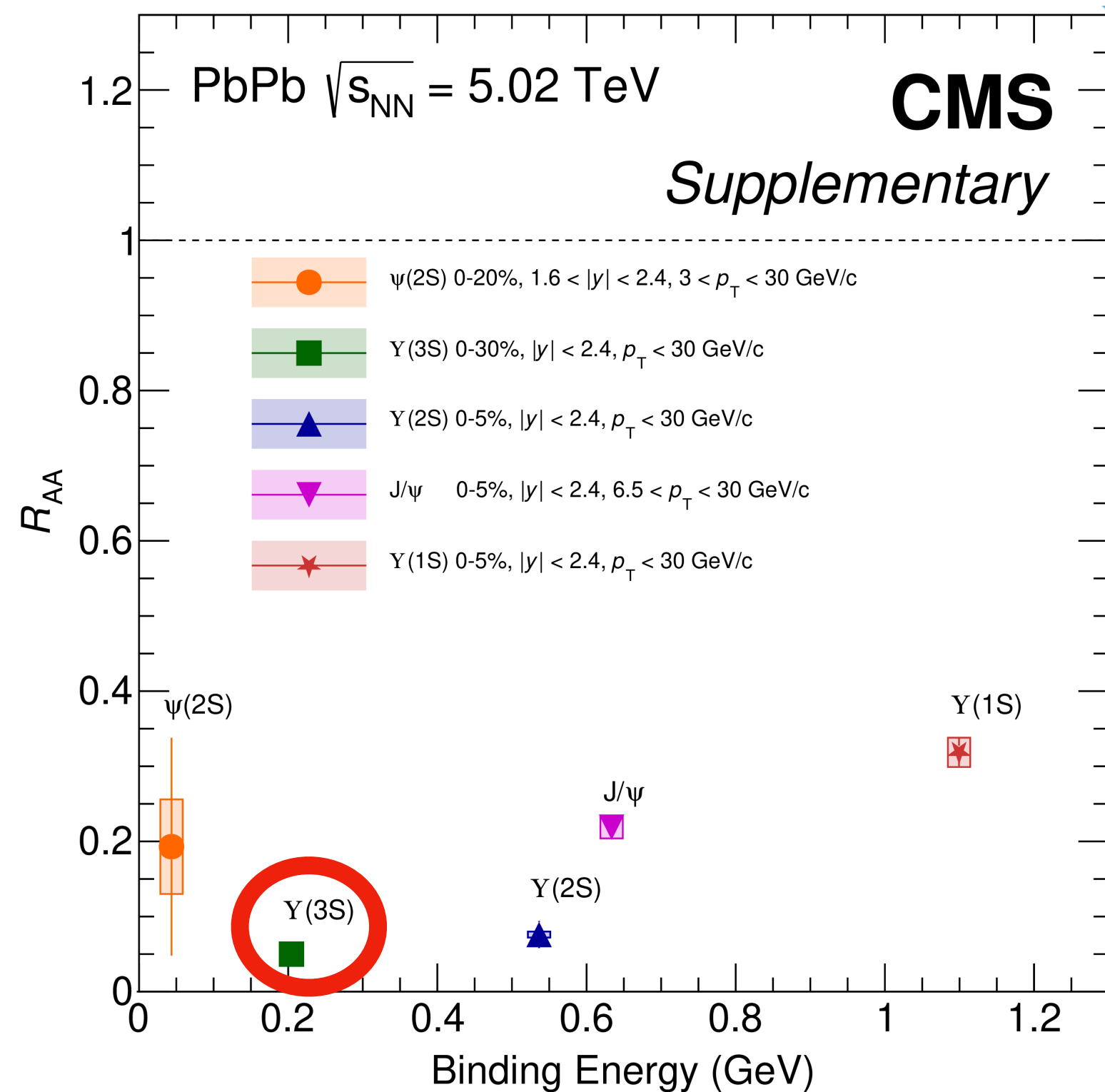
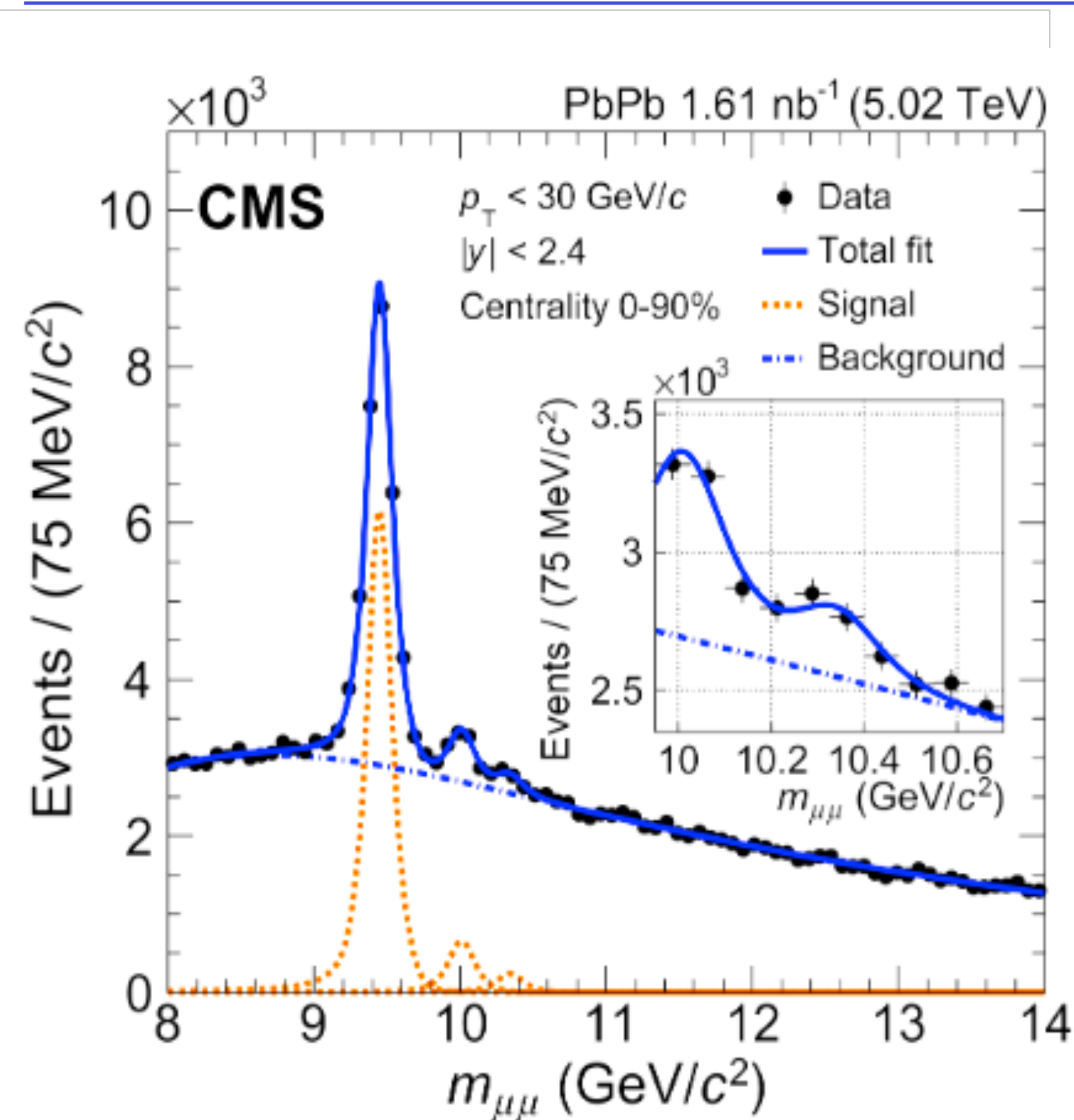
	E_{binding} (GeV)
J/ψ	0.64
ψ'	0.05
χ_c	0.2
$\Upsilon(1S)$	1.1
$\Upsilon(2S)$	0.54
$\Upsilon(3S)$	0.31

Suppression determined by
T and binding energy

Sequential melting of quarkonia



Sequential melting of quarkonia



Lightly bound states:

almost completely gone

Tightly bound states:

mostly melted at LHC energies

and top RHIC

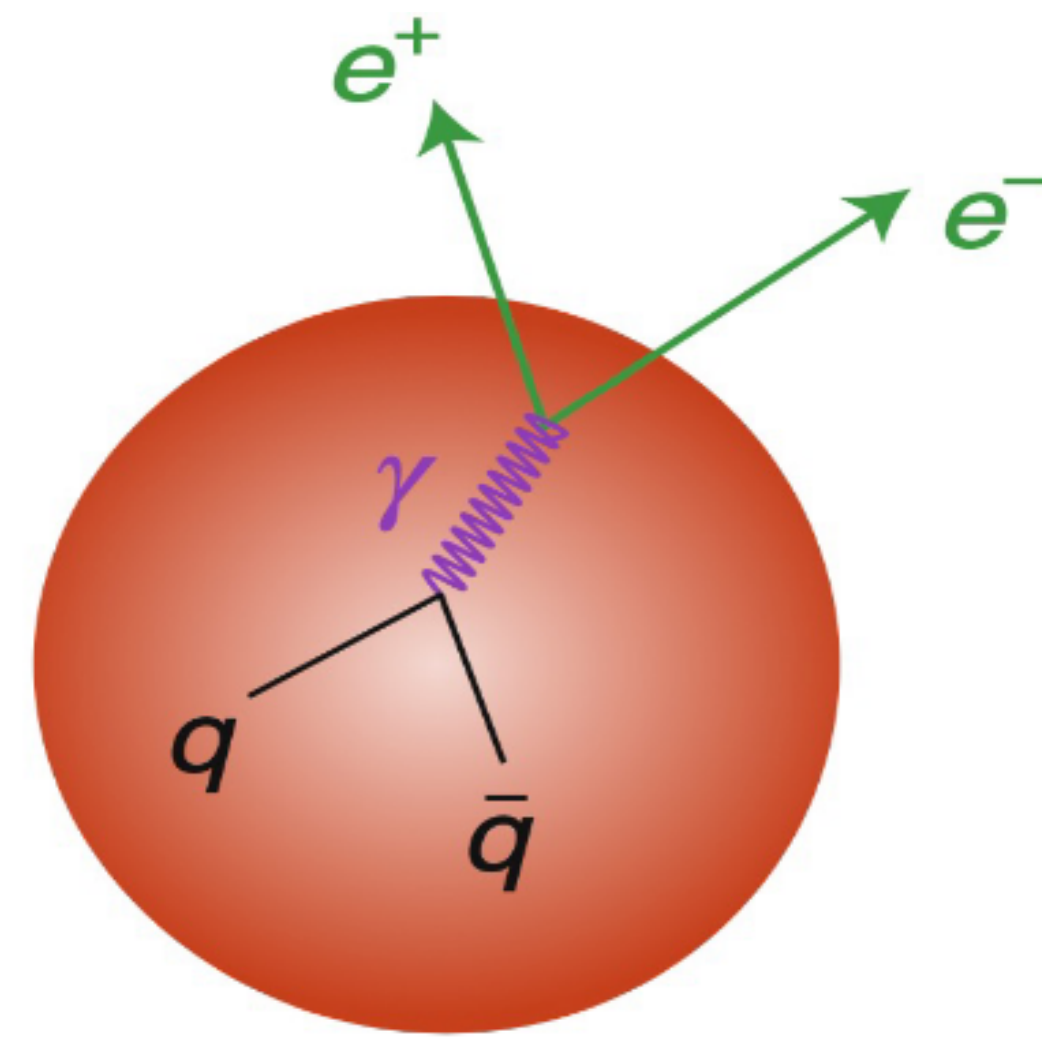
$T > 1.5 T_c \sim 300 \text{ MeV}$

Extracting the initial T : non-interacting probe

Di-leptons probe medium over its whole evolution.
Escape medium without interacting (no color charge)

Production rate proportional to
QGP temperature

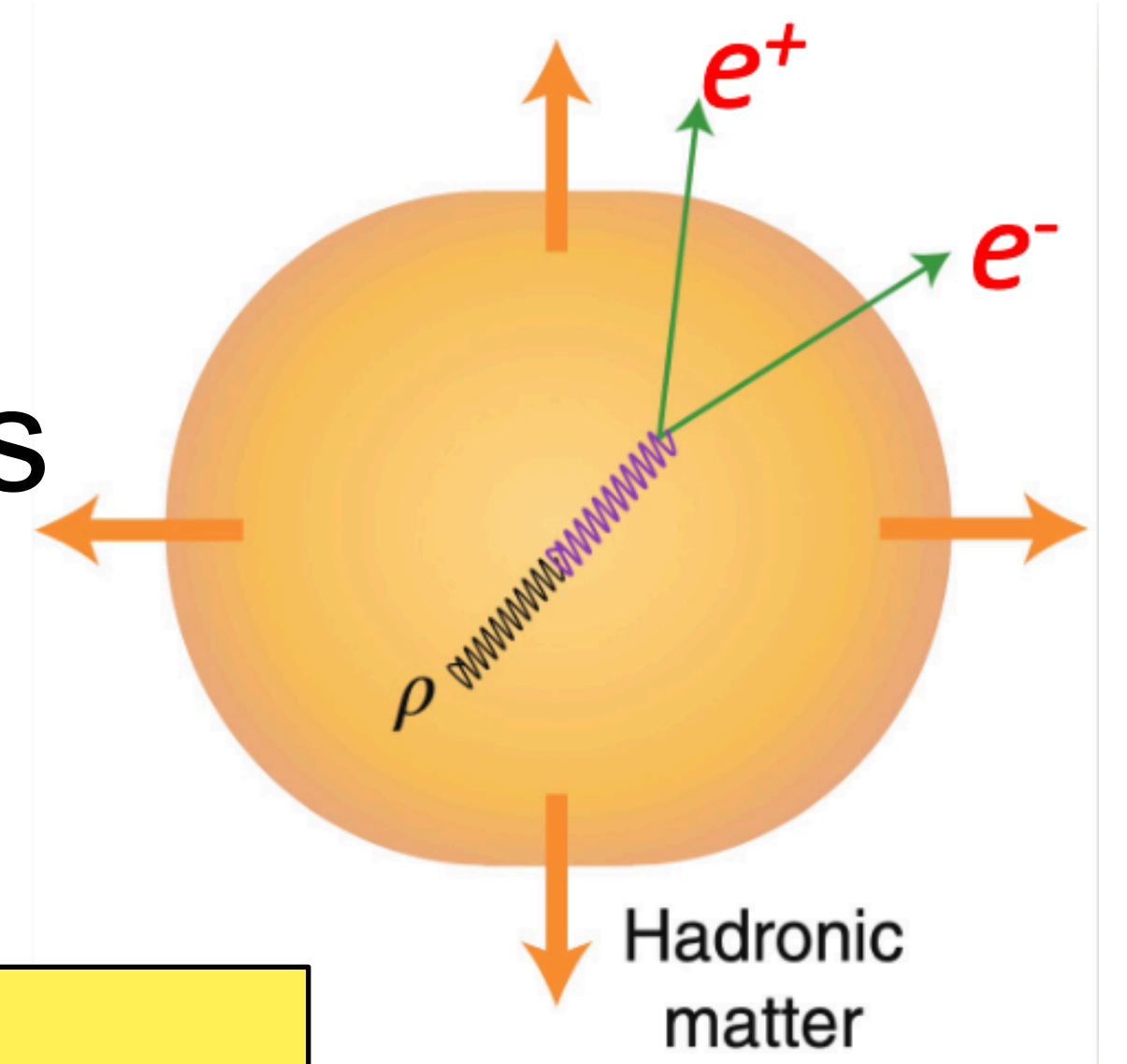
: Early time measurement



Quark-gluon
plasma

ρ spectral function broadens
when sitting in hot bath

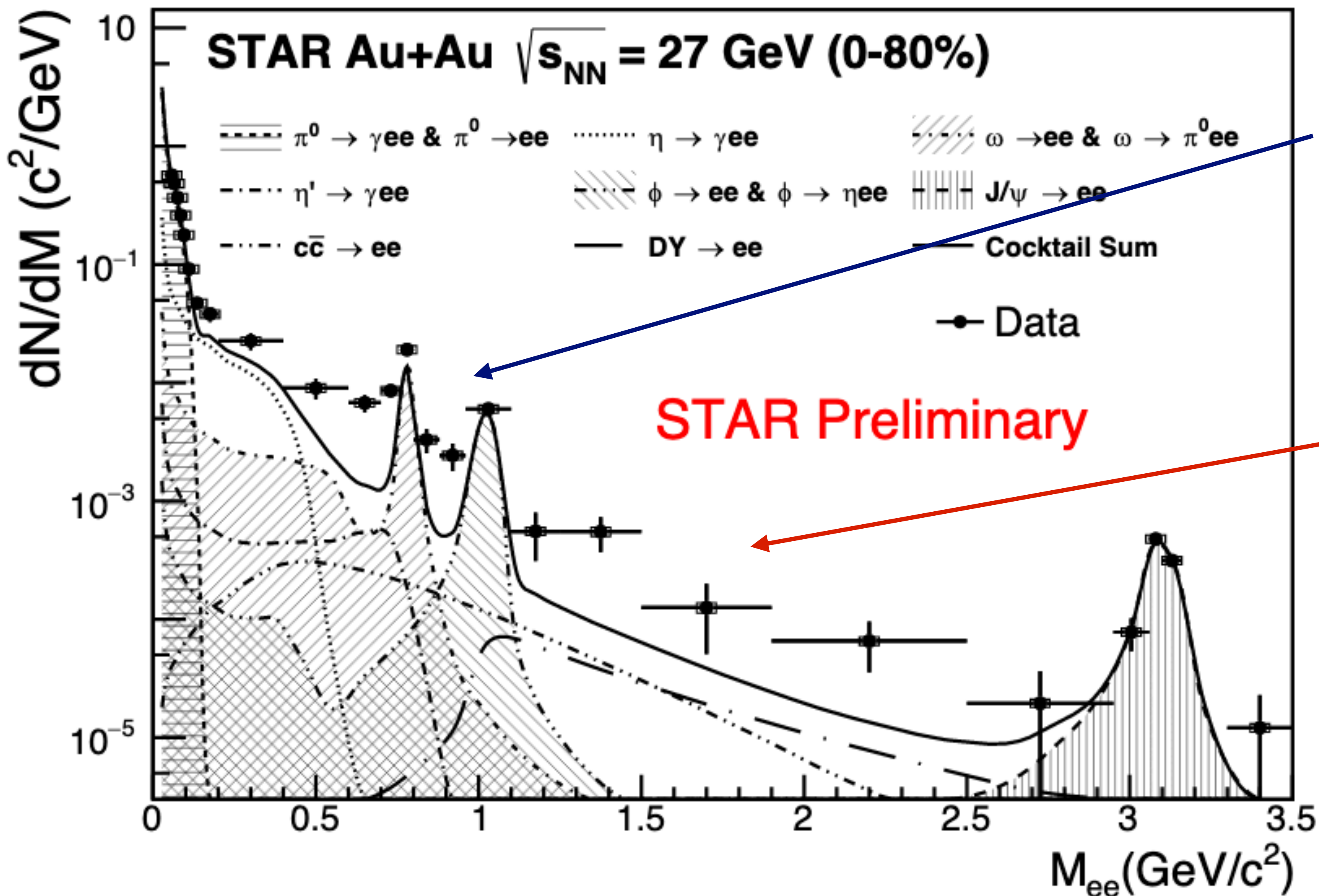
: Later time measurement



Hadronic
matter

Two for the price of one:
Different di-lepton invariant mass
ranges probe different times

Extracting the signal



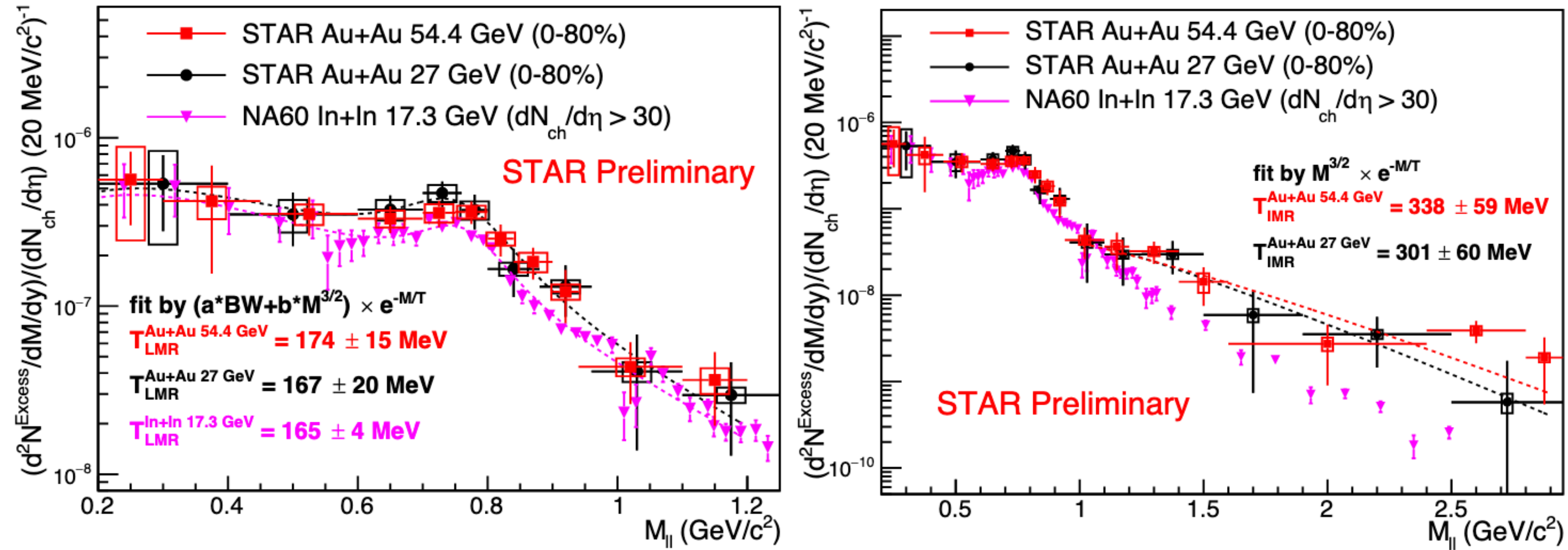
Low mass range

STAR Preliminary

Intermediate mass range

Clear enhancement for LMR and IMR

Extracting the temperatures



Low mass range: Similar mass spectrum, similar T ,
in-medium ρ produced & broadened in similar heat
bath from $\sqrt{s_{NN}} = 17-56$ GeV

Intermediate mass range:

$$T(\sqrt{s_{NN}} = 54.6) = 338 \pm 59 \text{ MeV} \sim T(\sqrt{s_{NN}} = 27) = 301 \pm 60 \text{ MeV}$$

$$T(\sqrt{s_{NN}} = 17) \sim 246 \text{ MeV}$$

Different medium below 20 GeV?

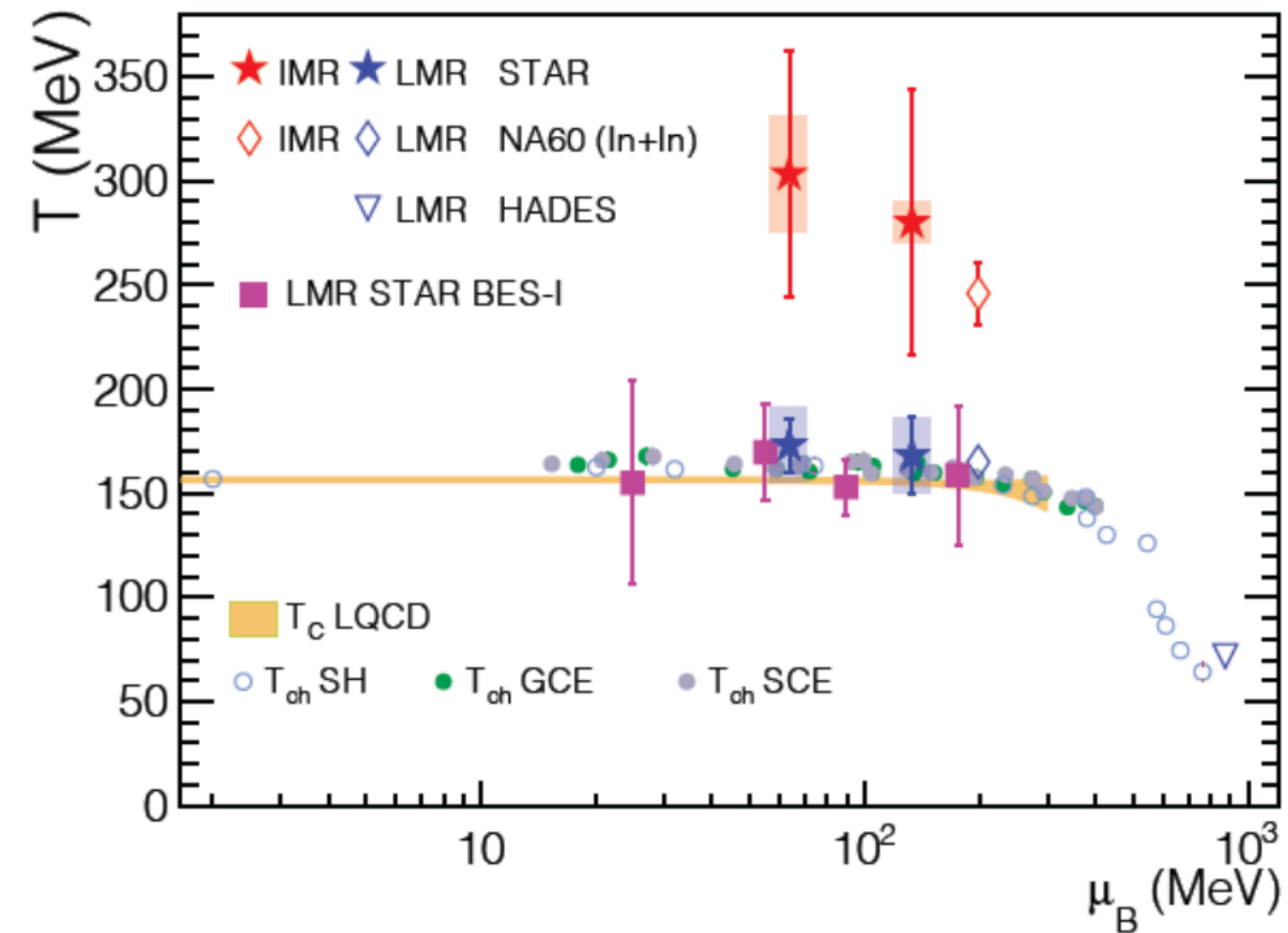
How hot is ~200 MeV ?

- A. Approximately the same as the hottest recorded T in Indiana (~46.7 °C/116 °F, Collegeville, 1936)
- B. Approximately that of molten gold (~1000 °C)
- C. Approximately that of the center of the sun (~15 million °C)
- D. Approximately that of a supernova (~10 billion °C)
- E. Even hotter

How hot is ~200 MeV ?

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- D. Approximately that of a supernova (~10 billion °C)
- E. Even hotter ~0.1 trillion °C

Initial T summary



Higher chemical potentials
at lower $\sqrt{s_{NN}}$

Hadronization occurs at ~ 170 MeV

T_{pc} from lattice

(chemical fits and dileptons)

At top RHIC energies (and LHC)

Initial temperature > 300 MeV

(Quarkonia and photons)

Above $\sqrt{s_{NN}} \sim 30$ GeV

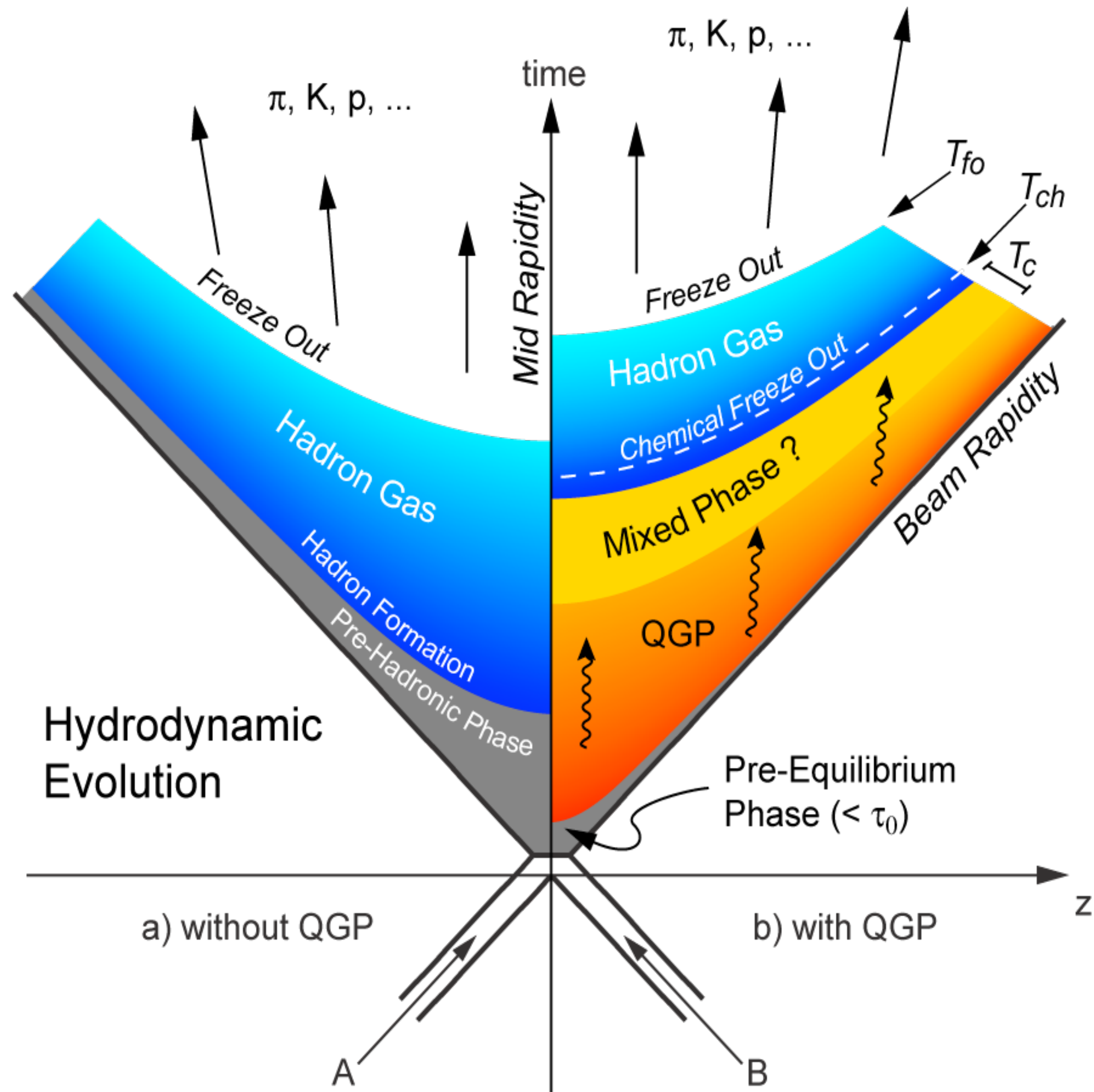
Initial temperature > 300 MeV

Potentially dropping below 20 GeV

(dileptons)

Initial T above T_{pc} for
 $\sqrt{s_{NN}} > 20$ GeV

Summary of the collision's evolution



Lattice (2-flavor):

$$T_C \approx 173 \pm 8 \text{ MeV}$$

$$\varepsilon_C \approx (6 \pm 2) T^4 \approx 0.70 \text{ GeV/fm}^3$$

Chemical freeze-out:

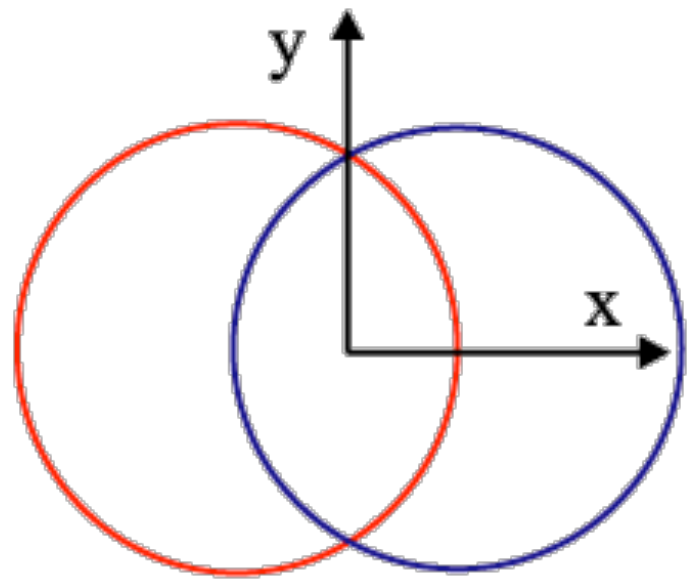
($T_{ch} \leq T_C$): inelastic scattering ceases

Kinetic freeze-out:

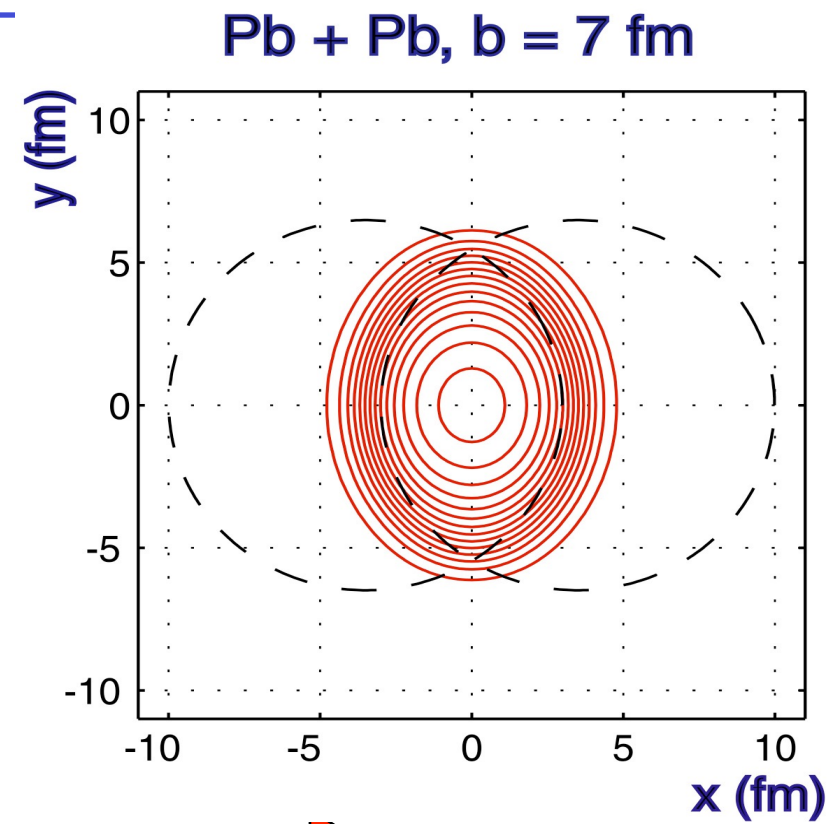
($T_{fo} \leq T_{ch}$): elastic scattering ceases

Many constituents \Rightarrow
Thermal Equilibrium?

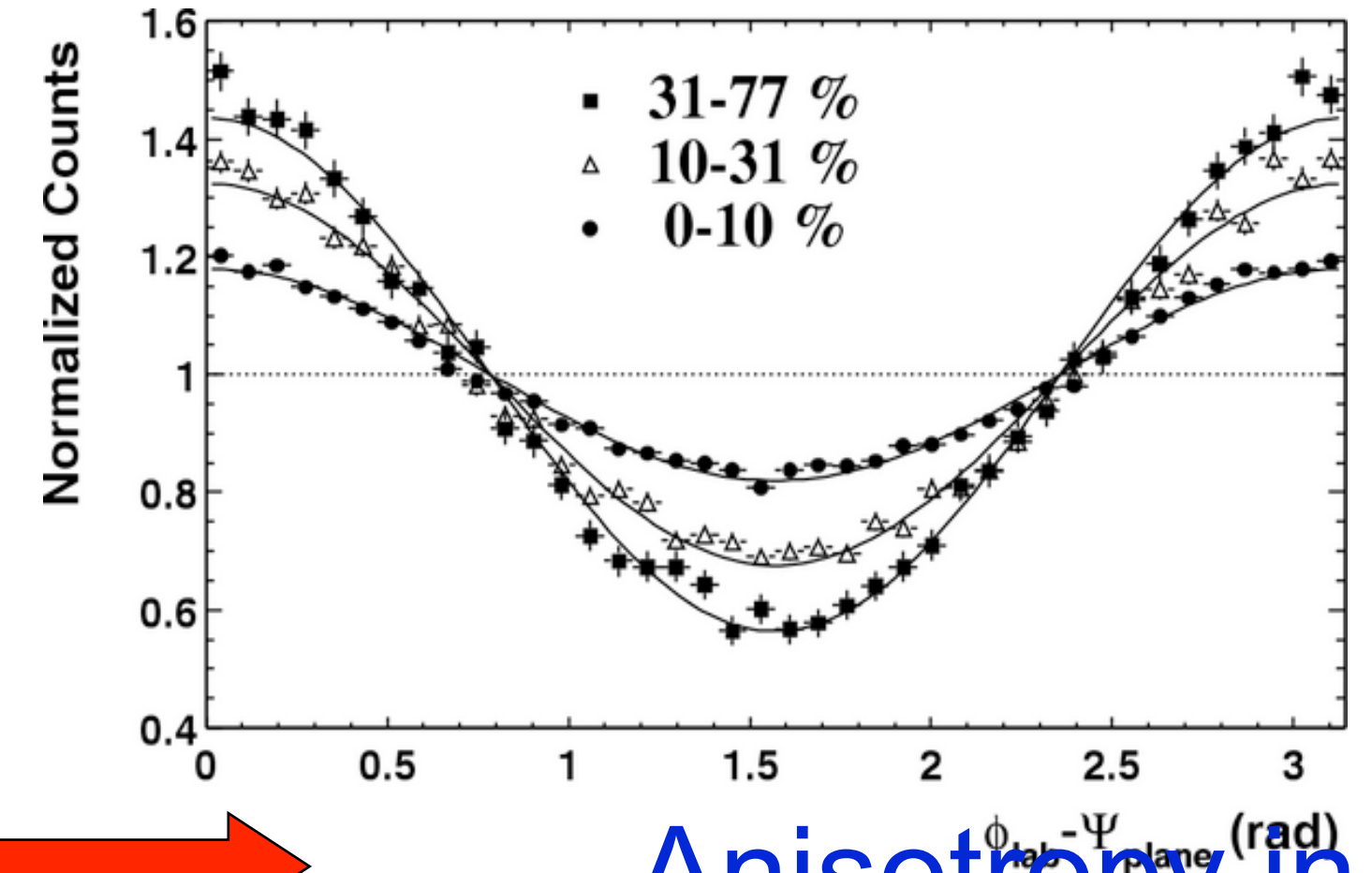
Initial conditions: Thermalization



Almond shape overlap region in coordinate space



Interactions/
Rescattering



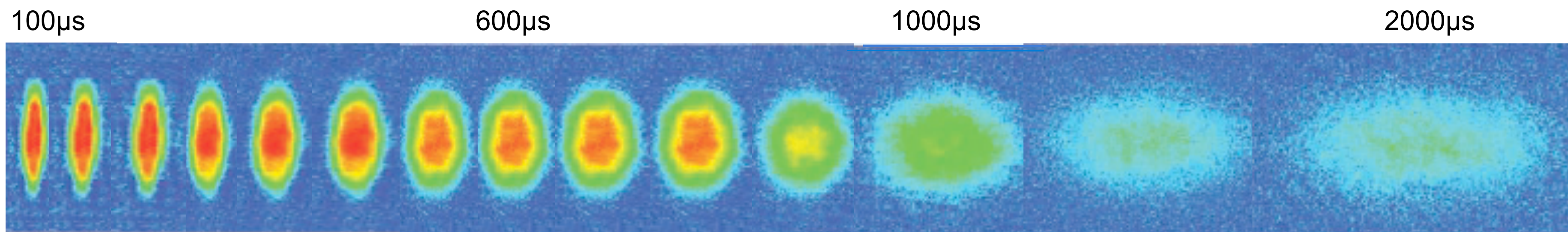
Anisotropy in momentum space

$$dN/d\phi \sim 1 + 2 v_2(p_T) \cos(2\phi) + \dots$$

$$\phi = \text{atan}(p_y/p_x)$$

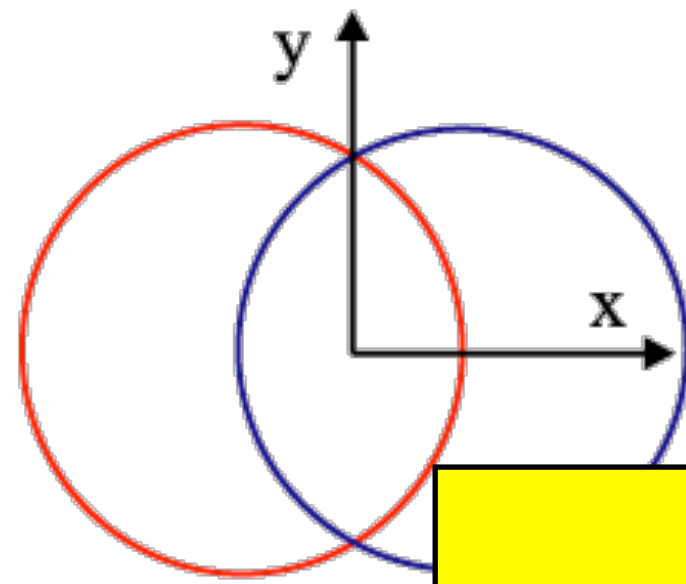
$$v_2 = \langle \cos 2\phi \rangle$$

v_2 : 2nd harmonic Fourier coefficient in $dN/d\phi$ relative to reaction plane

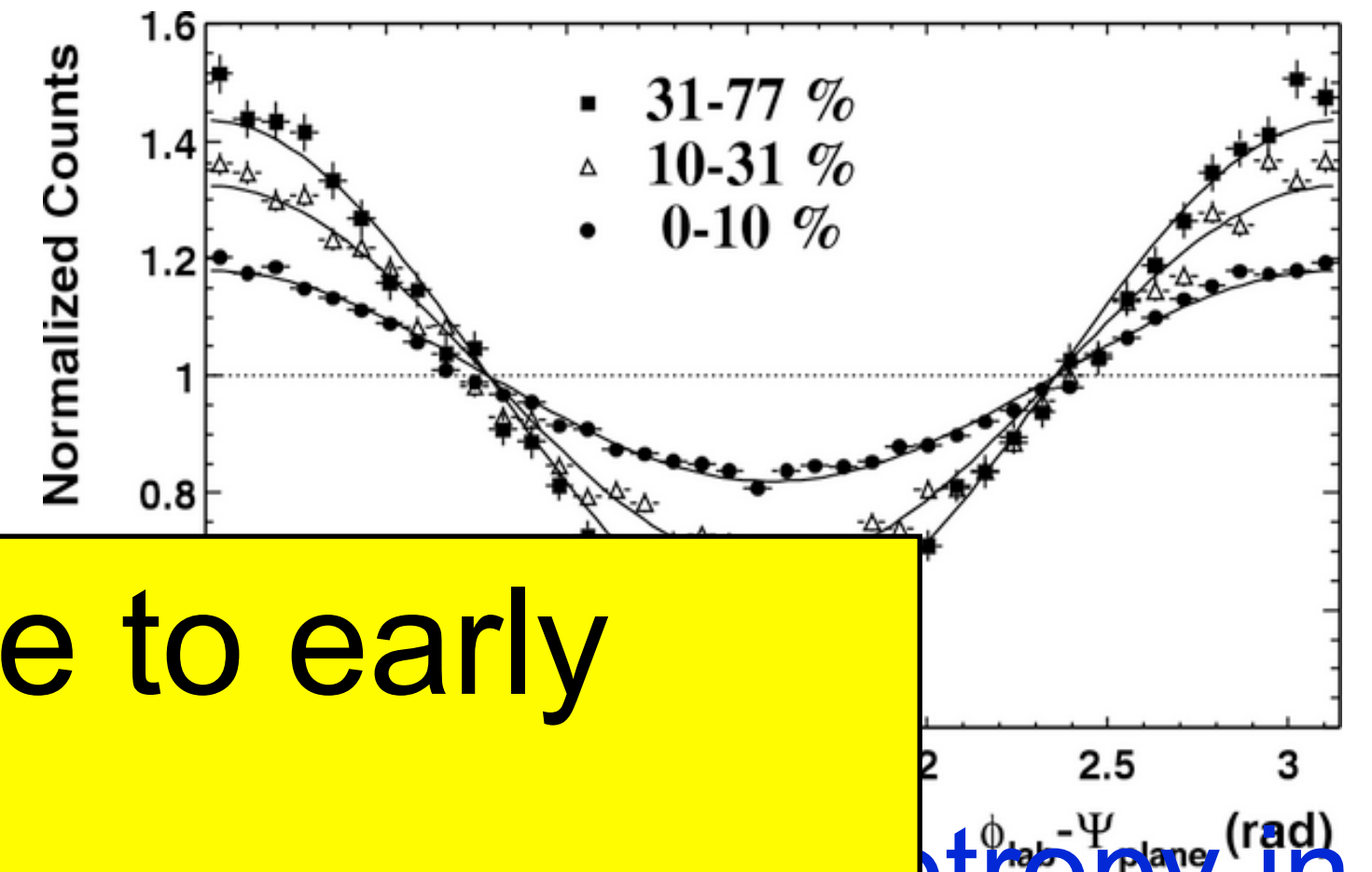
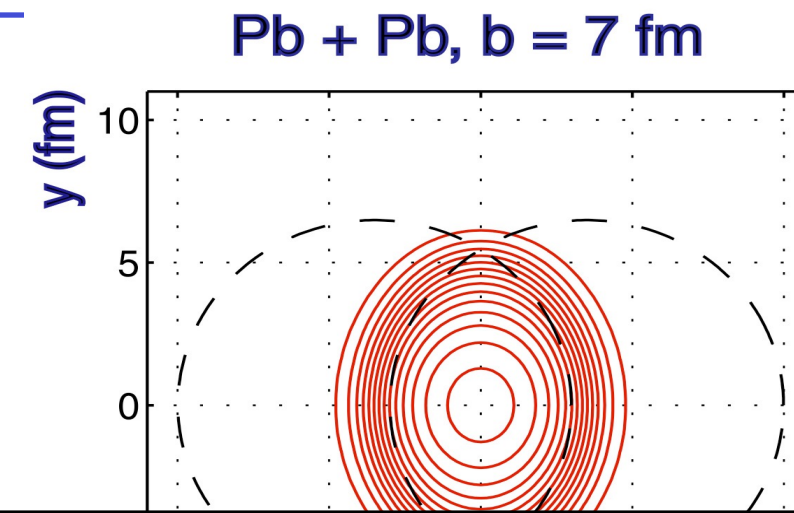


Time

Initial conditions: Thermalization



Almond shaped region in space

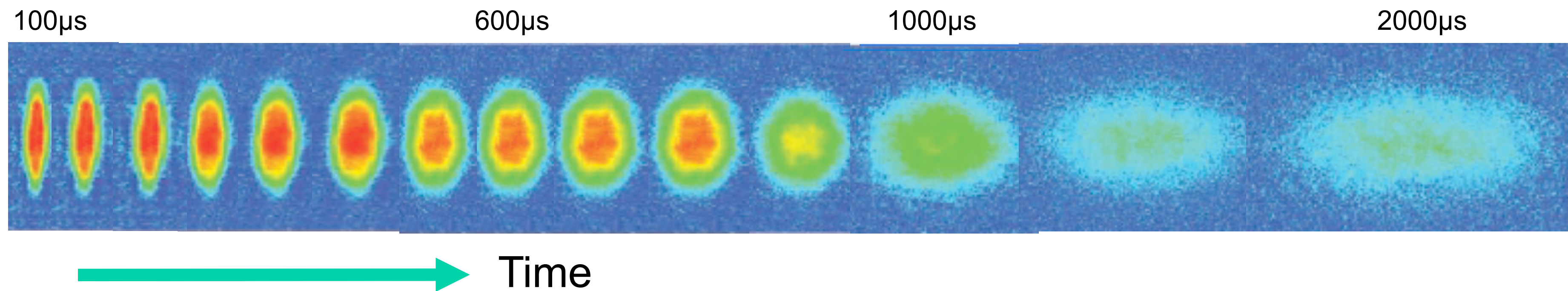


Elliptic flow observable sensitive to early evolution of system

Mechanism is self-quenching

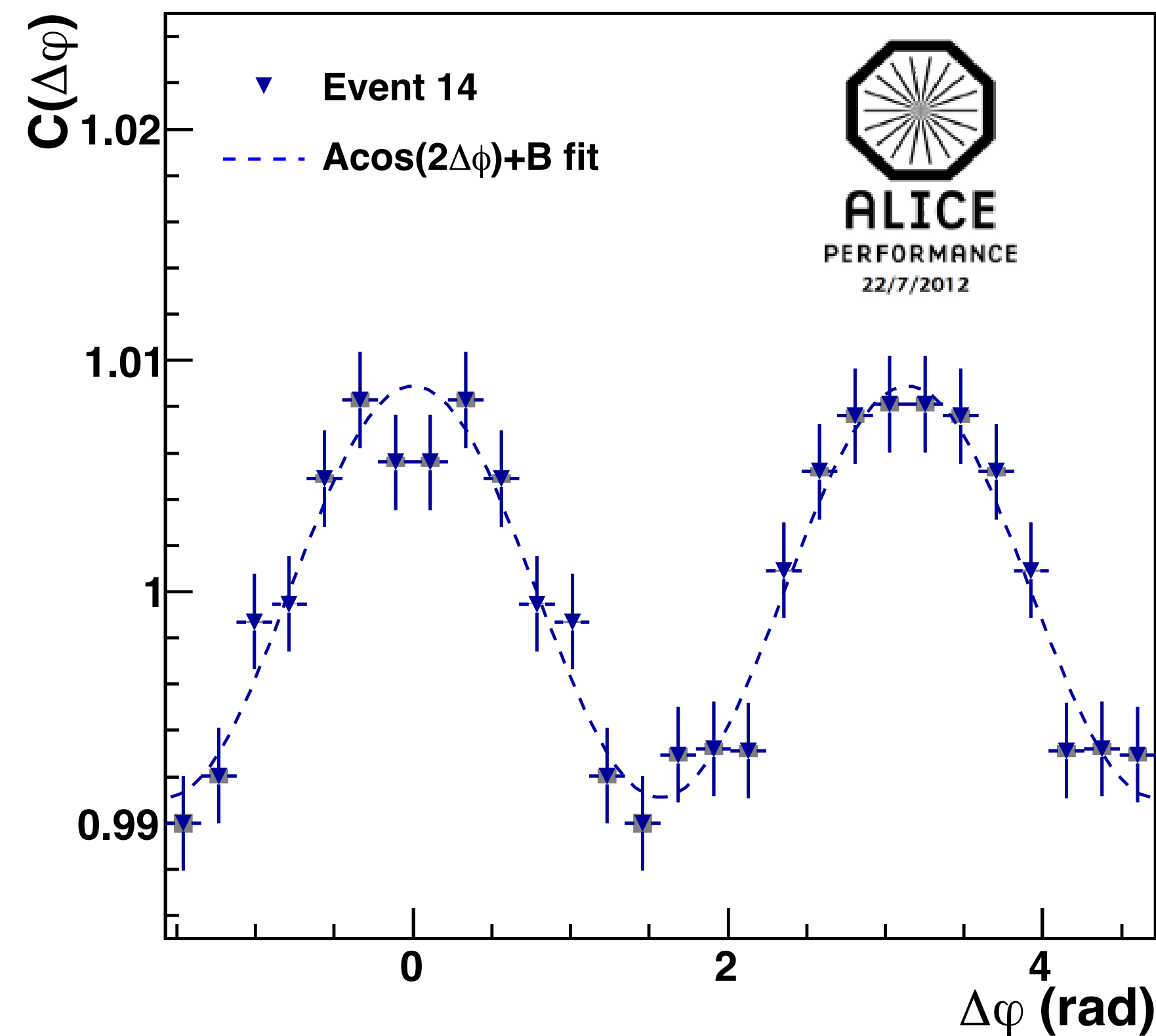
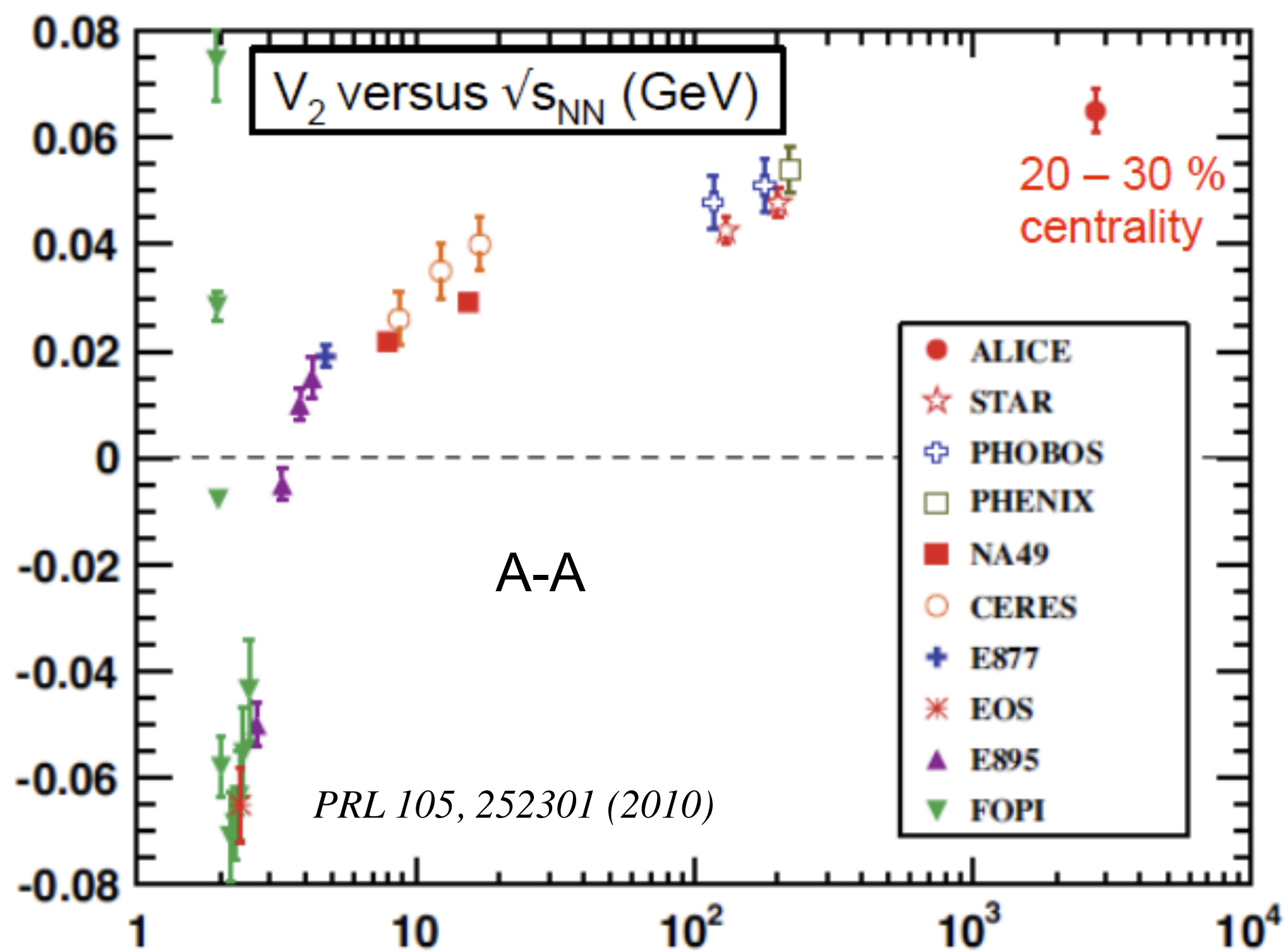
Large v_2 is an indication of *early* thermalization

Entropy in momentum space



Time

Early thermalization - elliptic flow



v_2 (p_T int.) LHC $\sim 1.3x$ (p_T int.) RHIC

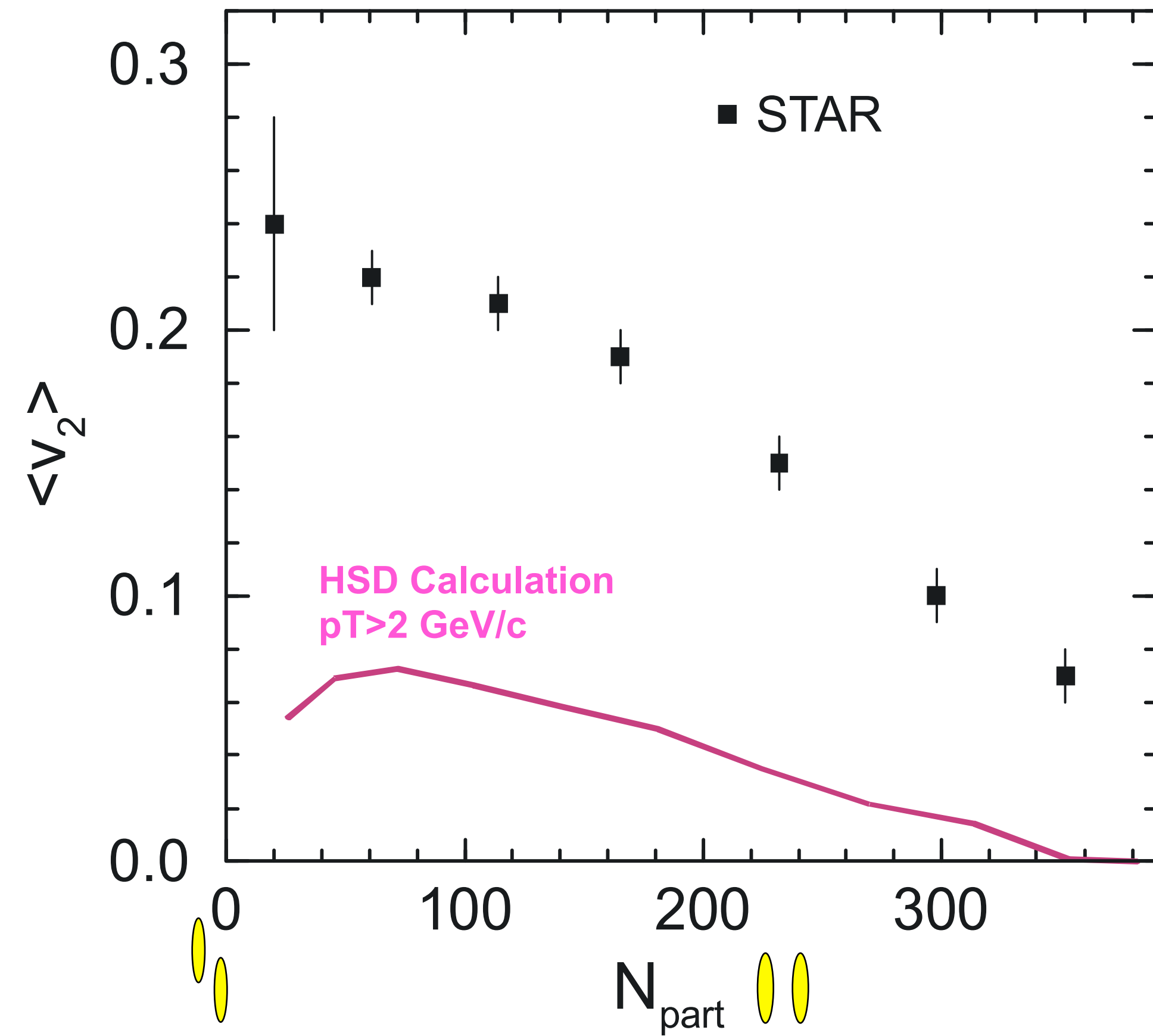
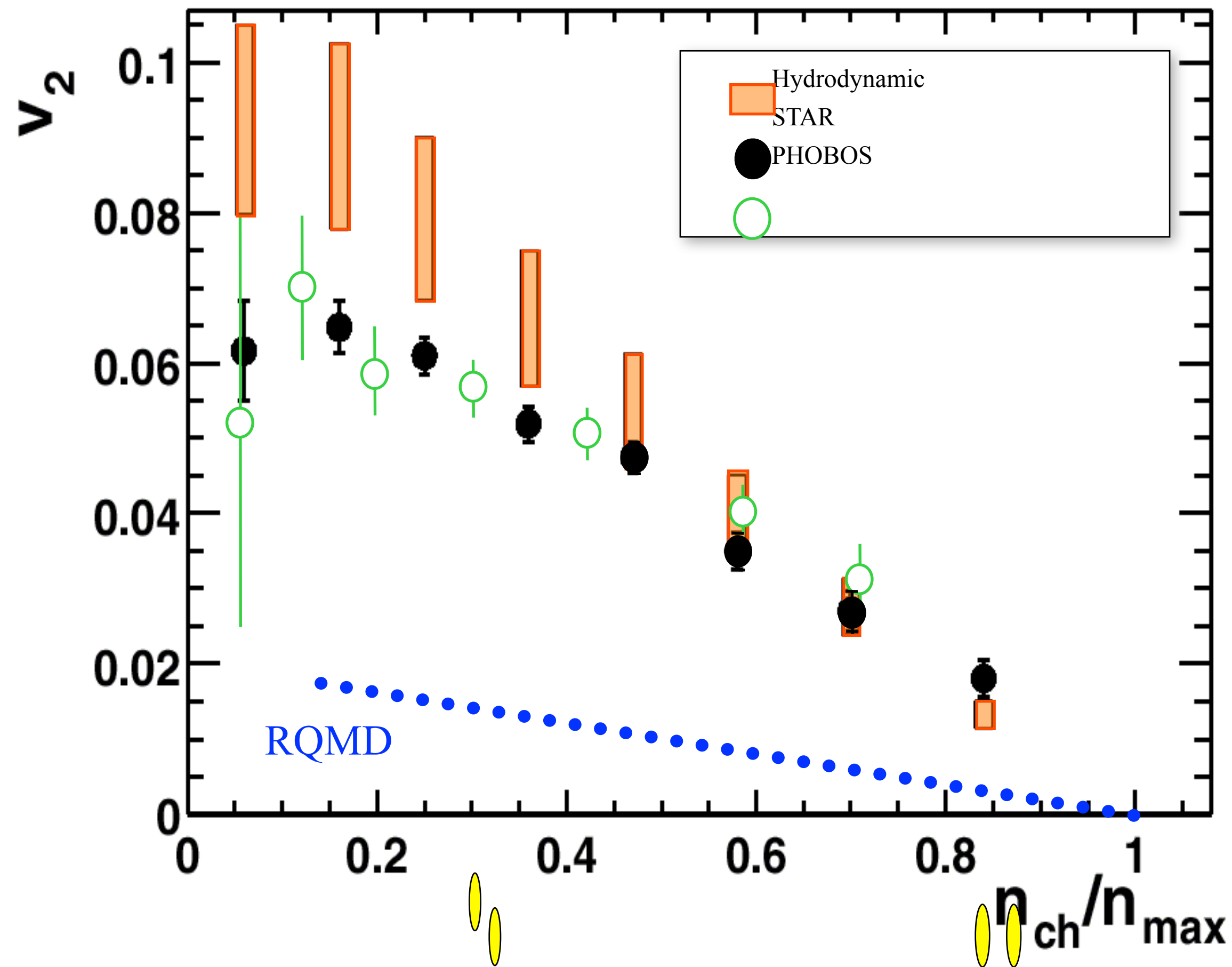
Overall increase is consistent with increased radial expansion leading to a higher mean p_T

Such high event multiplicity flow measured event-by-event

Strong evidence for thermalization

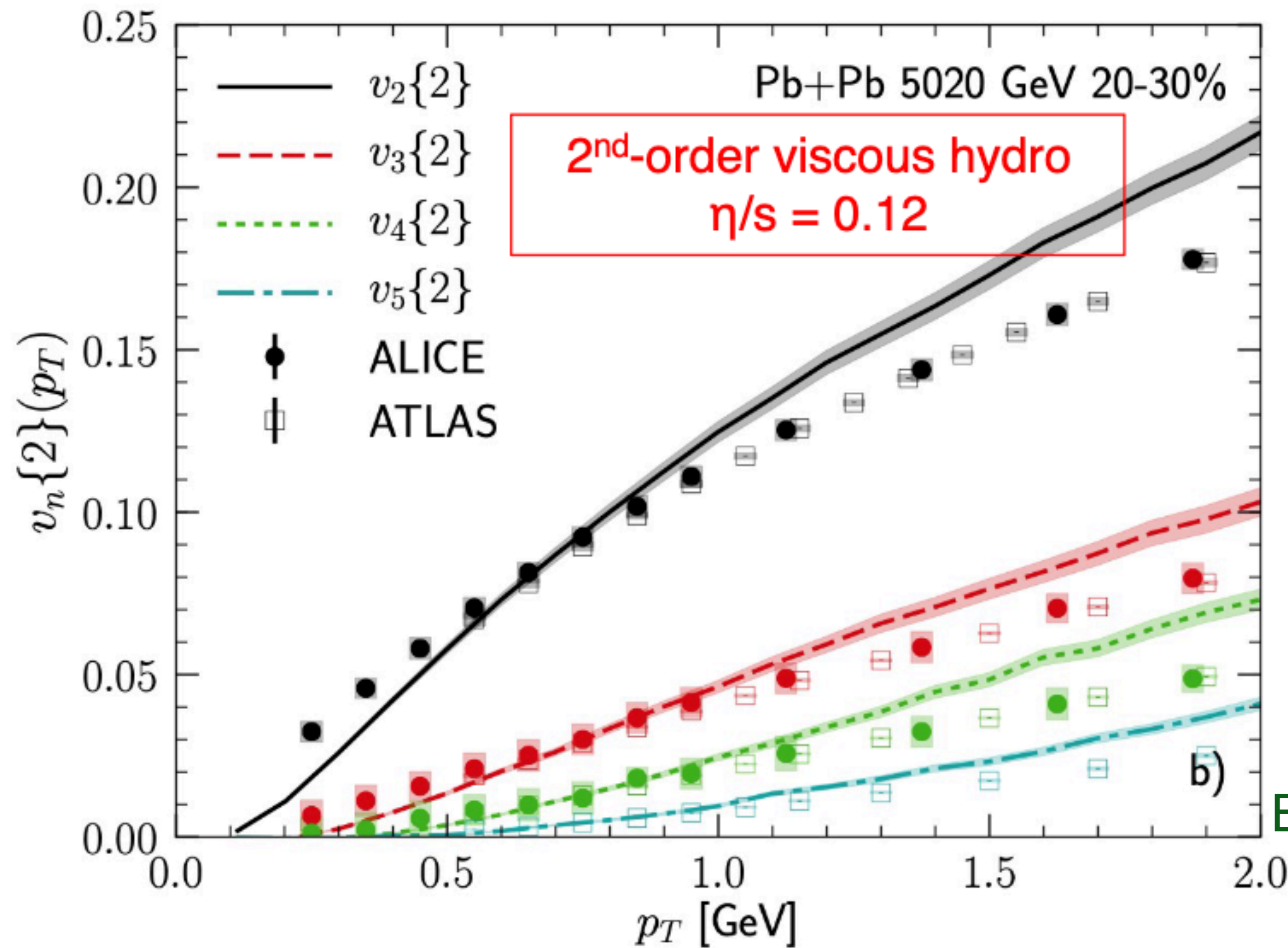
Just a gas of hadrons?

Hadronic transport models (e.g. RQMD, HSD, ...) with hadron formation times ~ 1 fm/c, fail to describe



Not a gas of weakly interacting hadrons

Its a fluid



Data well described by hydrodynamical models with very low viscosity to entropy ratio

A near-perfect fluid!

BNL Press release in 2005
CERN Press release 2010

‘confirms that the much hotter plasma produced at the LHC behaves as a very low viscosity liquid (a perfect fluid)...’

Better description with
non-zero η/s
+ realistic initial conditions
+ hadronic rescattering afterburner

Evidence for partonic degrees of freedom

Elliptic flow is additive

If partons are flowing the *complicated* observed flow pattern in $v_2(p_T)$ for hadrons

$$\frac{d^2N}{dp_T d\phi} \propto 1 + 2v_2(p_T) \cos(2\phi)$$

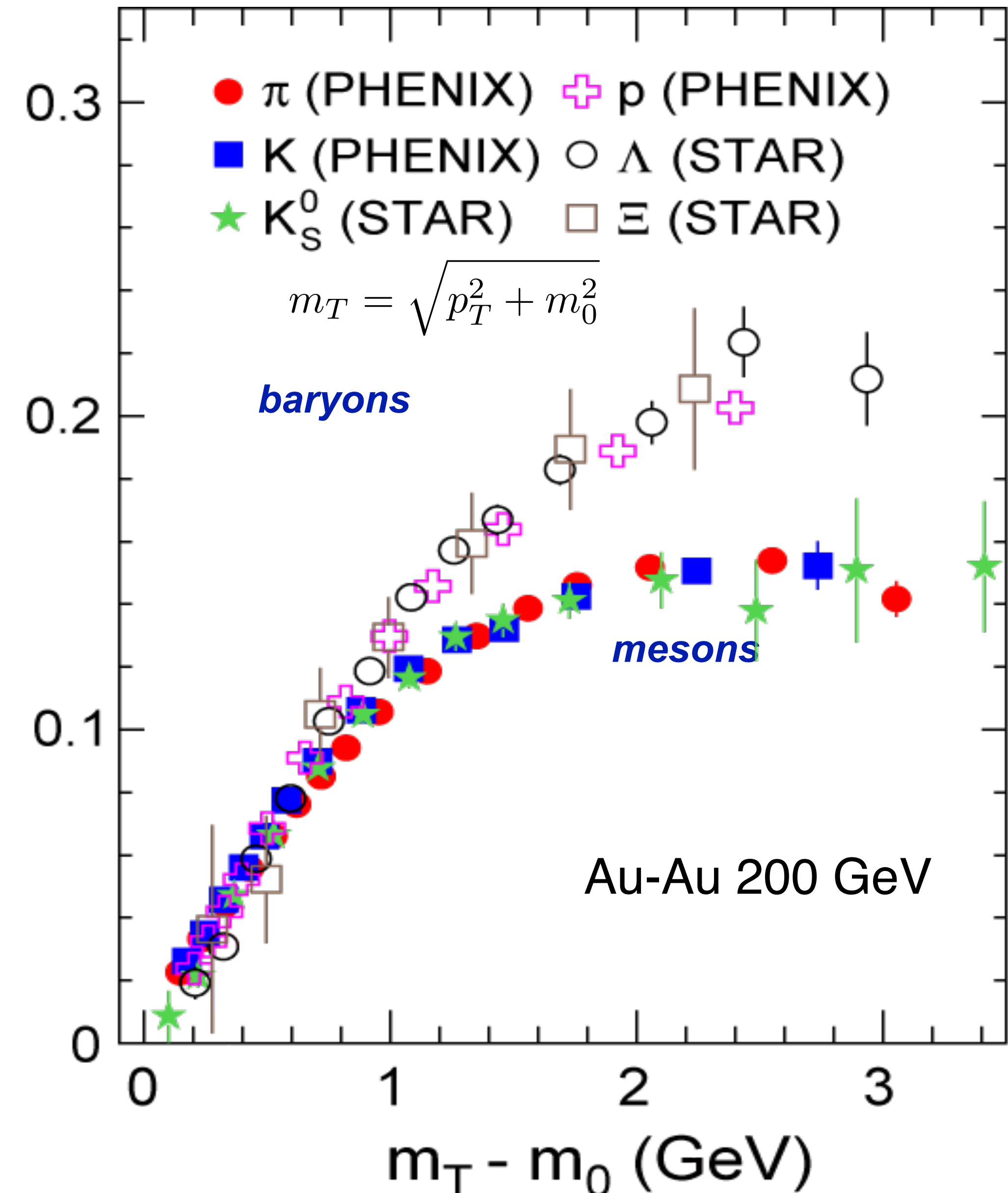
v_2

should become *simple* at the quark level

$$p_T \rightarrow p_T / n$$

$$v_2 \rightarrow v_2 / n$$

$n = (2, 3)$ for (meson, baryon)



Evidence for partonic degrees of freedom

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$$\frac{d^2N}{dp_T d\phi} \propto 1 + 2v_2(p_T) \cos(2\phi)$$

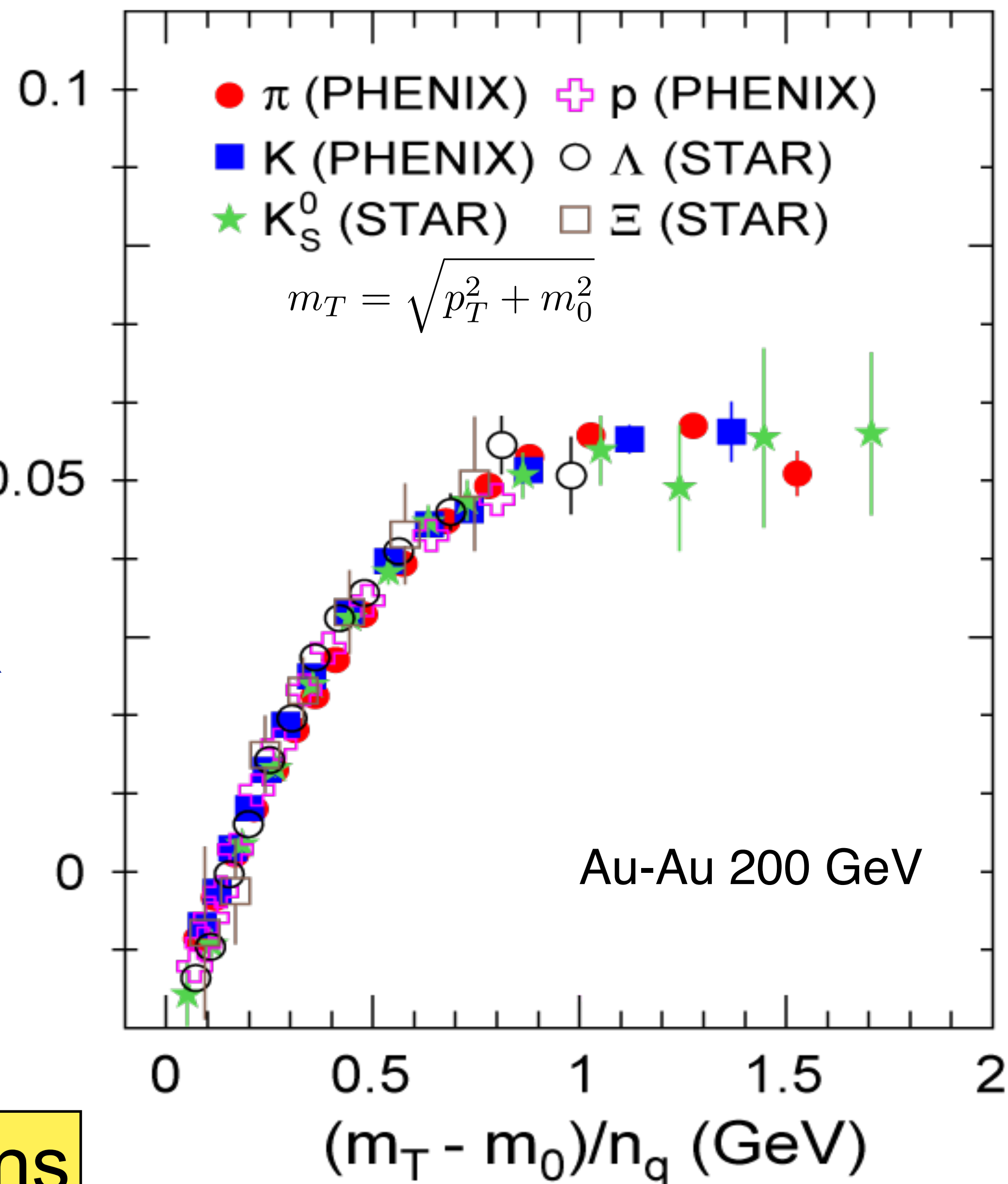
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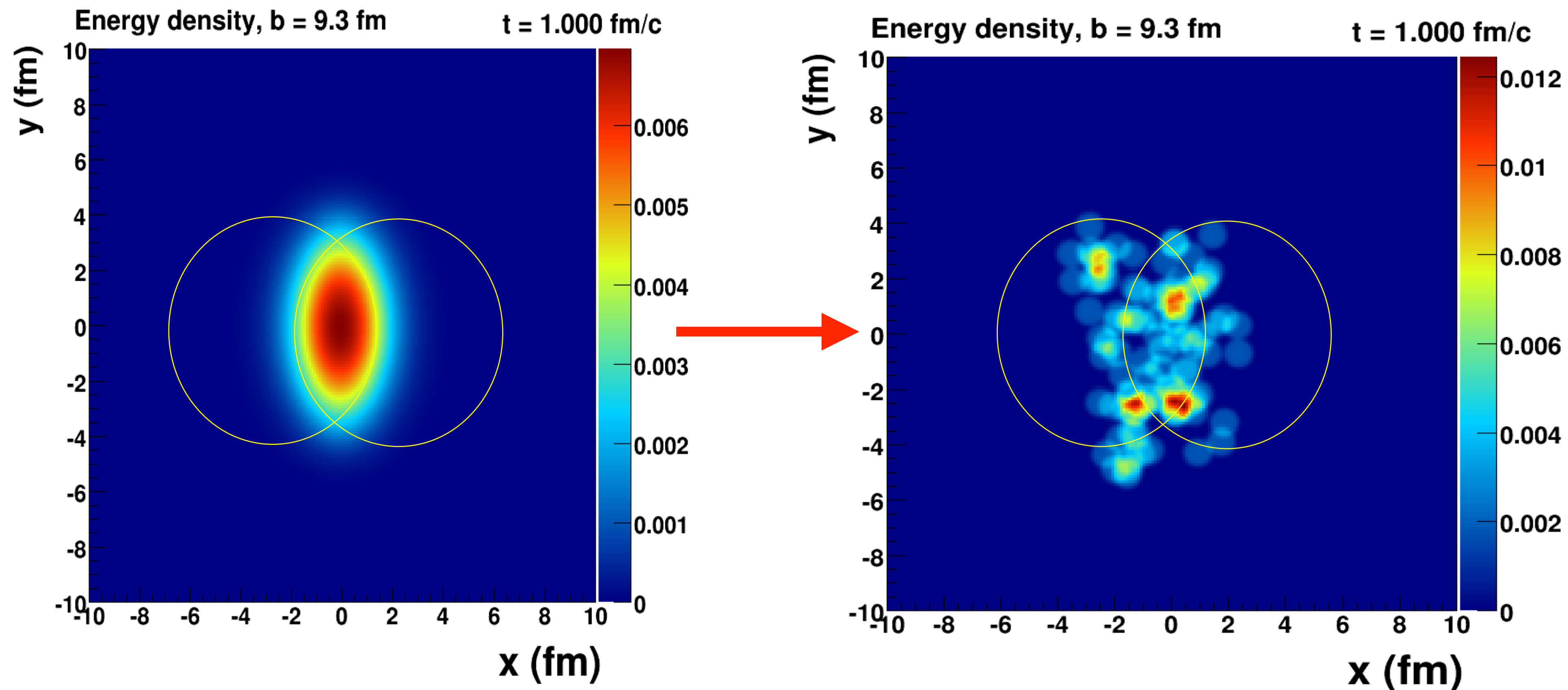
$$v_2 \rightarrow v_2 / n$$

$n = (2, 3)$ for (meson, baryon)

Constituents of QGP are partons



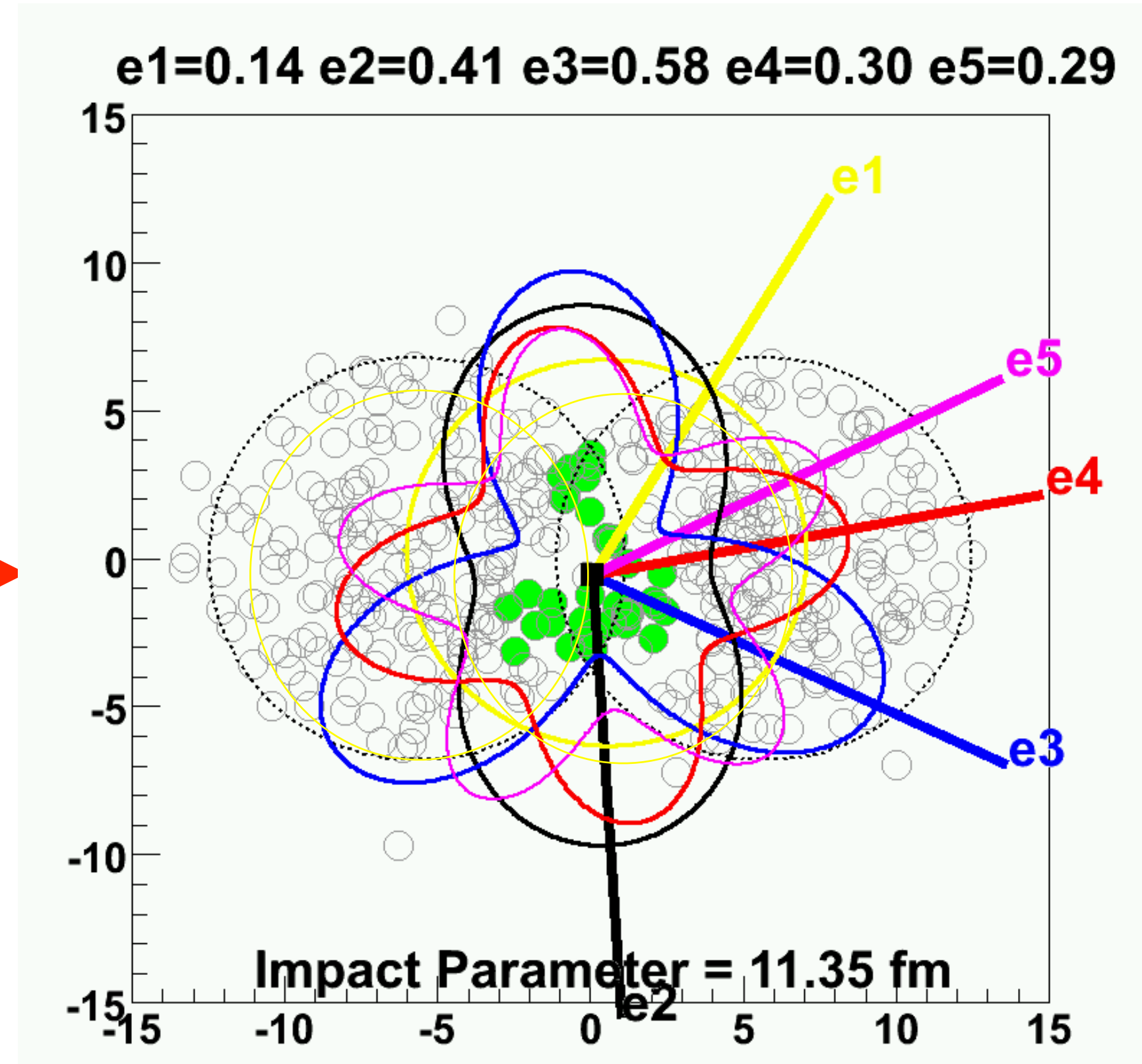
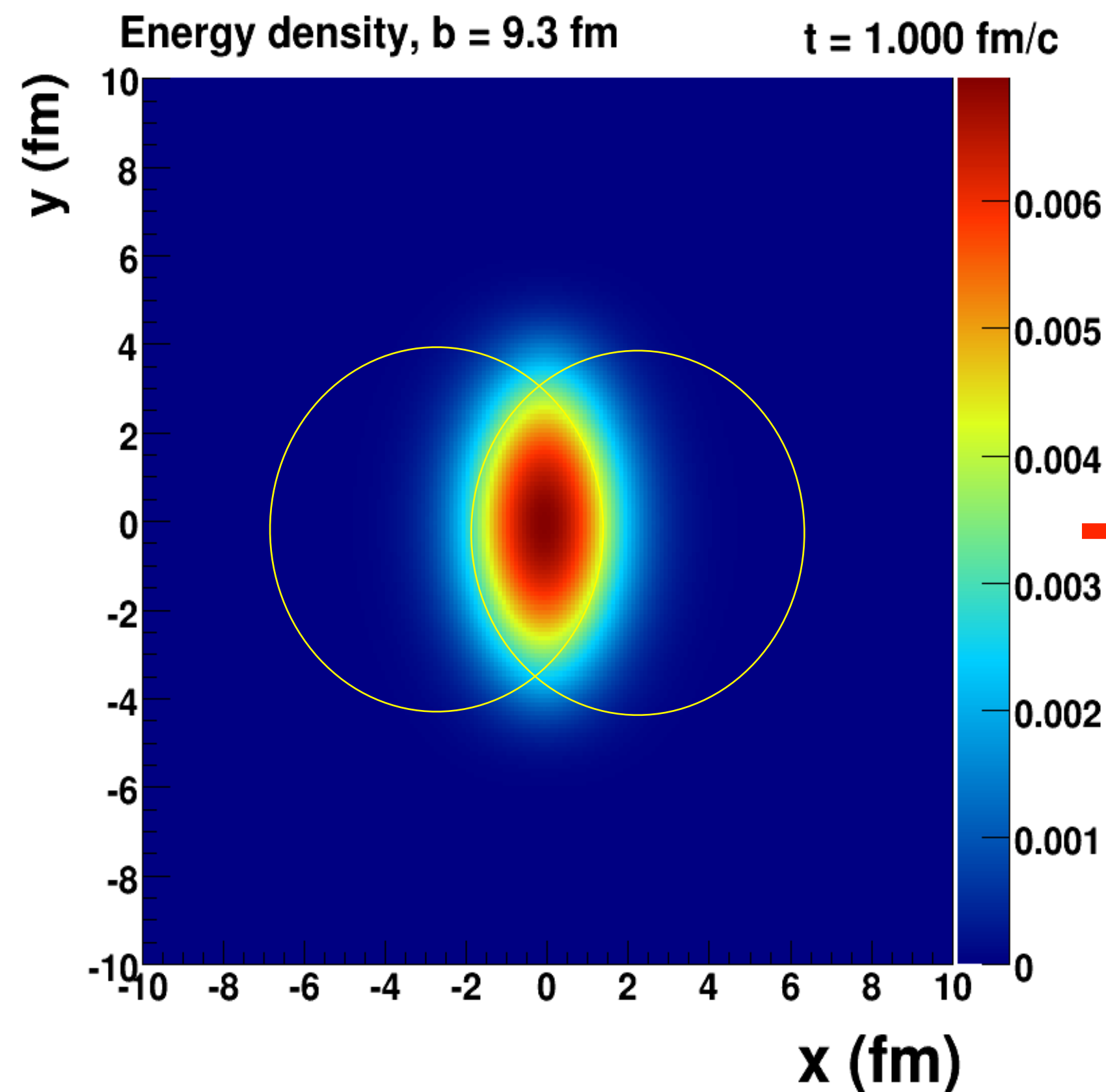
Initial conditions are complex



Event-by-event fluctuations in initial conditions are important
- induce angular correlations

Pressure gradients convert **all spatial** anisotropies into
momentum anisotropies

Initial conditions are complex



More than just elliptic flow

V_n -
magnitude of
the flow w.r.t
 n^{th} plane

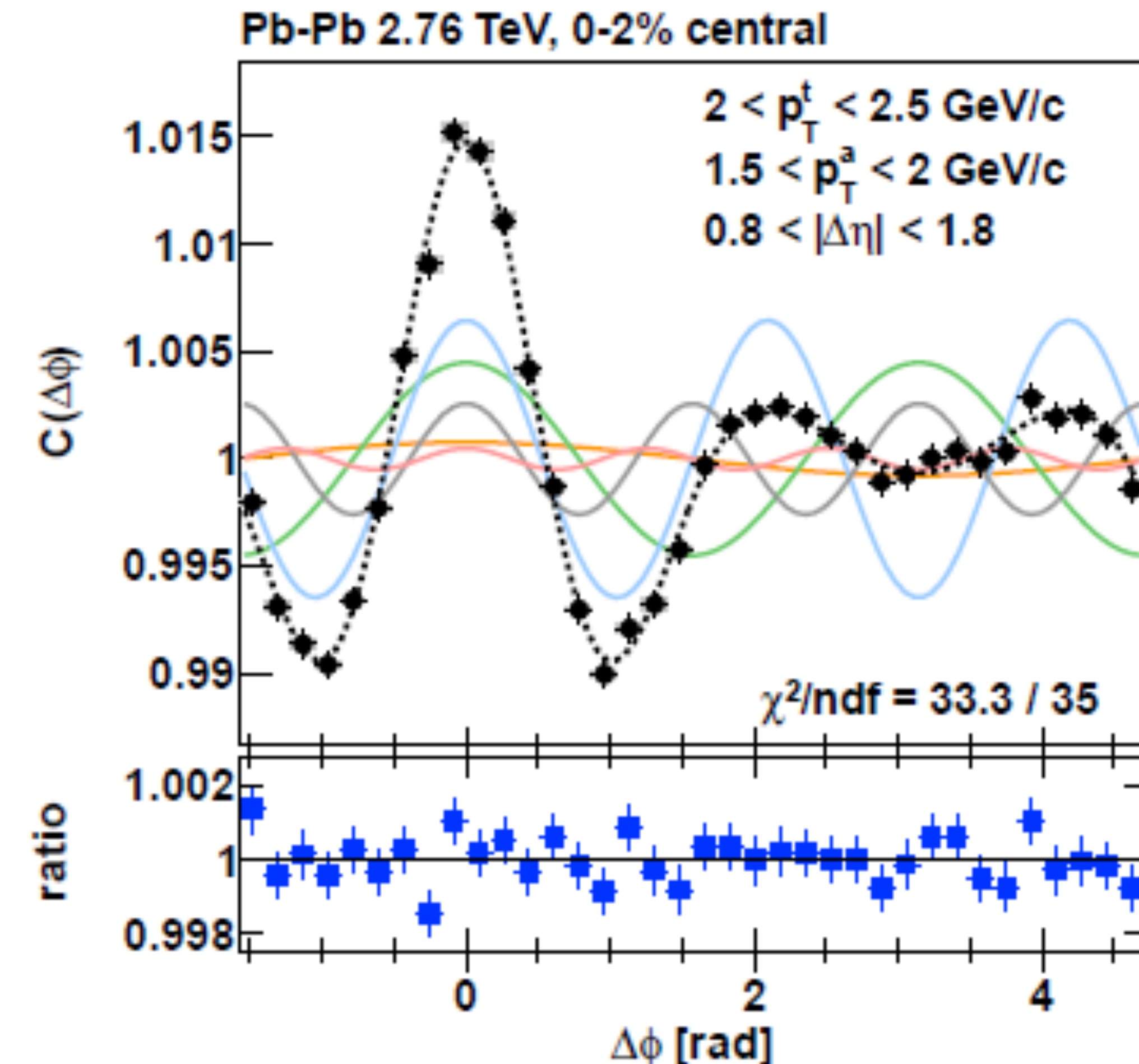
Event-by-event fluctuations in initial conditions are important
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Pressure gradients convert **all spatial** anisotropies into
momentum anisotropies

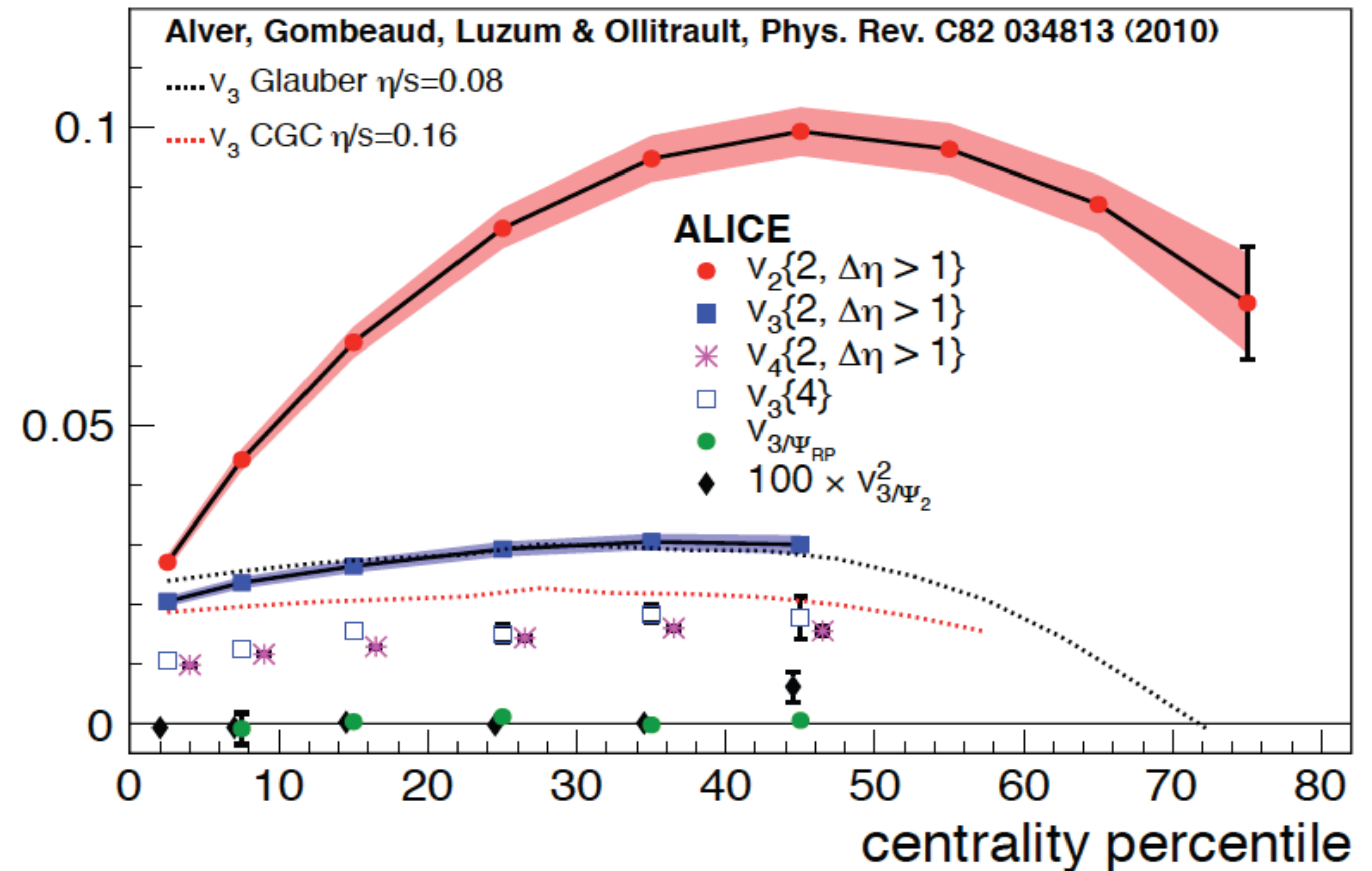
Higher harmonics

First 5 v_n components describe majority of correlations

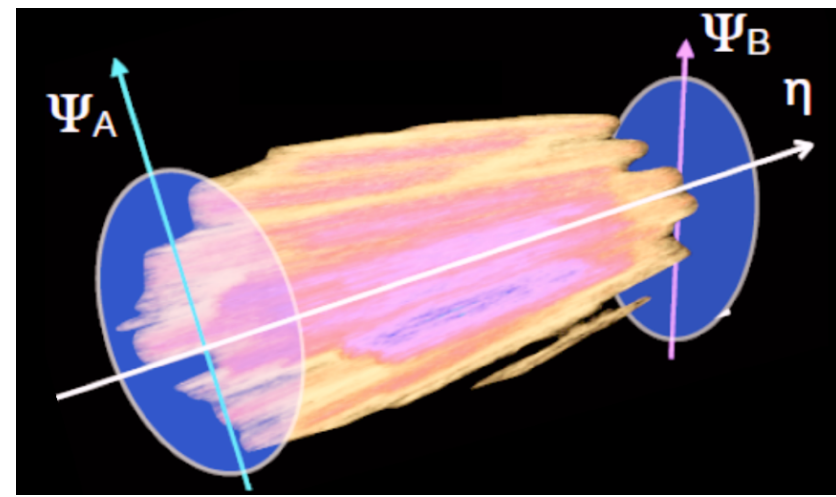
But higher orders have been extracted



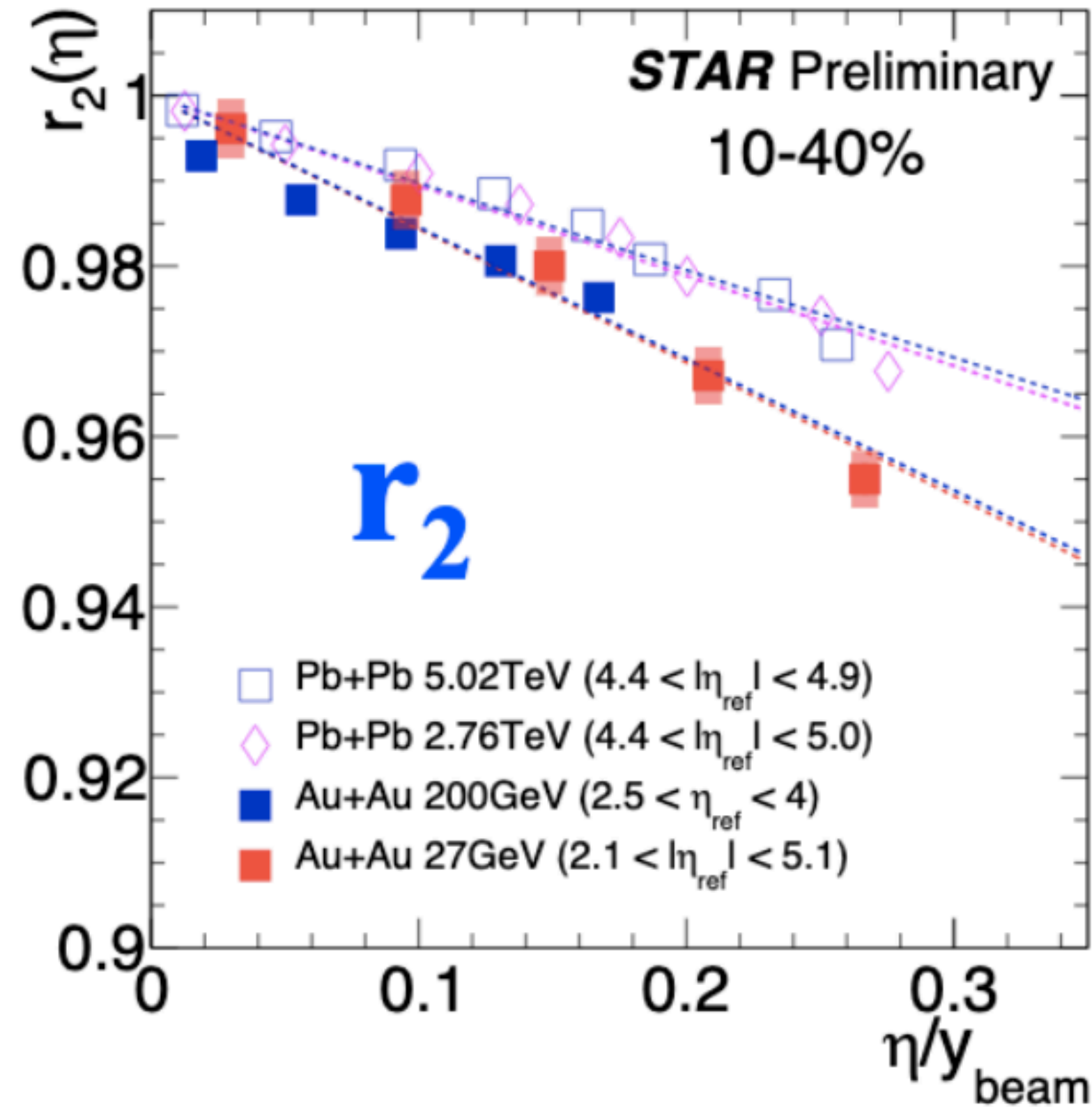
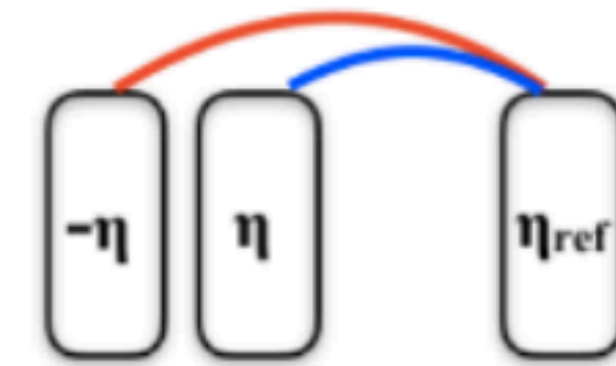
Data indicate fluctuating initial conditions



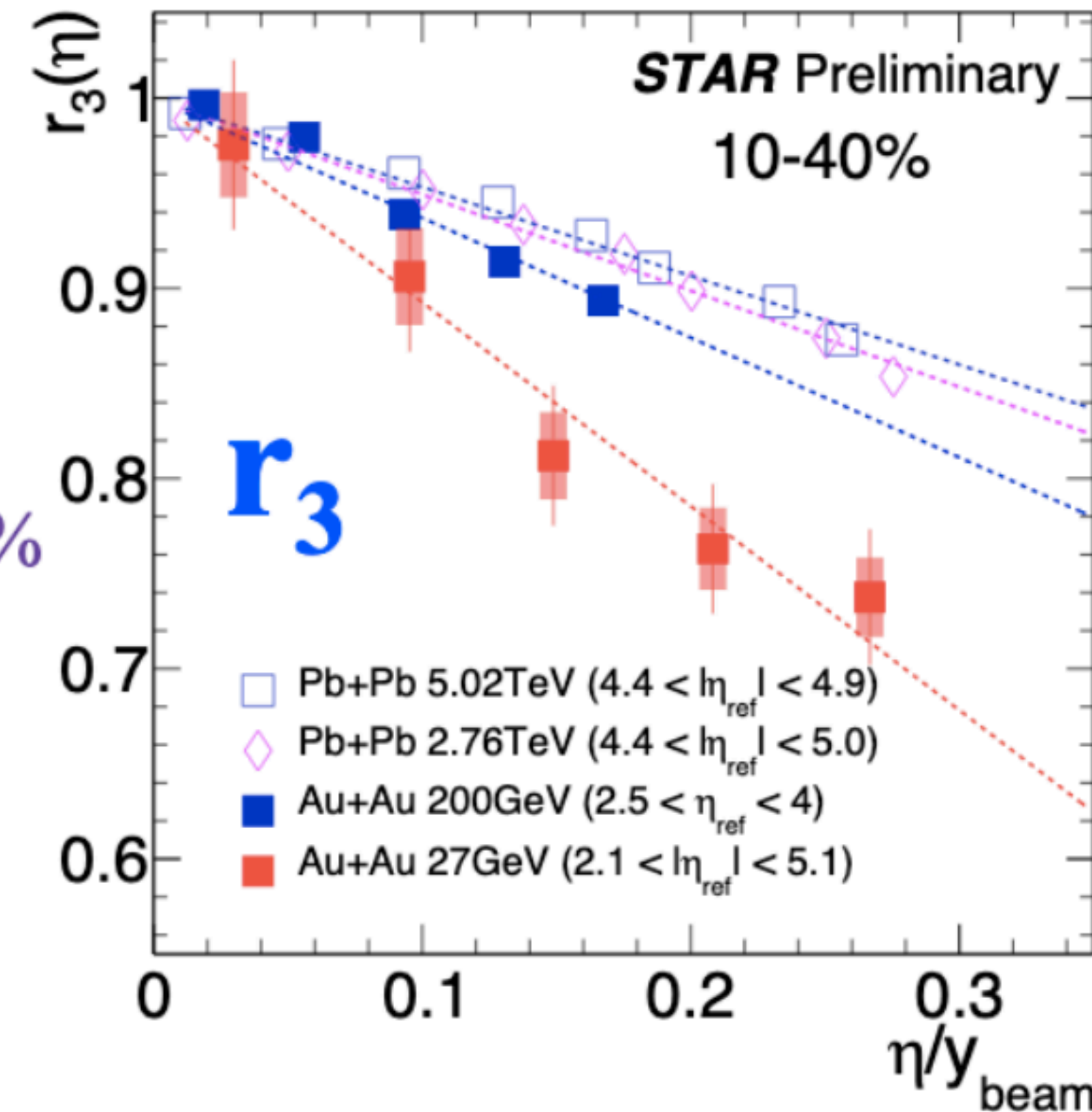
What about the longitudinal dimension?



$$r_n(\eta) = \frac{\langle V_n(-\eta)V_n^*(\eta_{\text{ref}}) \rangle}{\langle V_n(\eta)V_n^*(\eta_{\text{ref}}) \rangle}$$



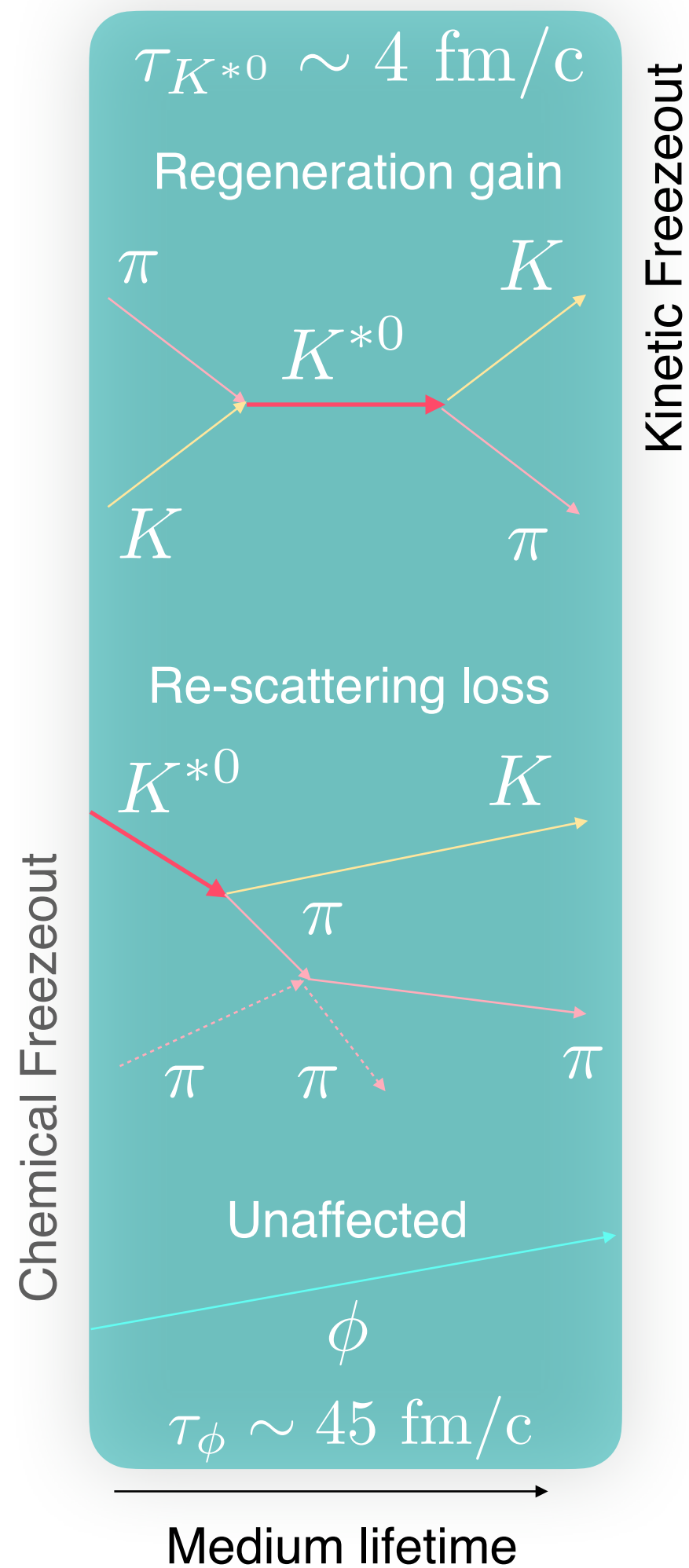
r_3 shows up to 30% decorrelation



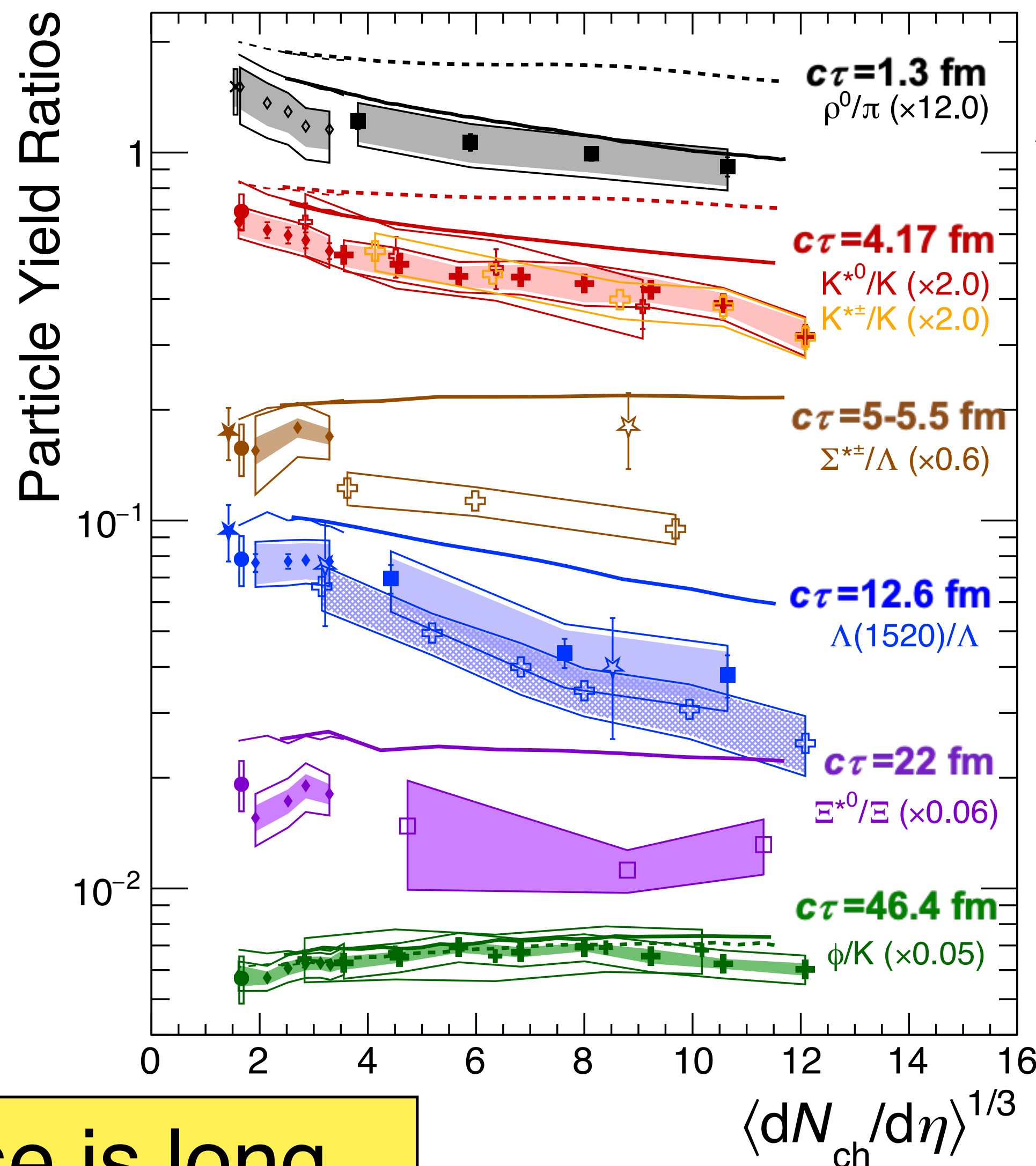
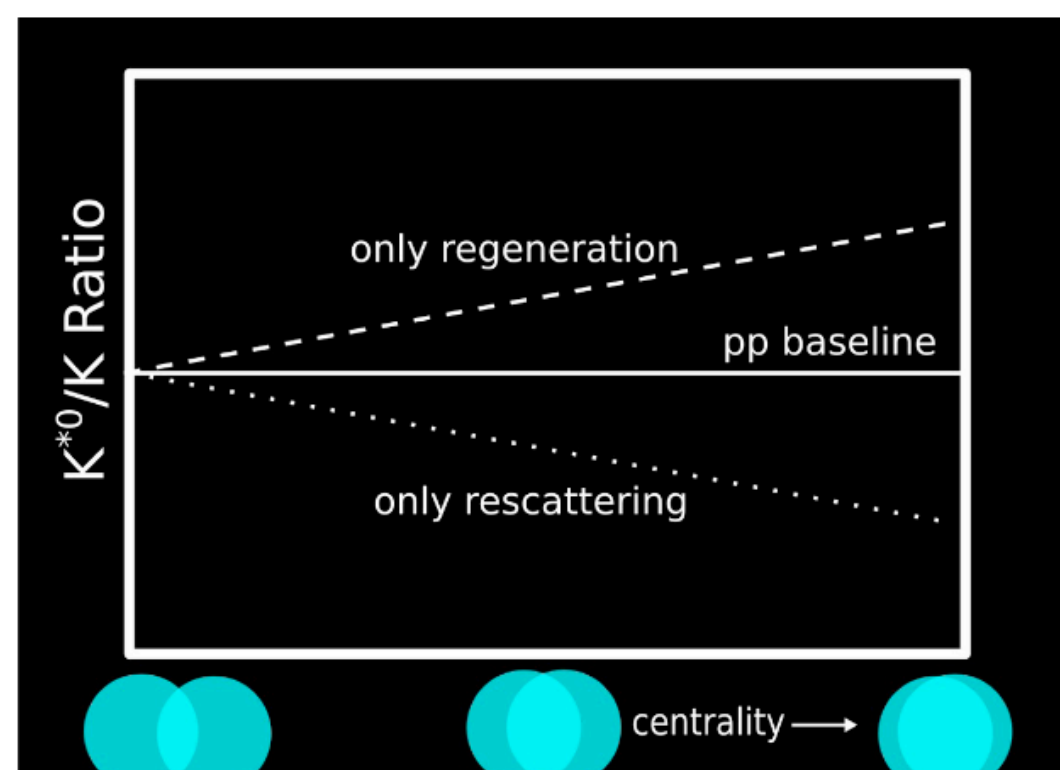
Lower energies stronger flow de-correlation
- less boost invariant

QGP medium has a twist

What about the hadronic phase?



Resonance/non-resonance probes hadronic phase between chemical and kinetic freeze-out



ALICE Preliminary

- \diamond p-Pb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$
- \square Pb-Pb $\sqrt{s_{NN}} = 2.76 \text{ TeV}$
- \oplus Pb-Pb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$
- \boxplus Xe-Xe $\sqrt{s_{NN}} = 5.44 \text{ TeV}$

ALICE

- \times pp $\sqrt{s} = 2.76 \text{ TeV}$
- \bullet pp $\sqrt{s} = 7 \text{ TeV}$
- \diamond p-Pb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$
- \blacksquare Pb-Pb $\sqrt{s_{NN}} = 2.76 \text{ TeV}$
- \oplus Pb-Pb $\sqrt{s_{NN}} = 5.02 \text{ TeV}$
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STAR

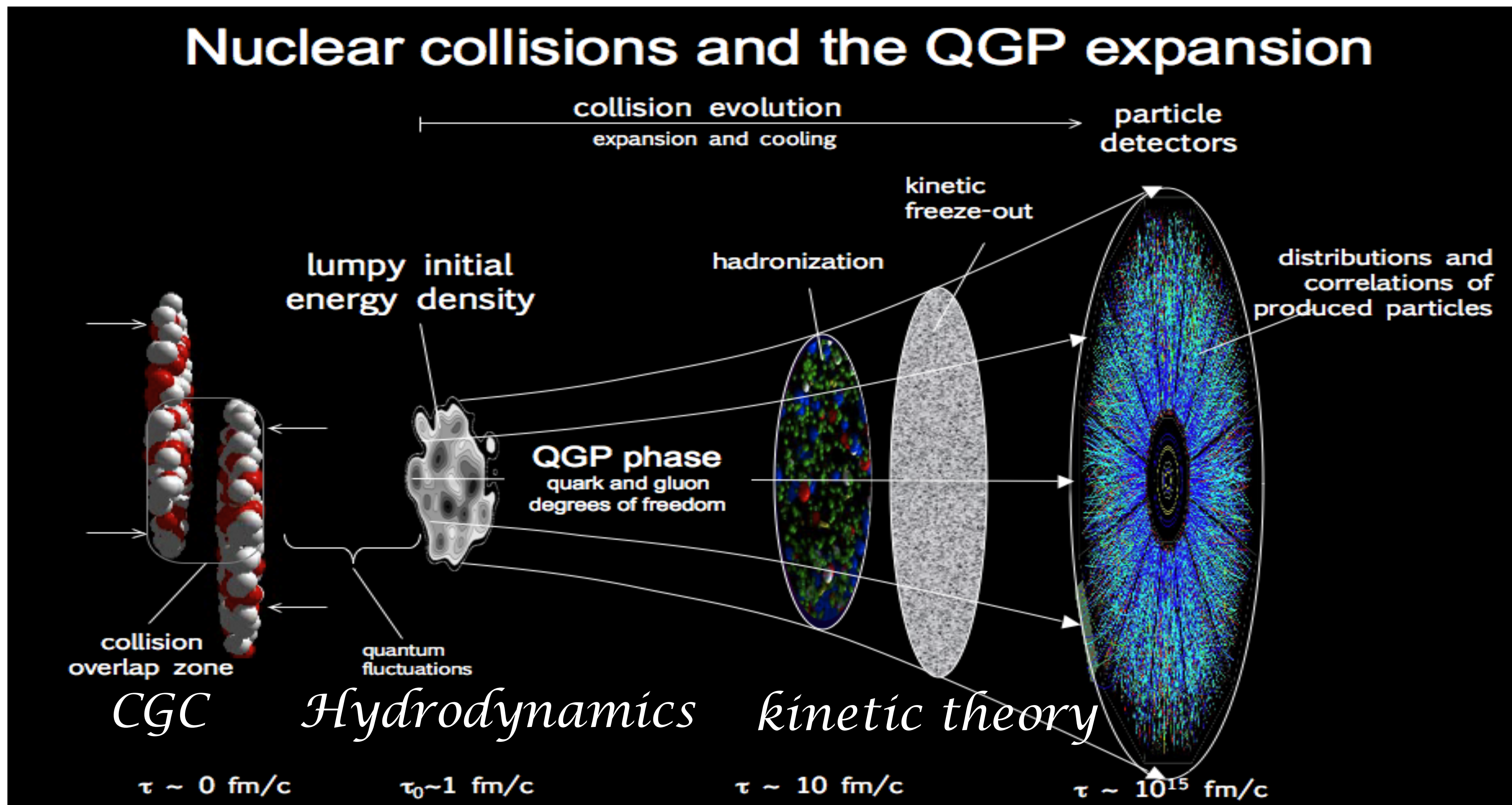
- \star pp $\sqrt{s} = 200 \text{ GeV}$
- \star Au-Au $\sqrt{s_{NN}} = 200 \text{ GeV}$

EPOS3

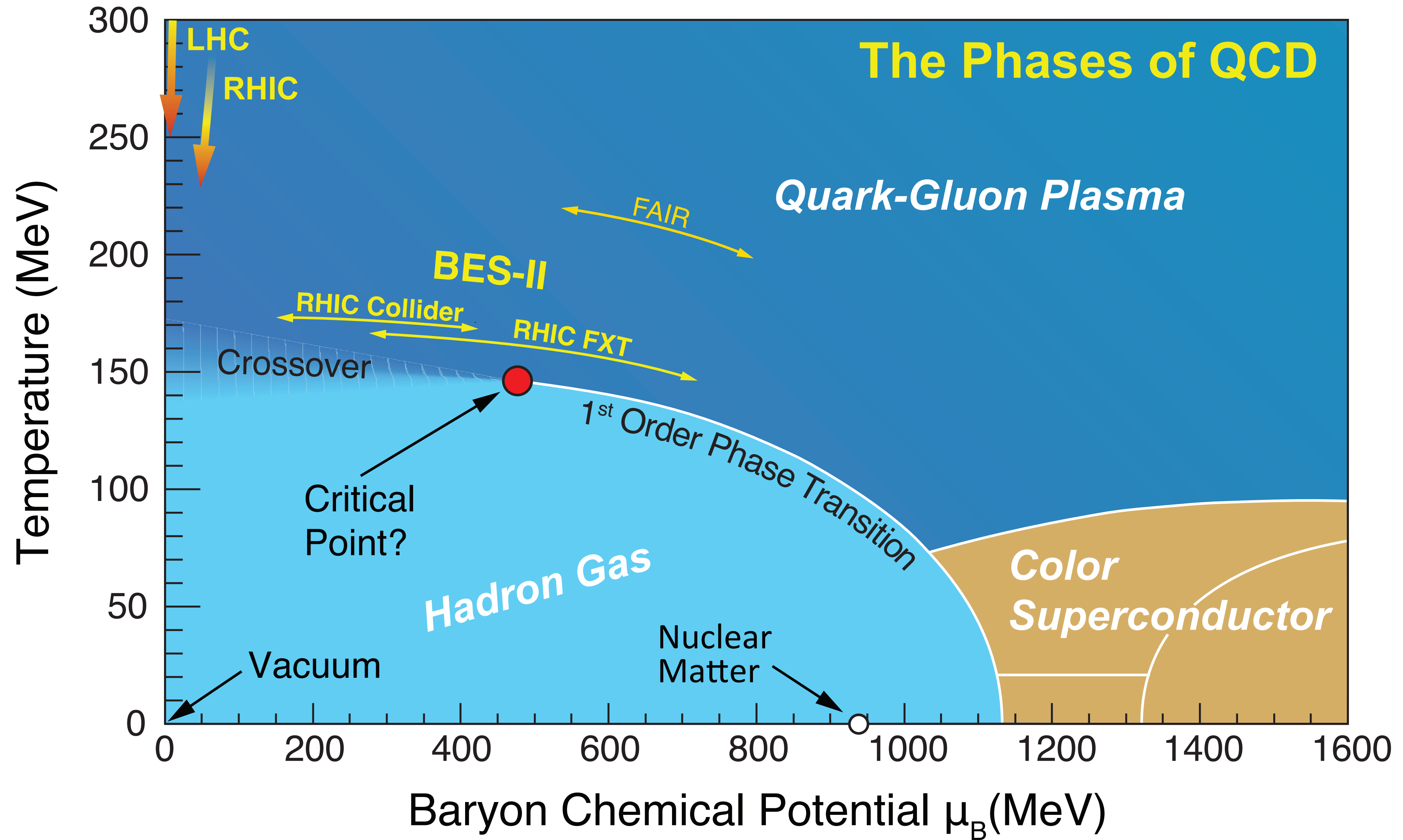
- p-Pb Pb-Pb
- UrQMD ON
- UrQMD OFF

Ratios suggest hadronic phase is long, rescattering cross-section also important

More detailed summary of the collision's evolution



Back to the phase diagram

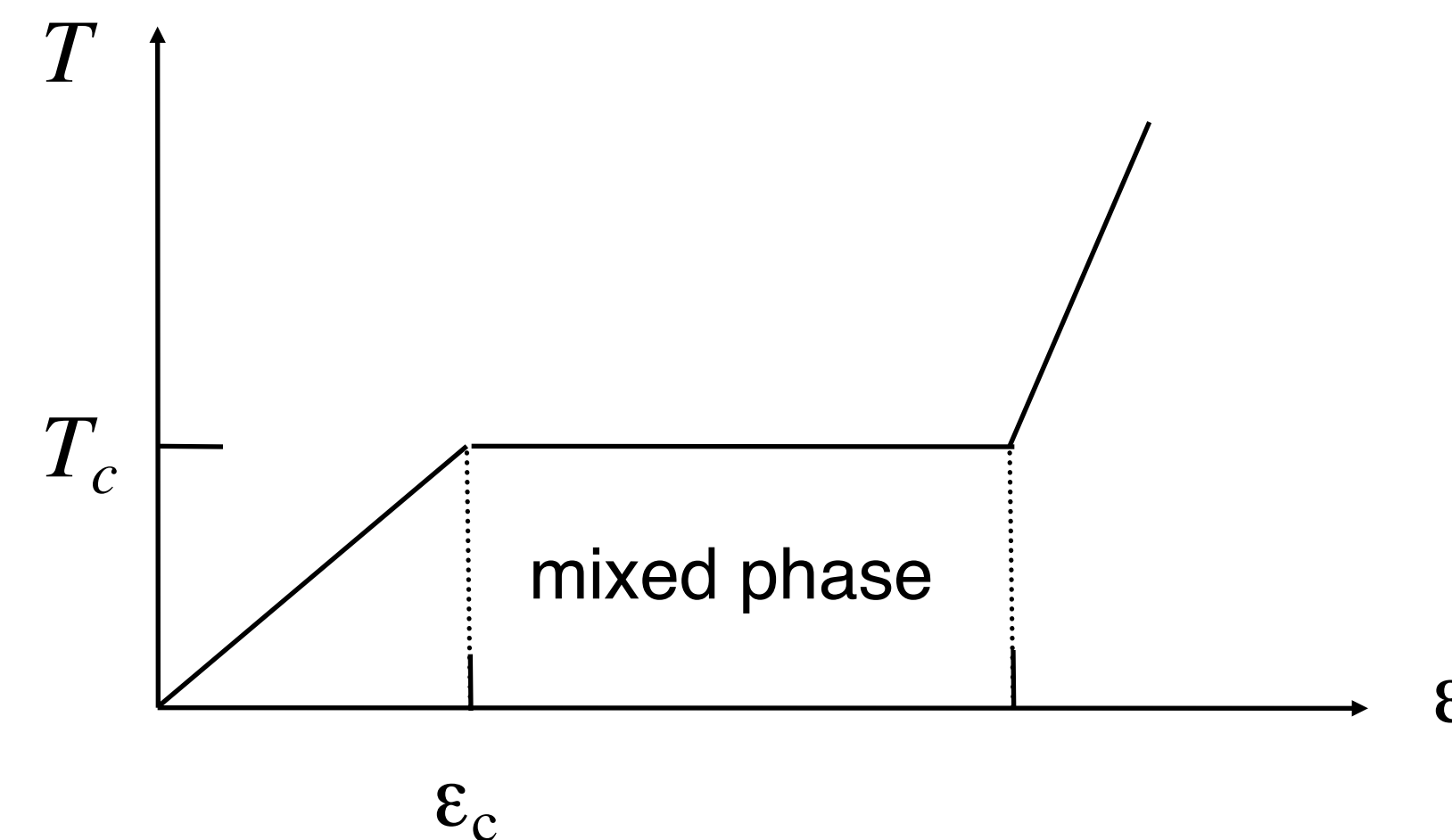
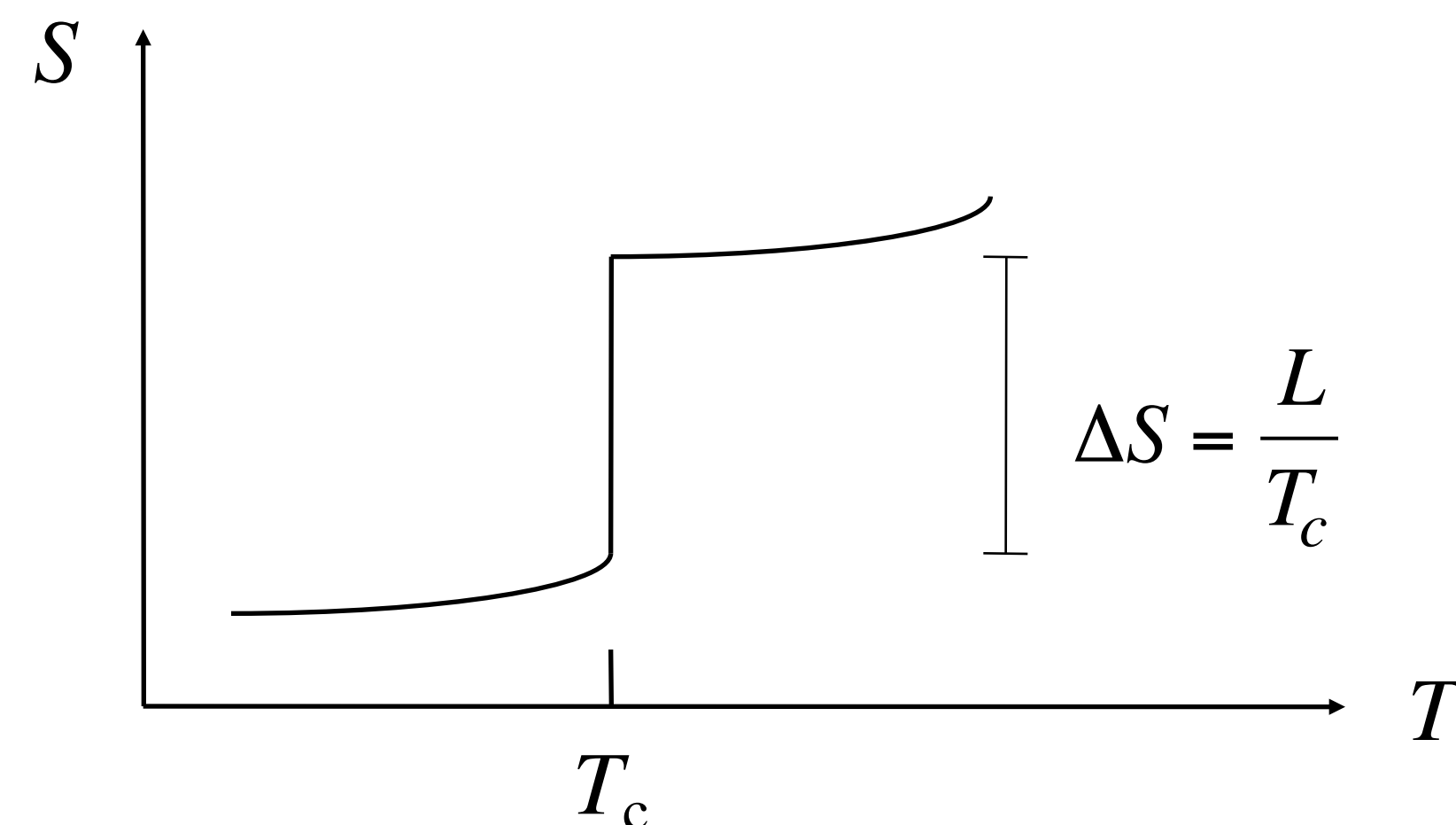


Thermodynamics - phase transitions

Phase transition or a crossover?

Signs of a phase transition:

1st order: **discontinuous in entropy** at T_c → Latent heat, a mixed phase



Higher order: **discontinuous in higher derivatives of $\delta^n S / \delta T^n$** → no mixed phase - system passed smoothly and uniformly into new state (ferromagnet)

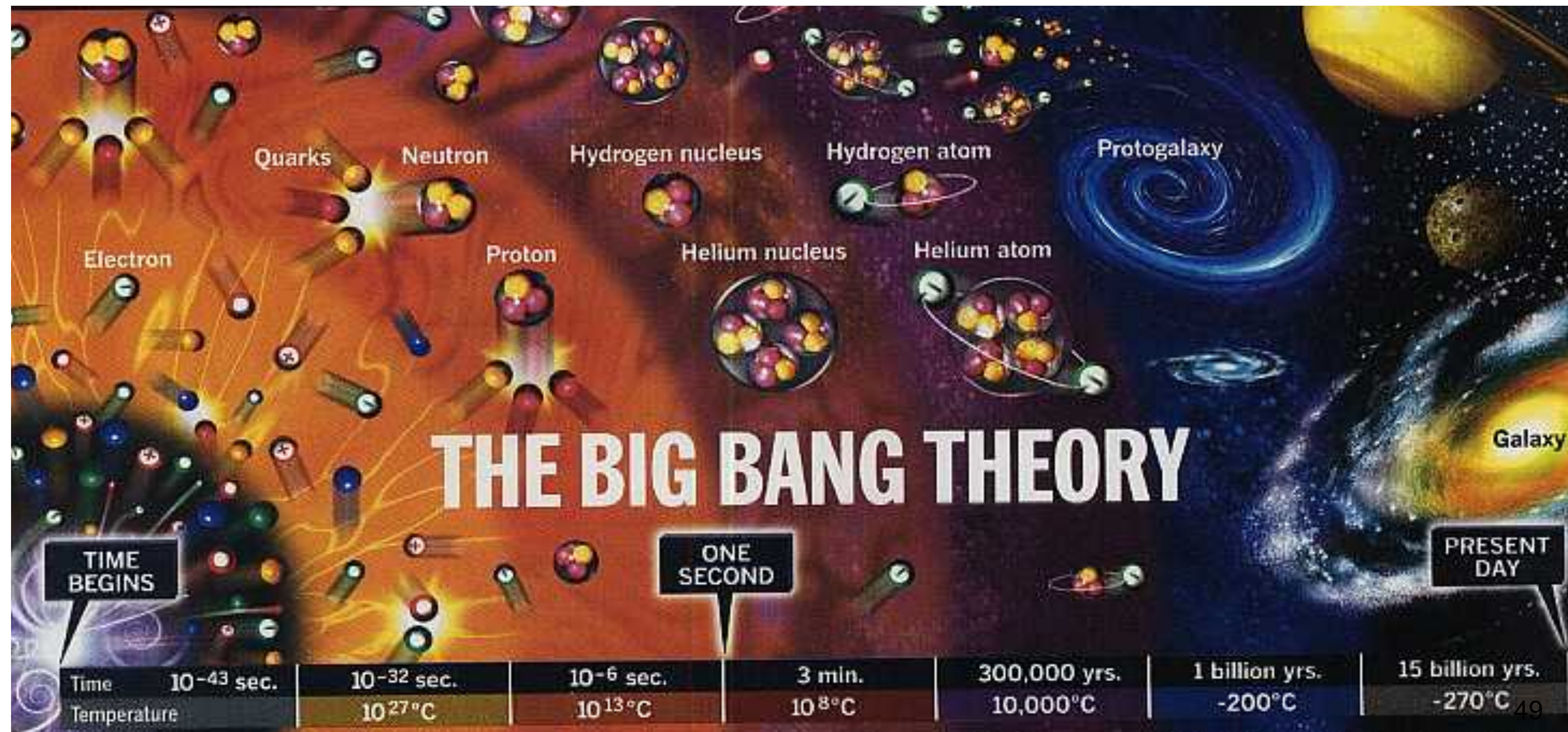
Temperature ⇔ transverse momentum

Energy density ⇔ transverse energy

Entropy ⇔ multiplicity

The order of the phase transition

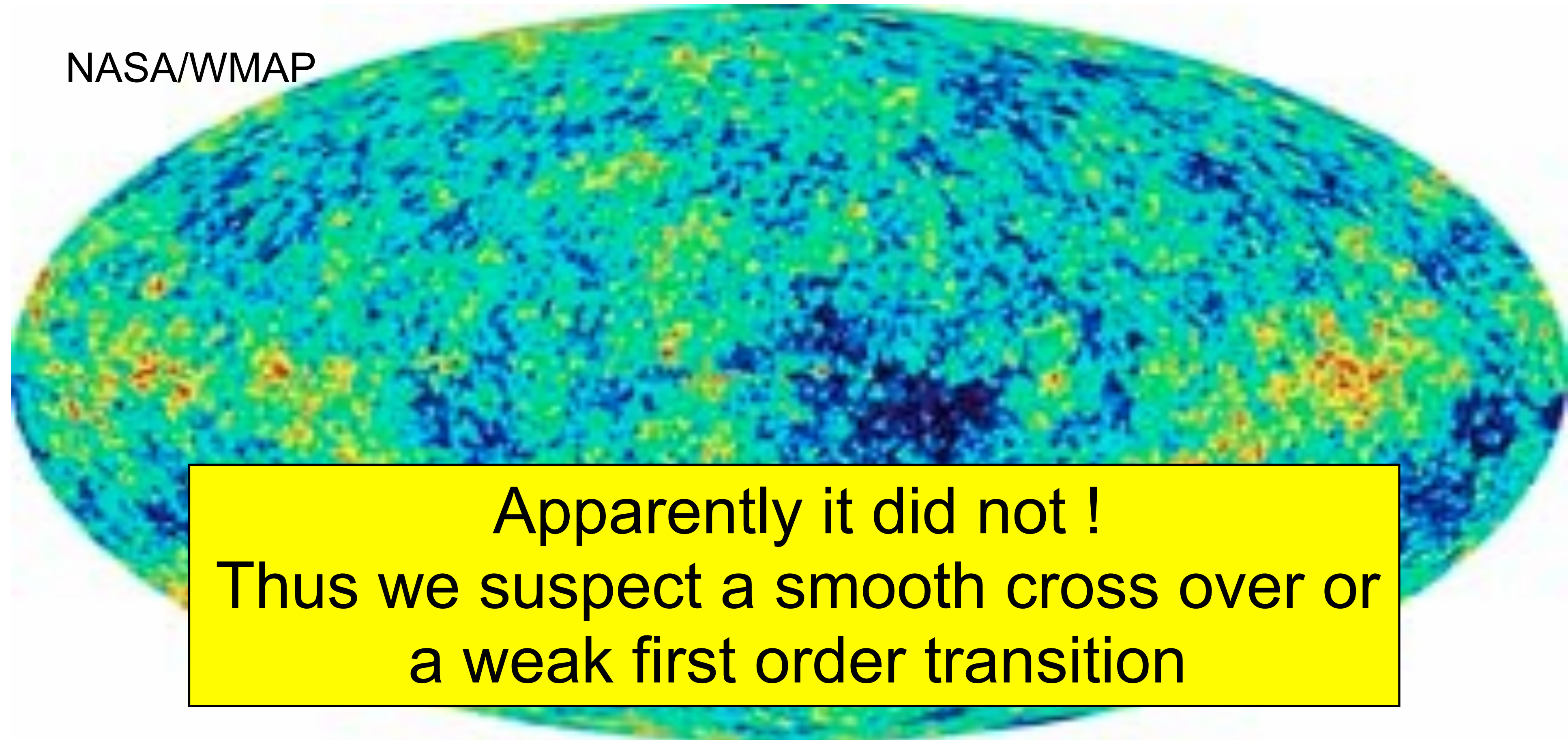
“A **first-order QCD phase transition** that occurred in the early universe would lead to a **surprisingly rich cosmological scenario.**” Ed Witten, Phys. Rev. D (1984)



The order of the phase transition

“A **first-order QCD phase transition** that occurred in the early universe would lead to a **surprisingly rich cosmological scenario.**” Ed Witten, Phys. Rev. D (1984)

NASA/WMAP



Apparently it did not !
Thus we suspect a smooth cross over or
a weak first order transition

**Is there a Critical Point or
evidence of an ordered
transition?**

The phase diagram of QCD - theoretical input

Very hard to extrapolate off $\mu_B = 0$ axis

Cross-over at low μ_B

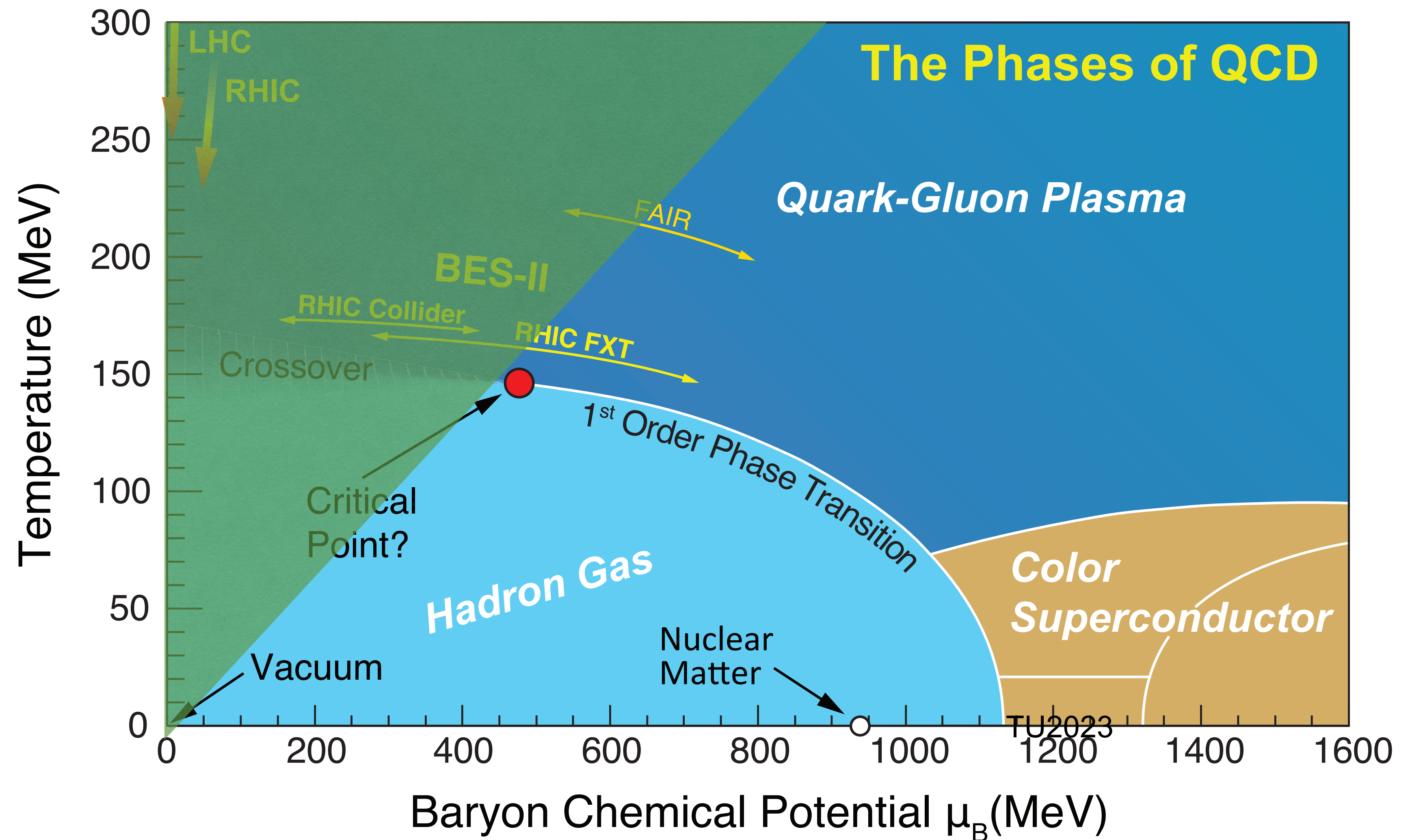
Disfavor QCD critical point at $\mu_B/T < 3$

Several calculations settling on CP at

$T \sim 90-100$ MeV
 $\mu_B \sim 500-600$ MeV

$\sqrt{s_{NN}} = 3-5$ GeV

CP might also not exist -
needs experimental answer



QCD creates a rich landscape to explore

Critical fluctuations

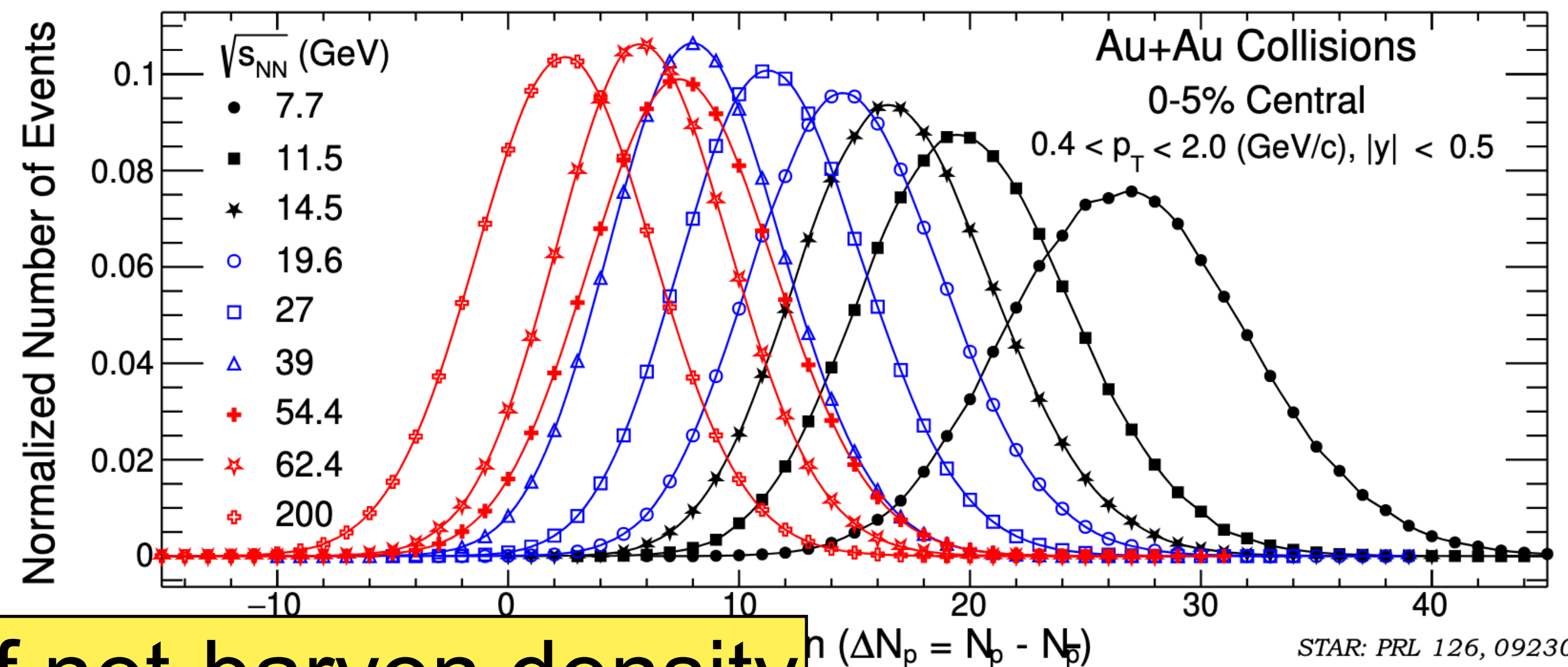
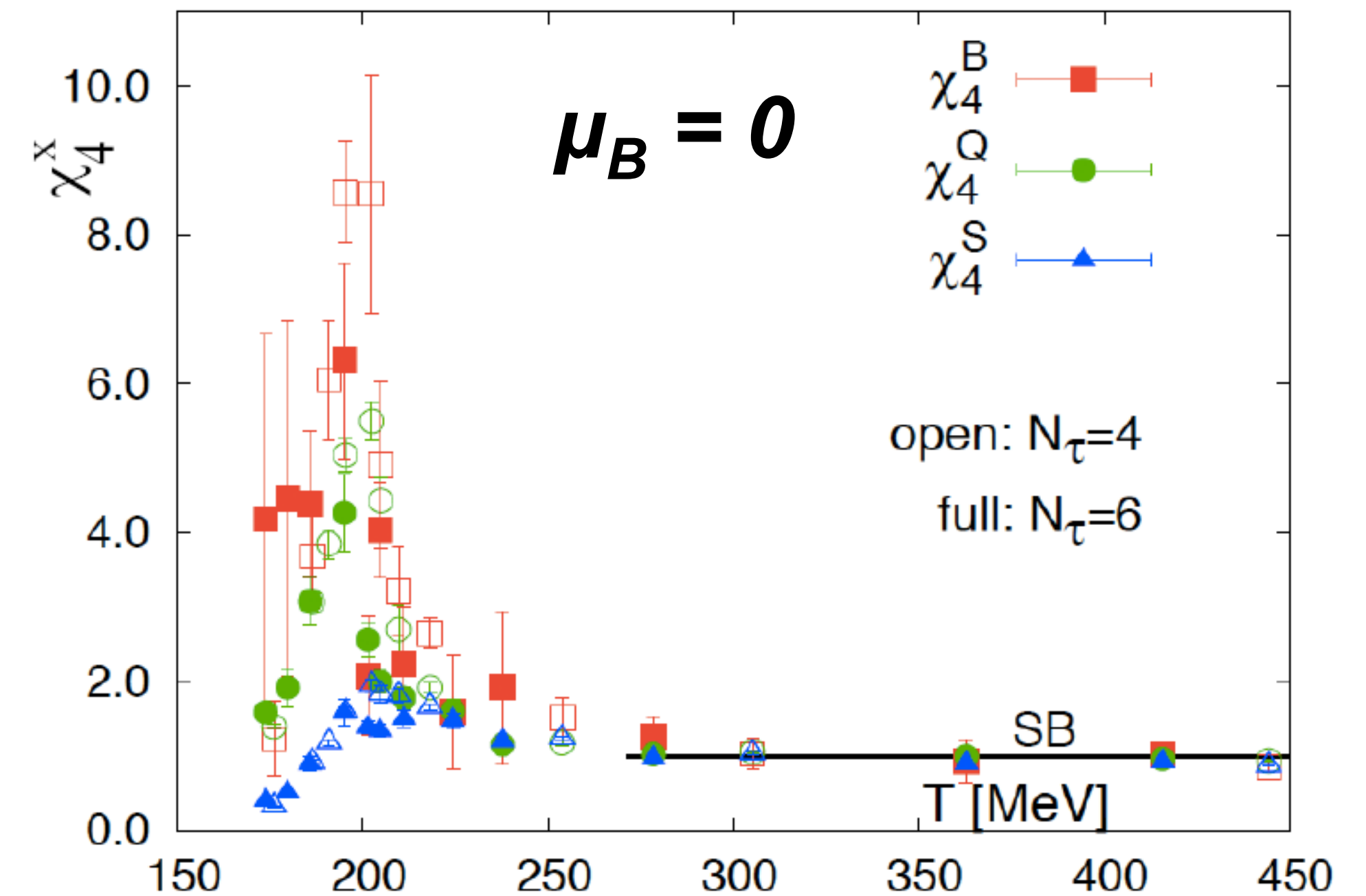
Critical Points:

- divergence of susceptibilities
e.g. magnetism transitions
- divergence of correlation lengths
e.g. critical opalescence

Lattice QCD:

Divergence of susceptibilities for conserved quantities (B,Q,S) at critical point

Divergences of conserved quantities may survive in the final state



Non-gaussian fluctuations of net-baryon density

Conserved quantities are the key

Particle number density, $N/V = n_k(T, \mu_k) = \frac{d_k}{(2\pi)^3} \int d^3\vec{p} \frac{1}{(-1)^{B_k+1} + \exp((\sqrt{\vec{p}^2 + m_k^2} - \mu_k)/T)} = (\partial p / \partial \mu_k)_T$

Theoretically susceptibilities of conserved quantities (B,Q,S) can be calculated :

$$\chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n} (p/T^4)}{\partial(\mu_B/T)^l \partial(\mu_S/T)^m \partial(\mu_Q/T)^n}.$$

Experiment measure event-by-event distribution of conserved quantities

Focus on net-proton as proxy for net-baryon

Take ratios to remove volume and T dependence

$$\delta N = N - \langle N \rangle$$

mean: $M = \langle N \rangle = VT^3 \chi_1,$

variance: $\sigma^2 = \langle (\delta N)^2 \rangle = VT^3 \chi_2,$

skewness: $S = \frac{\langle (\delta N)^3 \rangle}{\sigma^3} = \frac{VT^3 \chi_3}{(VT^3 \chi_2)^{3/2}},$

kurtosis: $\kappa = \frac{\langle (\delta N)^4 \rangle}{\sigma^4} - 3 = \frac{VT^3 \chi_4}{(VT^3 \chi_2)^2},$

(Kurtosis - 4th moment - “tailiness” of distribution)

$$\text{Kurtosis} \times \text{Variance}^2 \sim \chi^{(4)} / \chi^{(2)}$$

Presence of Critical Point?

Correlation lengths diverge \rightarrow Net-p $\kappa\sigma^2$ diverges

Top 5% central collisions:

Non-monotonic behavior

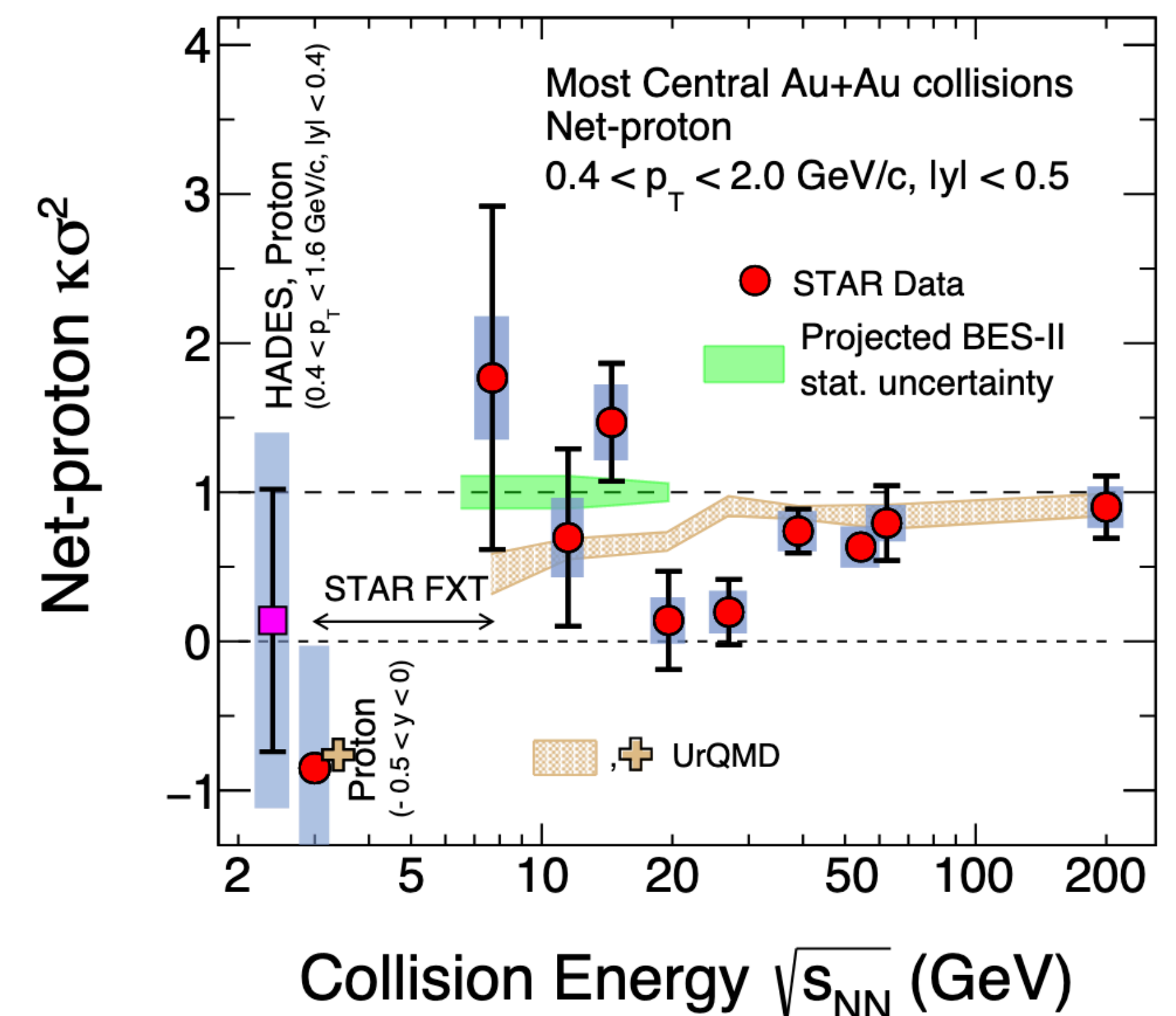
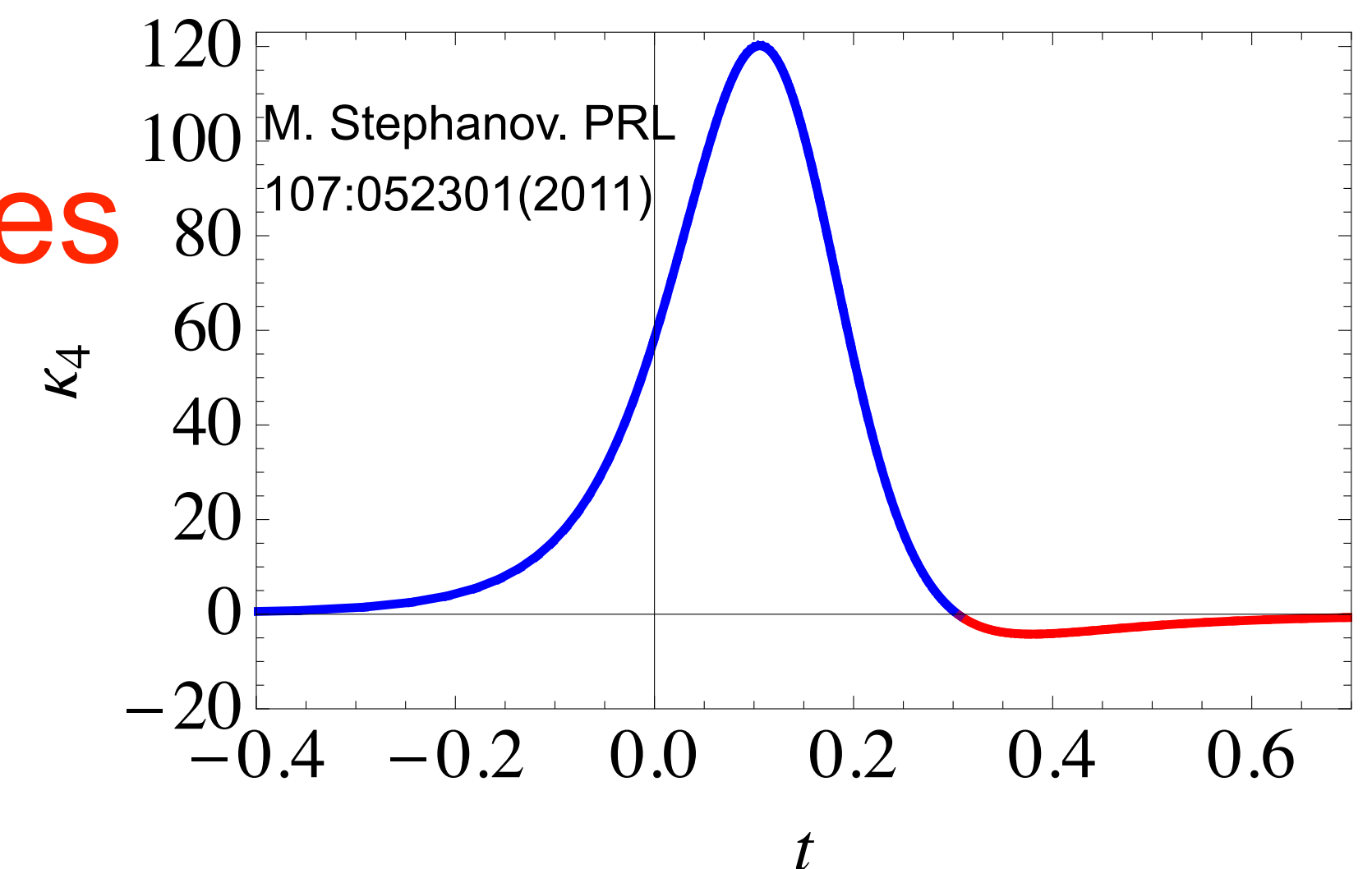
Enhanced p_T range \rightarrow enhanced signal

Not seen in peripheral data

UrQMD (no Critical Point):

shows suppression at lower energies

- due to baryon number conservation



Presence of Critical Point?

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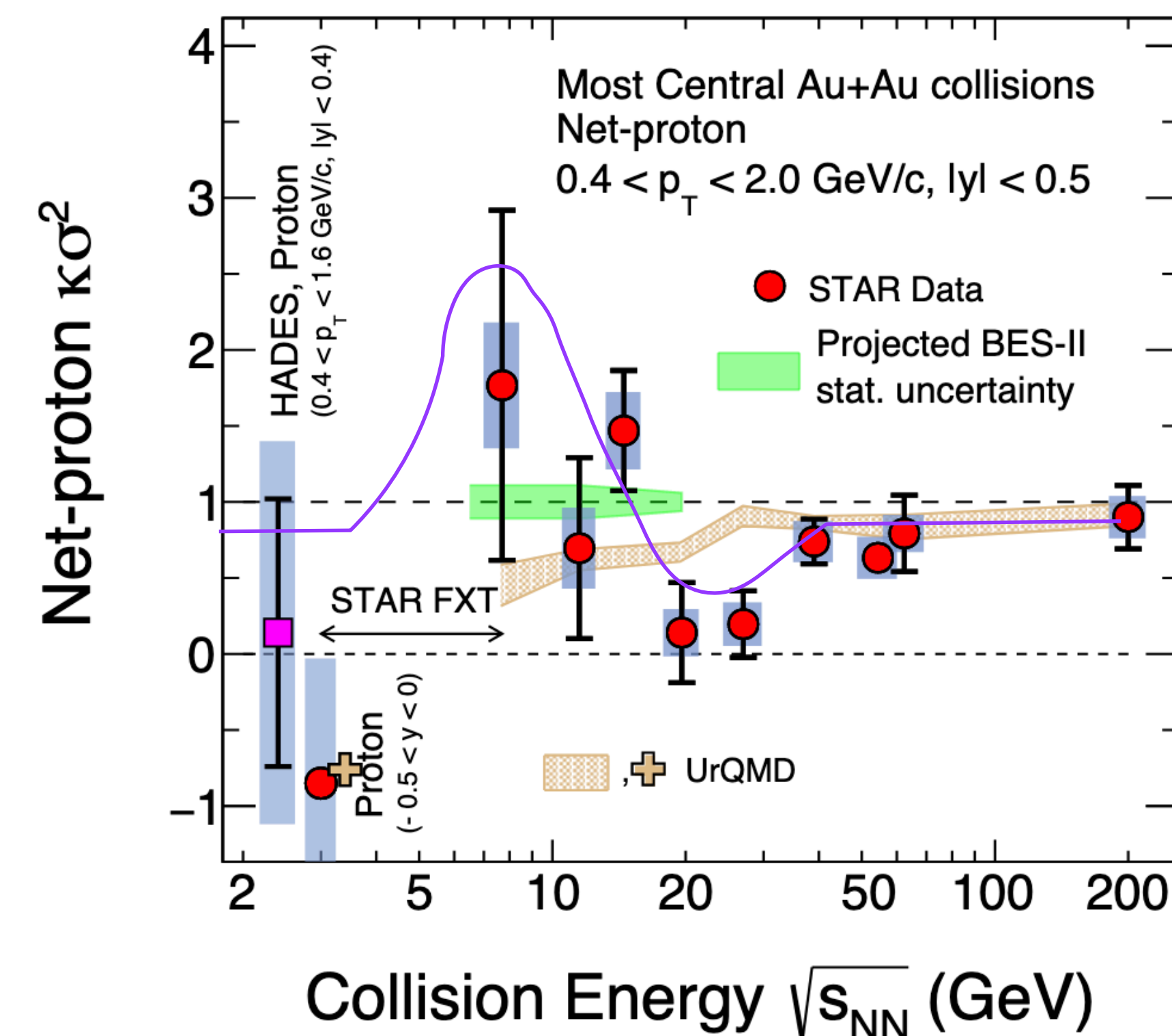
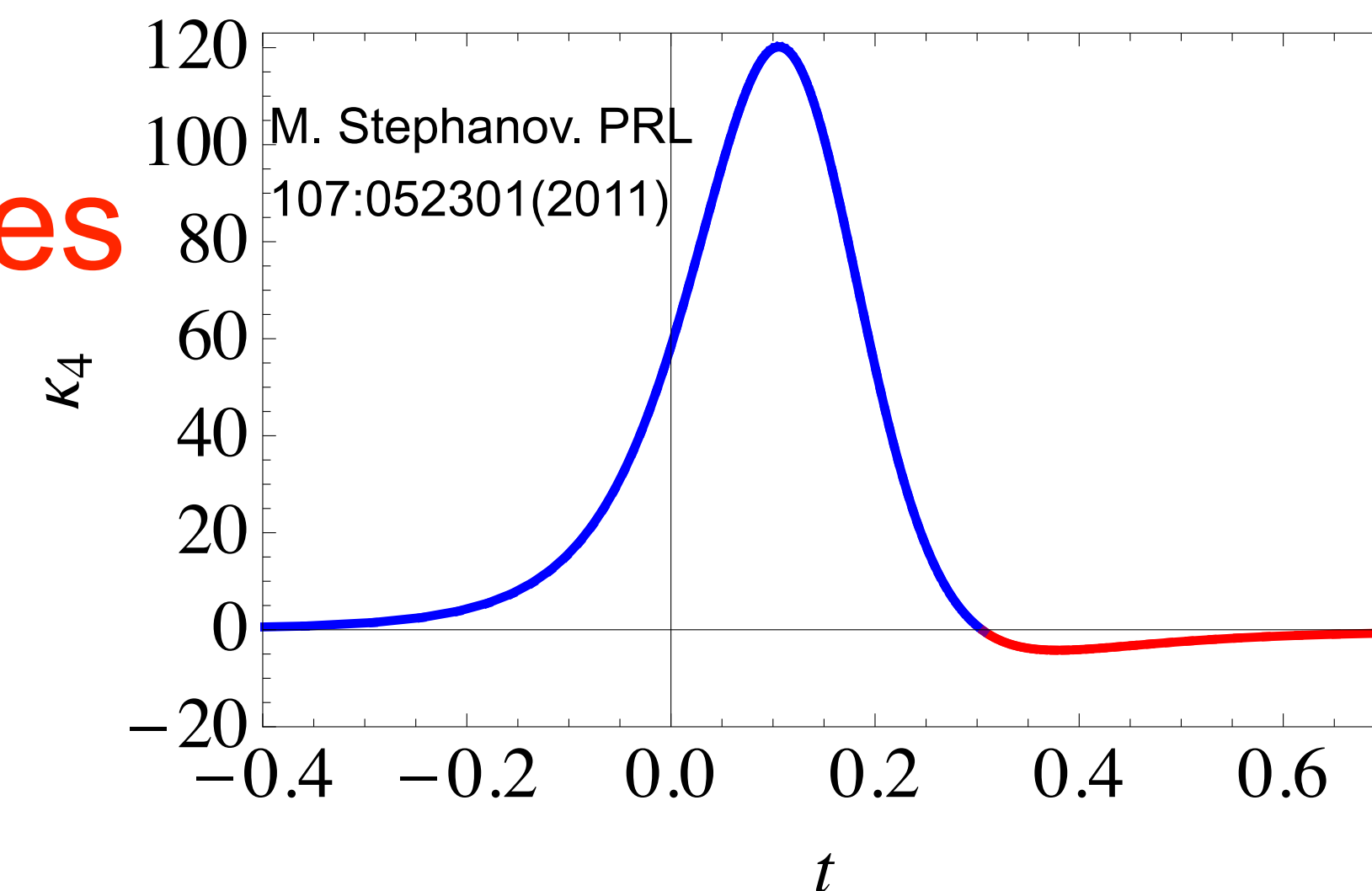
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UrQMD (no Critical Point):

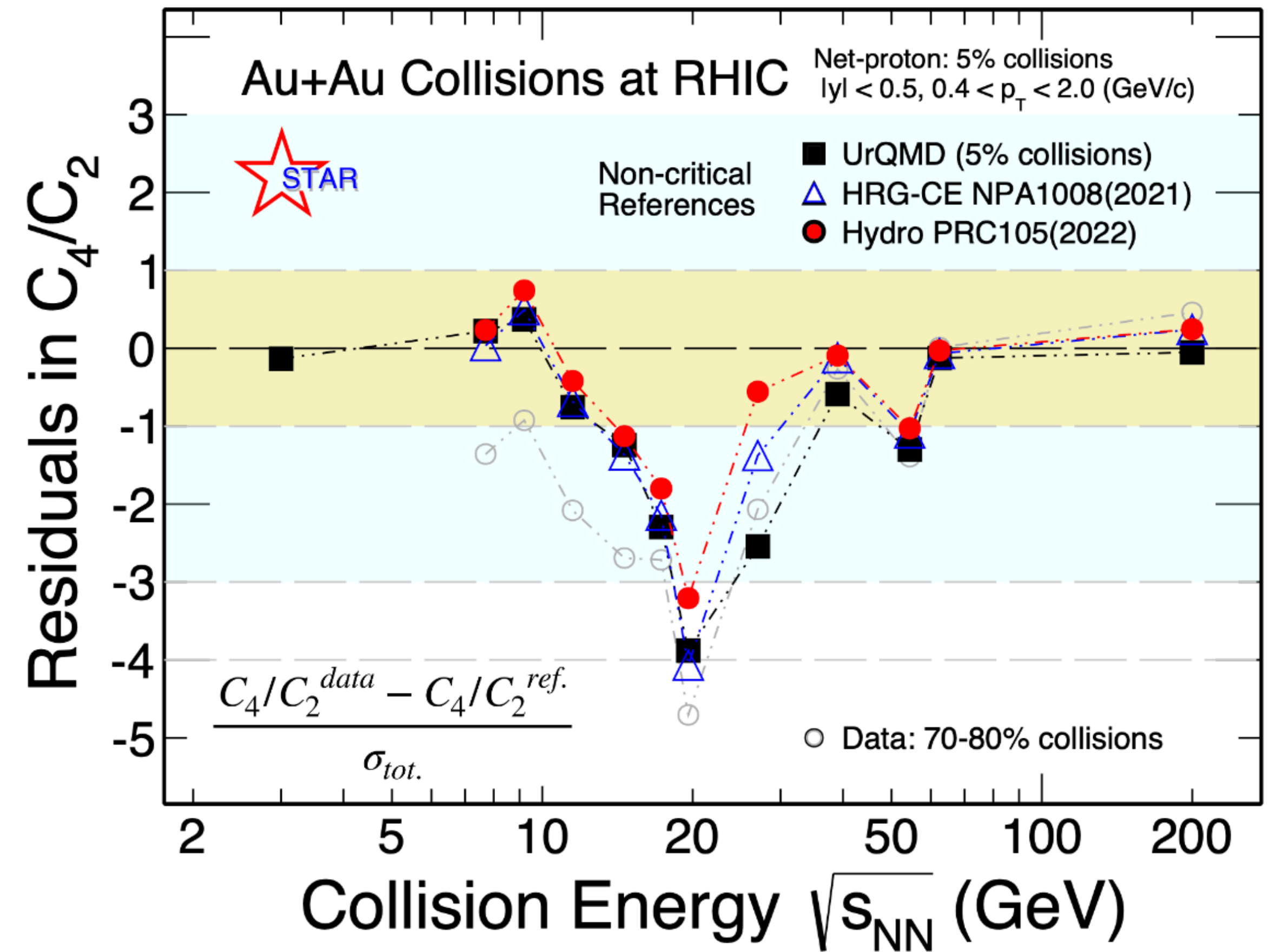
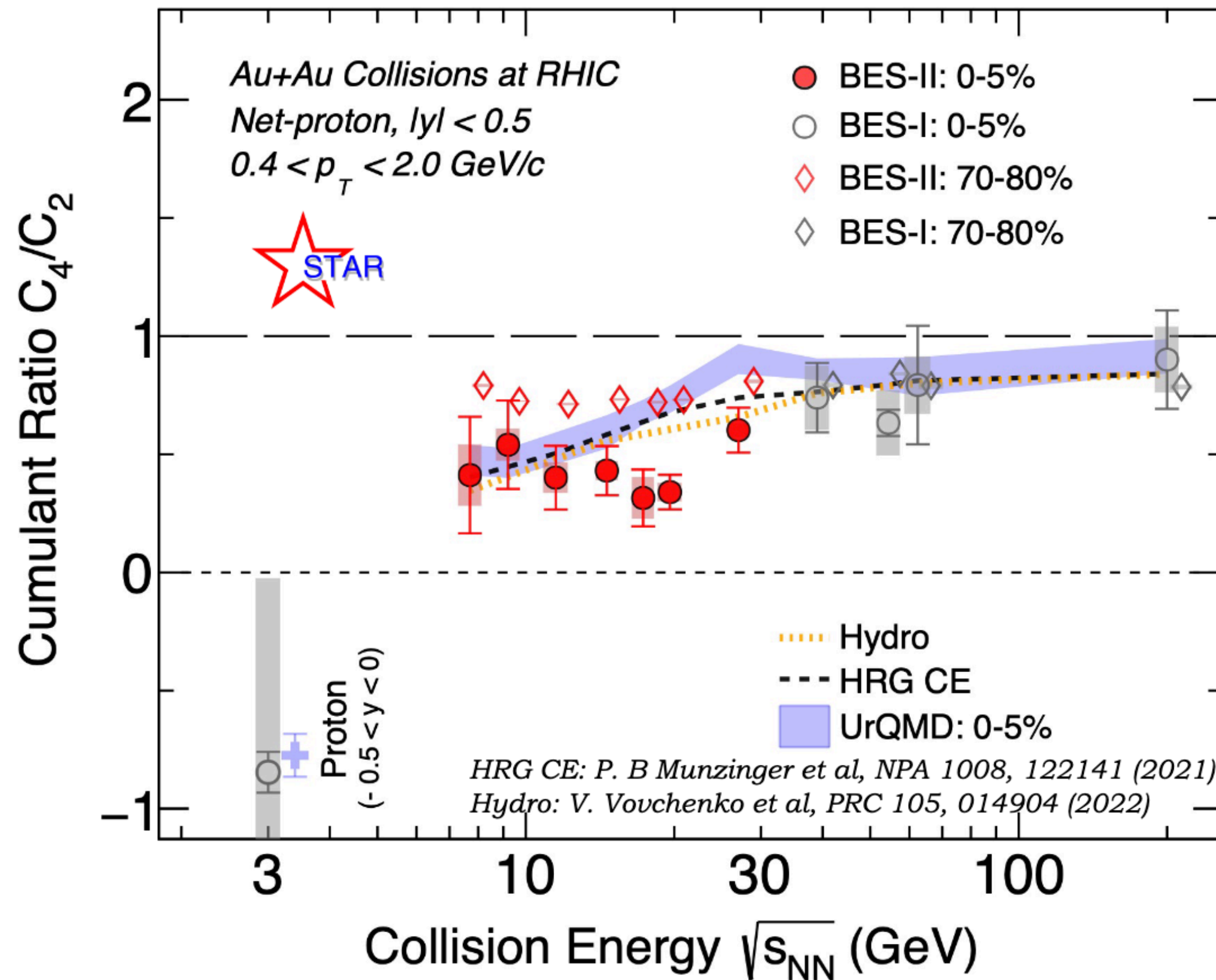
shows suppression at lower energies

- due to baryon number conservation

Hints of Critical fluctuations
More data needed



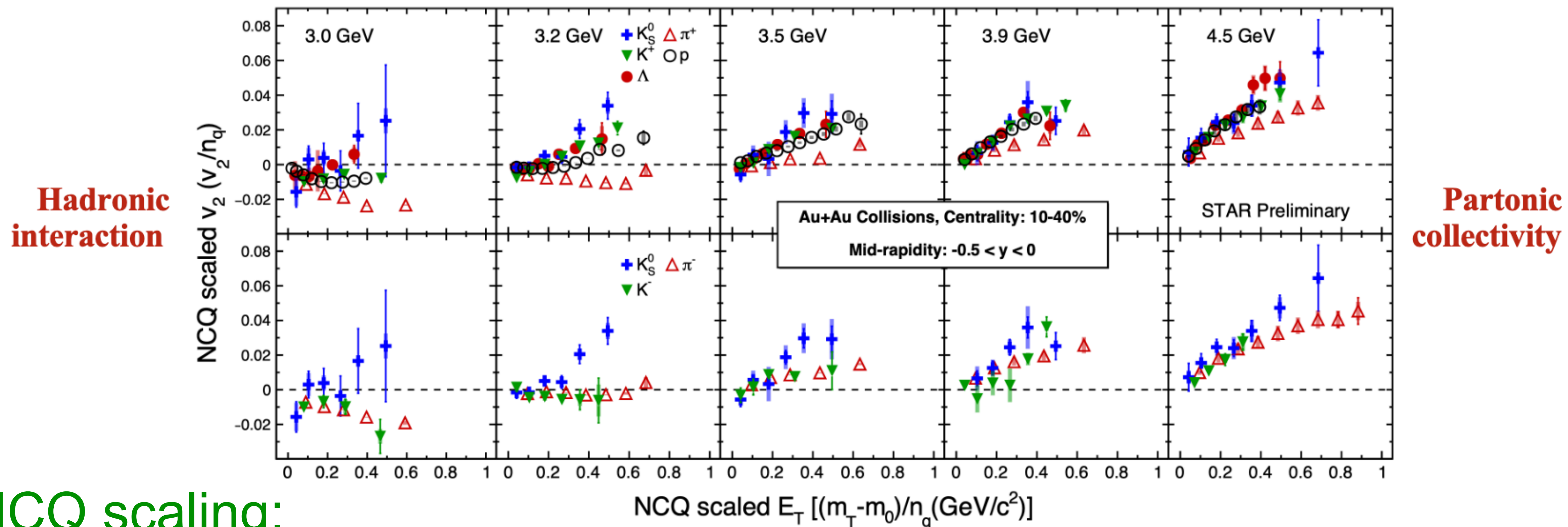
BES-II data released this month



$\kappa\sigma^2$ (C_4/C_2) minimum around ~ 20 GeV comparing to non-CEP models and 70-80% data

Maximum deviation: $3.2 - 4.7\sigma$ at ~ 20 GeV

Disappearance of partonic collectivity



NCQ scaling:

Fails at $\sqrt{s_{NN}} = 3.2$ GeV and lower

Gradually restores up to $\sqrt{s_{NN}} = 4.5$ GeV

Evident from $\sqrt{s_{NN}} = 7.7$ GeV onwards

Partonic:
 $\sqrt{s_{NN}} > 5$ GeV

Hadron dominated:
 $\sqrt{s_{NN}} < 3.2$ GeV

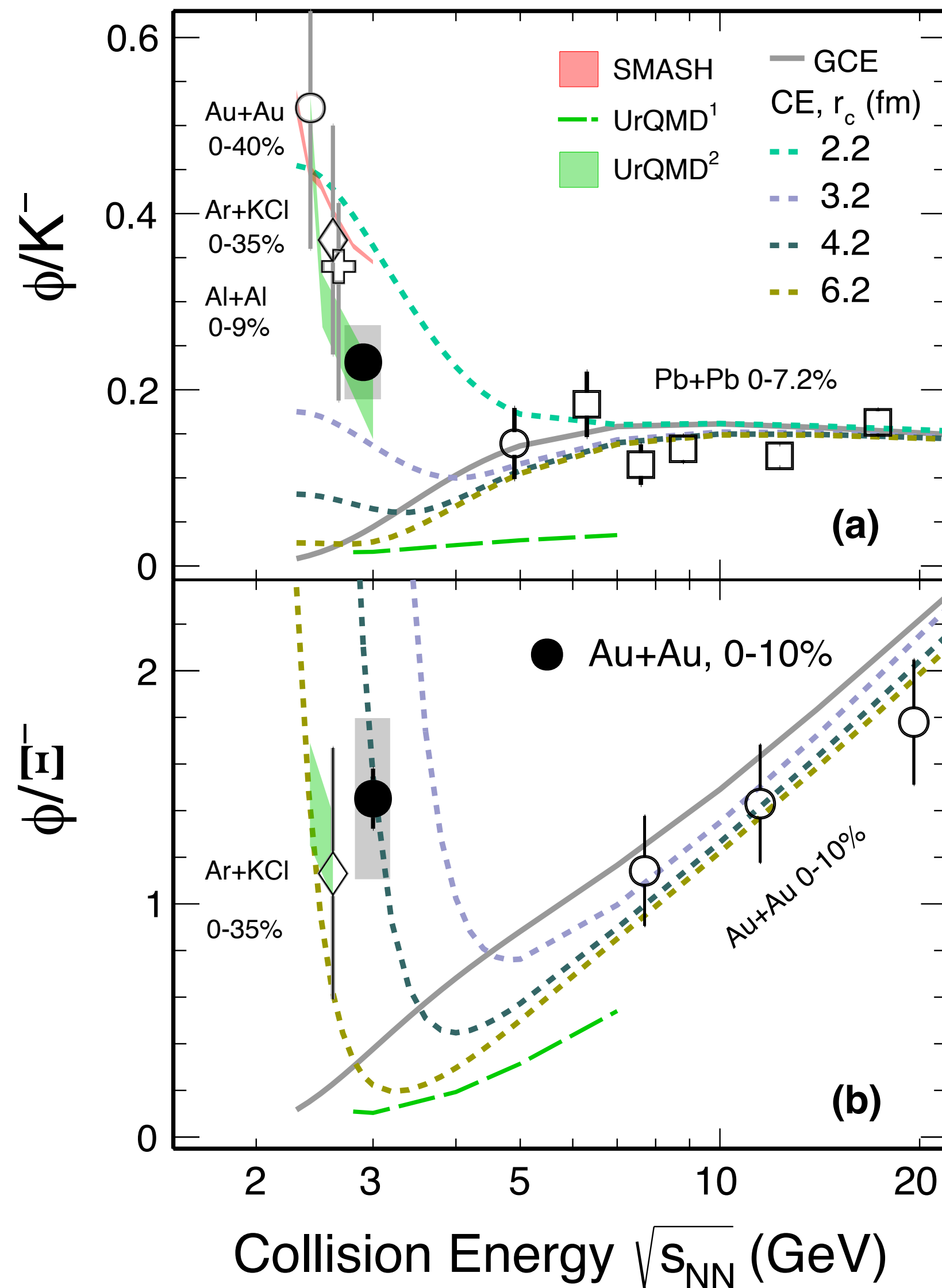
Probing (grand)canonical production

Things change at low $\sqrt{s_{NN}}$

Collision energy:

below threshold for Ξ

very close to threshold for ϕ



Local treatment of strangeness conservation crucial

Small strangeness correlation radius preferred
 $r_c \leq 4.2$ fm

CE cannot simultaneously describe ϕ/K^- and ϕ/Ξ^- ratios. Significant change in strangeness production at this low energy

$T_{ch} = 72.9$ MeV and $\mu_B = 701.4$ MeV

Softening of Equation of State

Fermi-Landau initial conditions with ideal hydro expansion : $c_s^2 = \partial P / \partial \varepsilon$

$c_s^2 = 0$ for a sharp phase transition

Softest Point: minimum in c_s^2

$$\frac{dn}{dy} = \frac{Ks_{NN}^{1/4}}{\sqrt{2\pi\sigma_y^2}} e^{-\frac{y^2}{2\sigma_y^2}} \quad \sigma_y^2 = \frac{8}{3} \frac{c_s^2}{1-c_s^4} \ln\left(\frac{\sqrt{s}}{2m_N}\right)$$

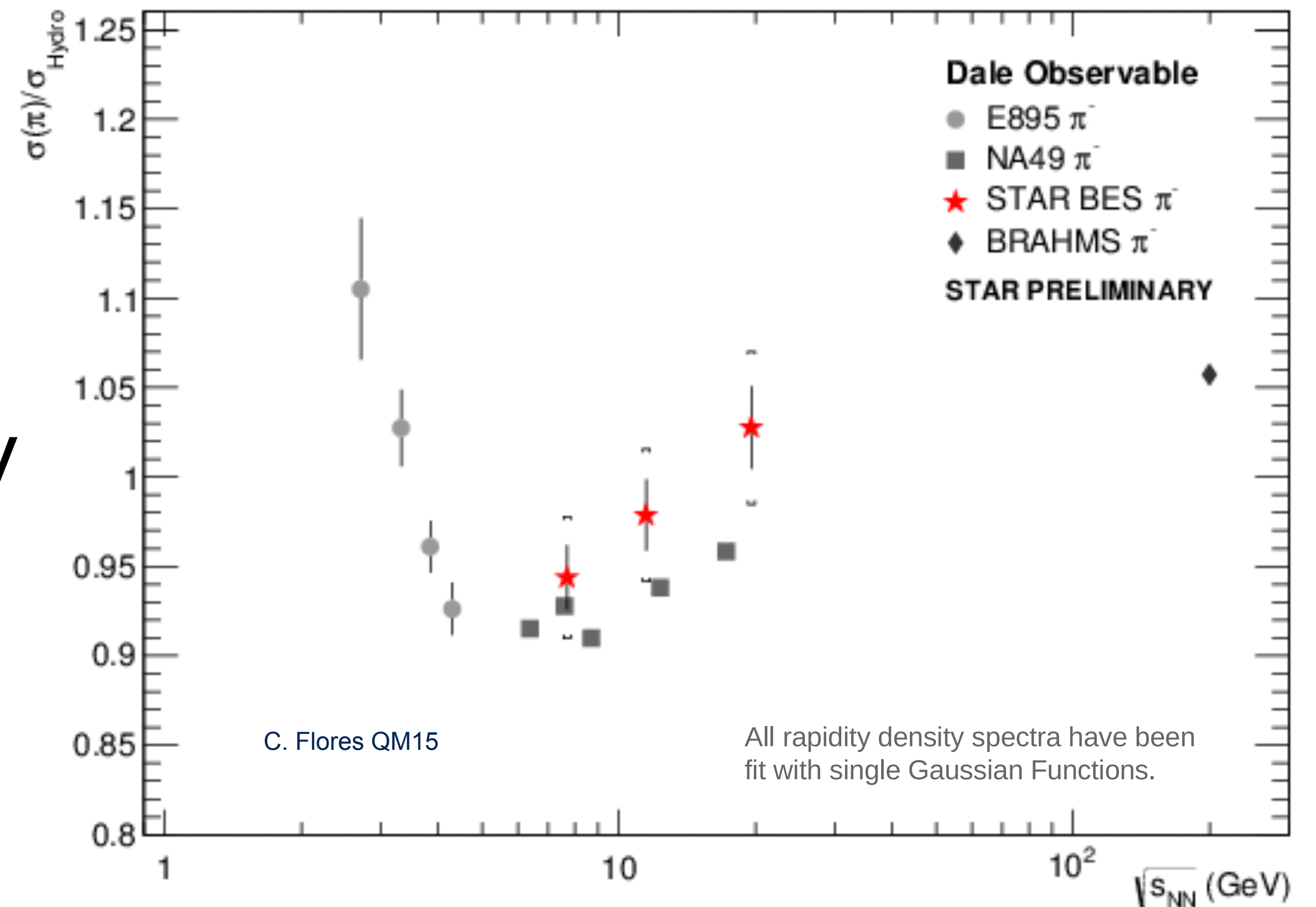
Minimum observed at $\sqrt{s} = \sim 7$ GeV

Minimum in the speed of sound?

$$c_s^2 \sim 0.26$$

Indication of softening
of EoS?

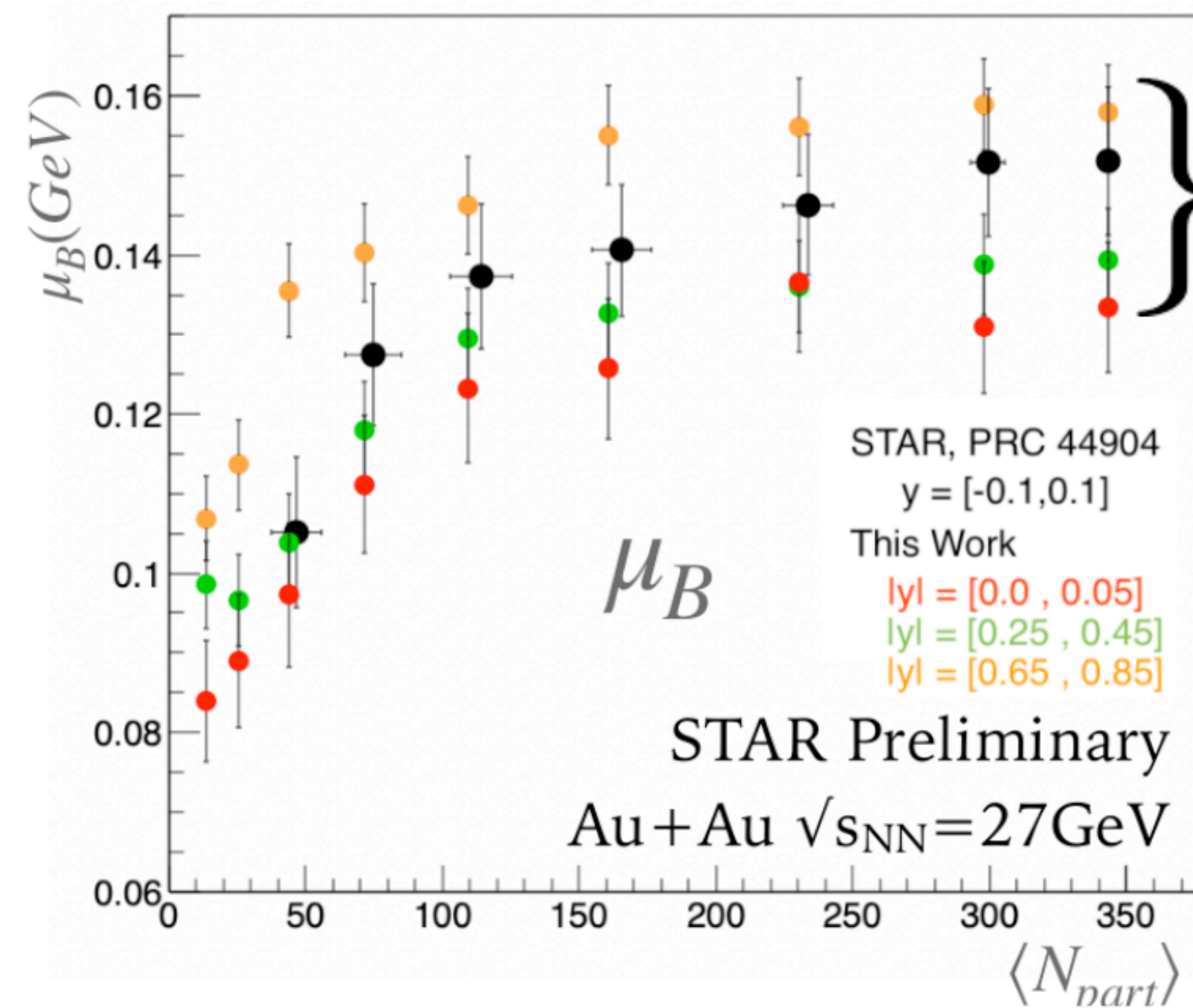
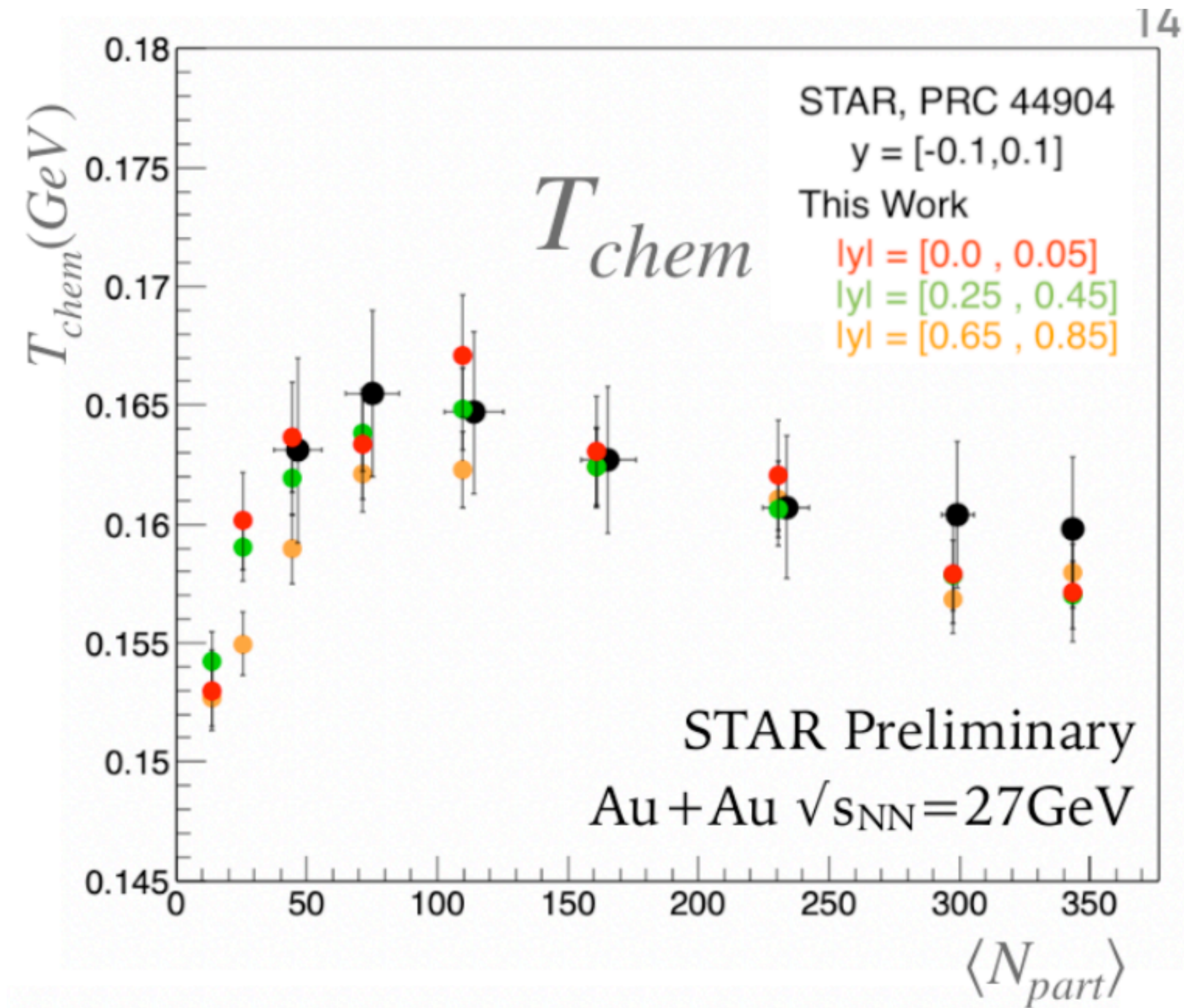
Confirm c_s in other ways?



E895: J. L. Klay et al, PRC 68, 05495 (2003)
NA49: S. V. Afanasiev et al. PRC 66, 054902 (2002)
BRAHMS: I.G. Bearden et al., PRL 94, 162301

Varying trajectory through the phase diagram?

With RHIC BES-II statistics and larger STAR TPC acceptance can explore rapidity dependence



Higher rapidity:

larger μ_B ,

similar T_{ch}

Next step: Compare mid-rapidity/low $\sqrt{s_{NN}}$ and high rapidity/high $\sqrt{s_{NN}}$

Chemical freeze-out parameters match but initial conditions differ.
Can we see the difference imprinted elsewhere?

Executive summary of bulk studies

Energy density of fireball way above that where hadrons can exist

Initial temperature of fireball way above that where hadrons can exist

We create a new state of matter in HI collisions - the QGP. Smooth transition from RHIC to LHC

QGP has quark and gluon degrees of freedom and flows like an almost “perfect” liquid, but there are significant hadronic final state interactions

No clear evidence yet for a Critical Point, but strong evidence that hadronic state dominates at low energies

Come back tomorrow to discuss more on how we are learning about the QGP from studying how partons interact with it?